

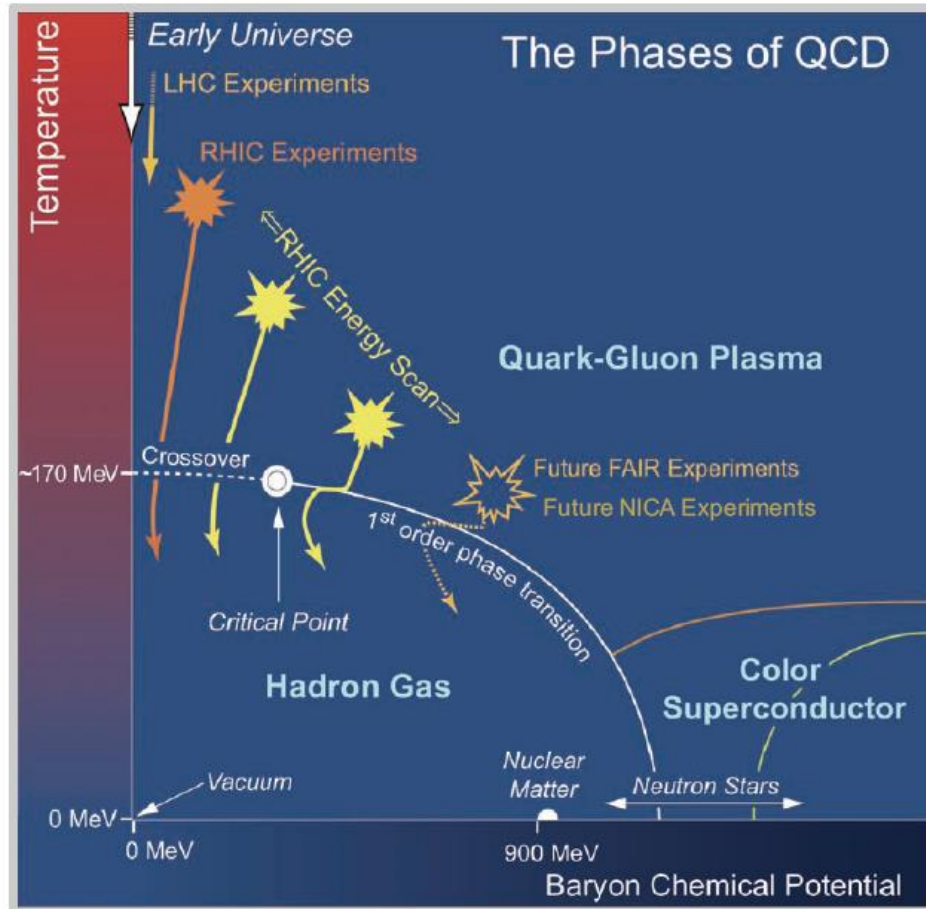
# Higher-order diagonal cumulants of $(\Lambda+K)$ -multiplicity distributions: Au+Au 27 GeV (Run18)

Changfeng Li and Nihar Sahoo

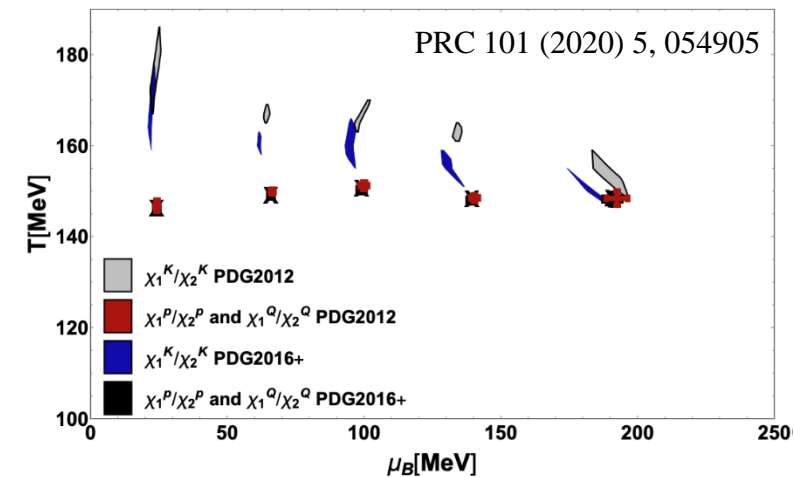
Shandong University, Qingdao, China



# Motivation

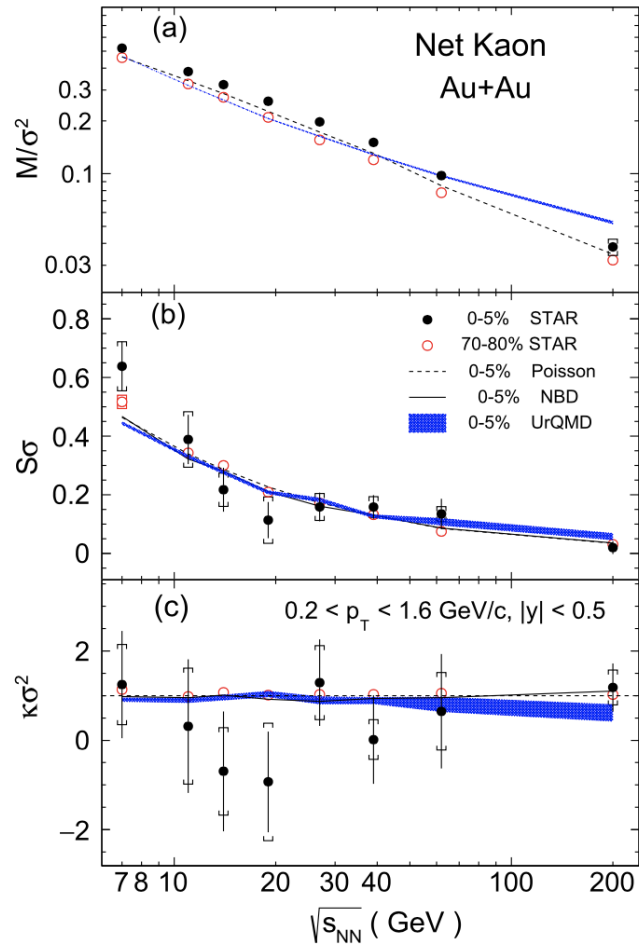


- Goal of the RHIC BES program
  - To explore the QCD Phase diagram and search for the QCD Critical Point
- Recently, many theoretical attempts have been made to extract freezeout (FO) parameters using higher order cumulants measurements
- And to understand strangeness dependent chemical FO parameters

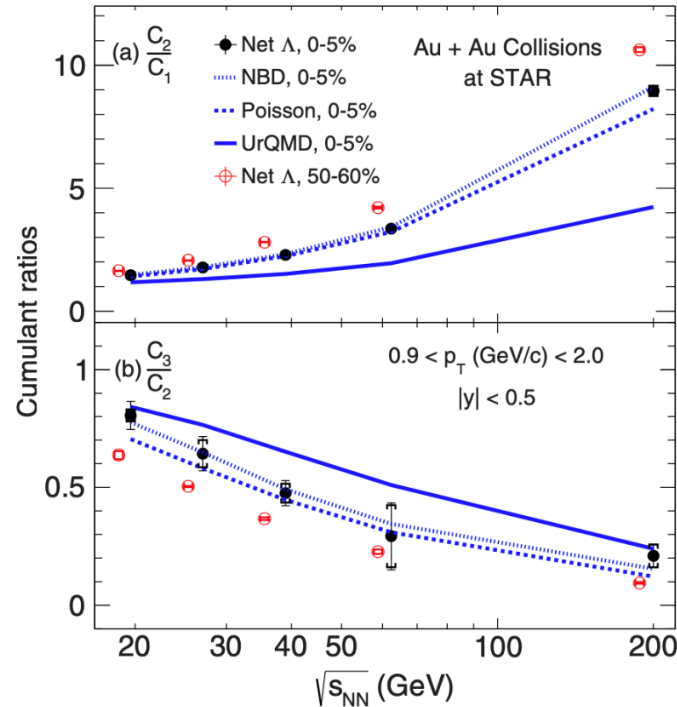


# STAR BES-I Net-Kaon and Net-Lambda results

Net-Kaon: PLB 785 (2018) 551



Net-Lambda: PRC 102 (2020) 2, 024903



- We plan to measure net-(Kaon+Lambda) multiplicity distributions for BES program.
- Net-(Kaon+Lambda) can be approximately considered as net-strangeness.
- Differential and precision measurements of net-K, net- $\Lambda$ , and net-(K+ $\Lambda$ ) are needed to understand the critical fluctuations and strangeness chemical freeze-out parameters at the BES energies

# Thermodynamic susceptibilities and cumulants

$$C_X^m = VT^3 \chi_X^m(T, \mu)$$

- X is conserved charge such as net-electric charge(Q)  
net-baryon number(B) and net-strangeness(S)
- $C_X^m$  is cumulant
- V is volume of the system.
- We can hardly know the volume or sometimes we want to compare thermodynamic susceptibilities of different system, so we use the ratio of susceptibilities to remove the volume term

Different order of cumulants

$$C_1 = \langle N \rangle$$

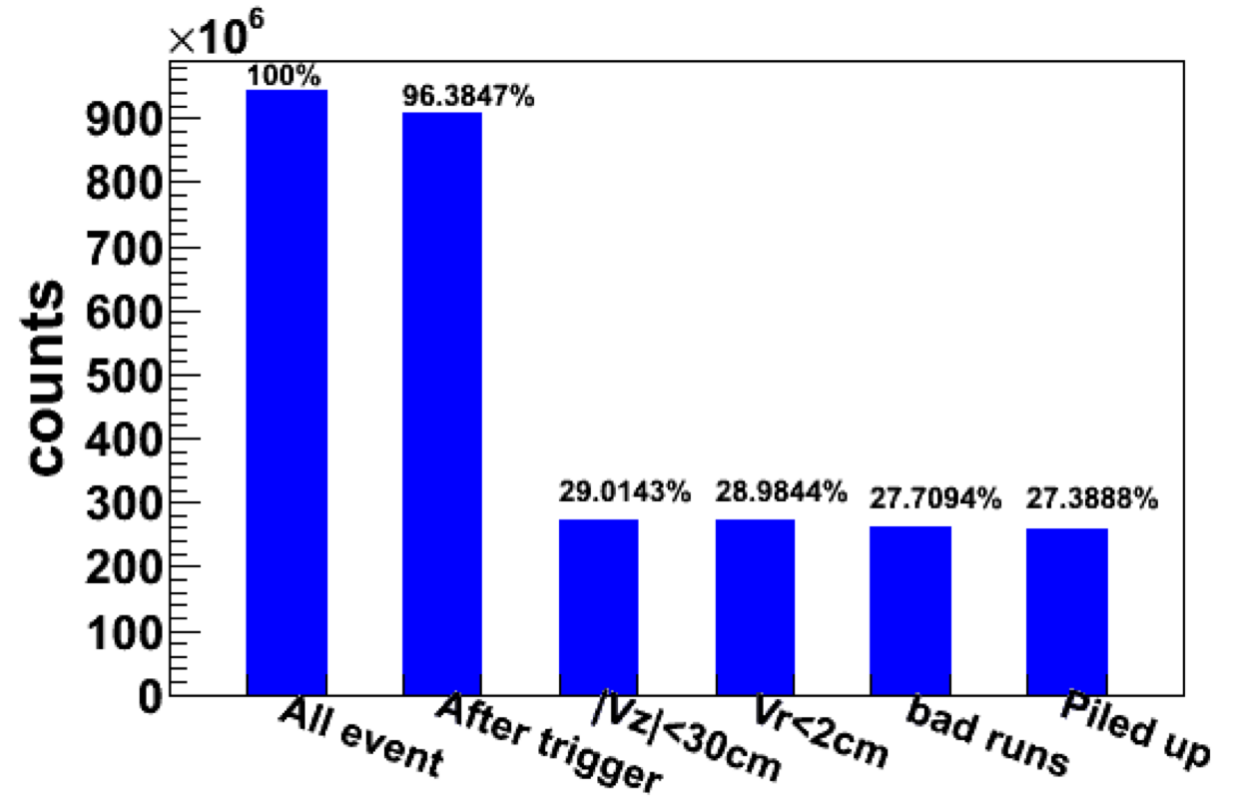
$$C_2 = \langle (\delta N)^2 \rangle$$

$$C_3 = \langle (\delta N)^3 \rangle$$

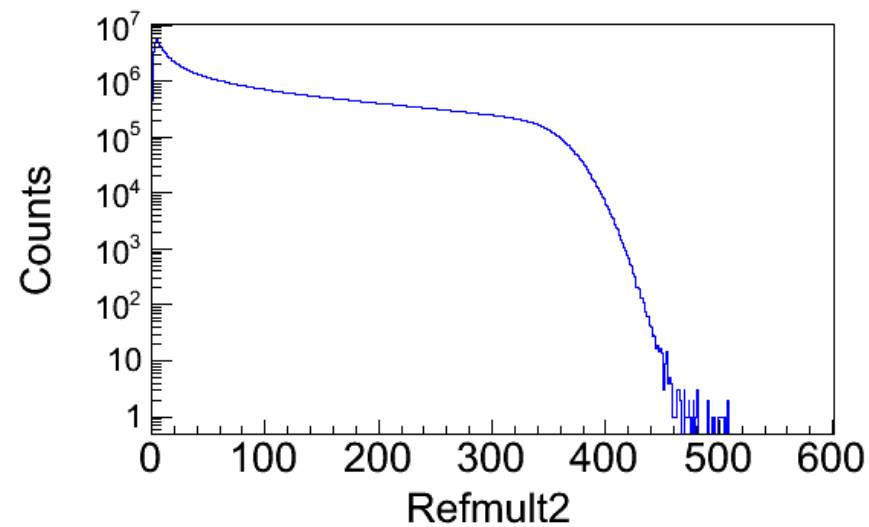
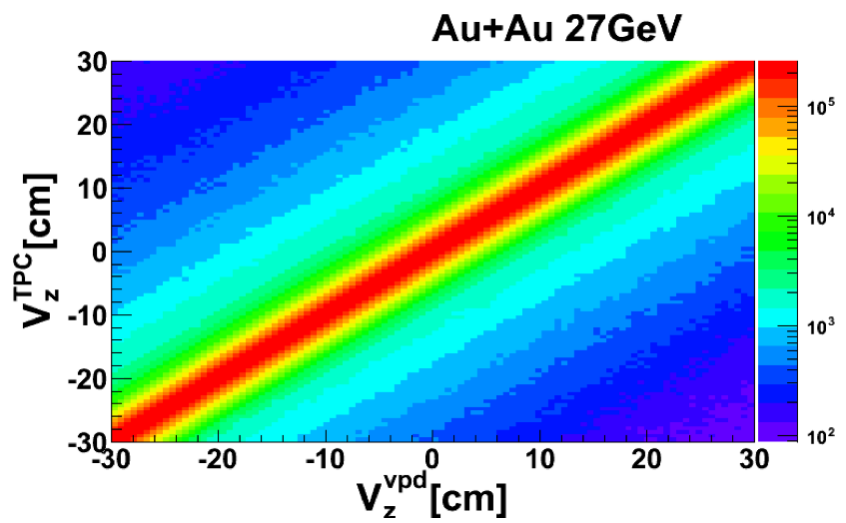
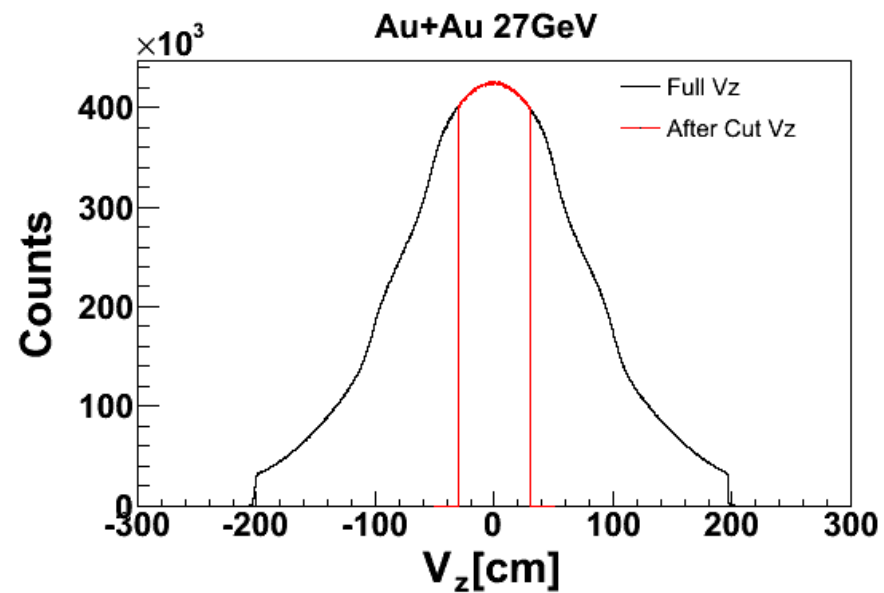
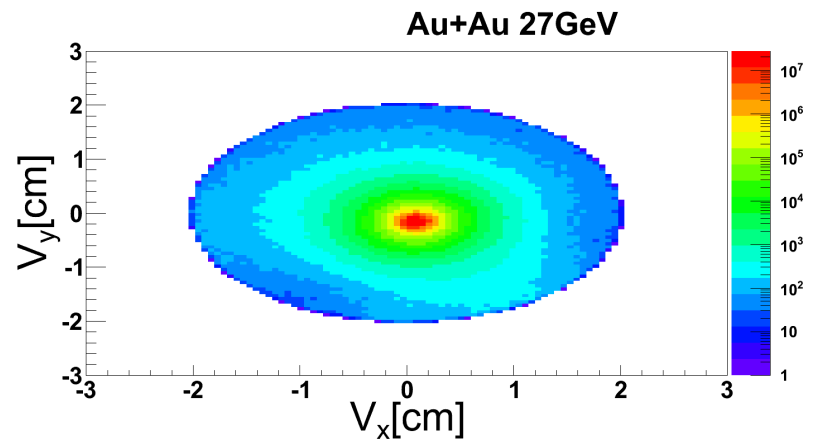
$$C_4 = \langle (\delta N)^4 \rangle - 3\langle (\delta N)^2 \rangle^2$$

# New 27 GeV (Run18) dataset

- Trigger setup name = 27GeV\_production\_2018
- Production = P19ib
- Trigger Ids = 610001, 610011, 610021, 610031, 610041, 610051
- $|V_z| < 30$  cm
- $V_r < 2$  cm



# Event QA



# QA: Bad run rejection and Pileup events removal

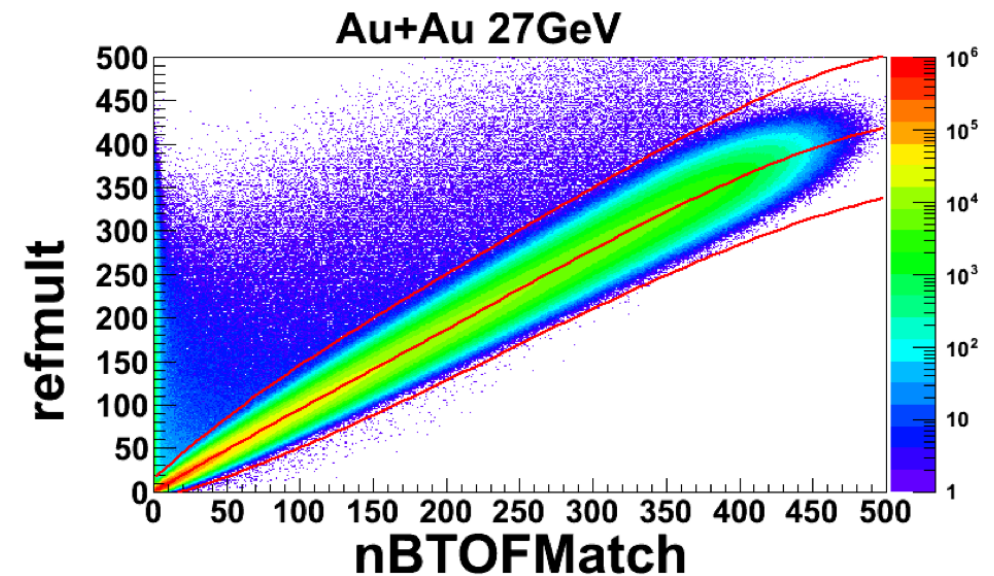
- Bad runs are selected based on the run-by-run check on  $\langle \text{eta} \rangle$ ,  $\langle \text{pT} \rangle$ ,  $\langle \text{Refmult} \rangle$ ,  $\langle \text{Tofmult} \rangle$ ,  $\langle \text{TofMatch} \rangle$ , etc.
- Outliers are selected those are  $5\sigma$  away from the local mean

Bad run list:

```
19130085 19131009 19131010 19131012 19131016 19131037 19131039 19131040
19131041 19131042 19131045 19131050 19131057 19132006 19132016 19132029
19132031 19132038 19132048 19132063 19133018 19133023 19134011 19134017
19134044 19135011 19135038 19135039 19135040 19136001 19136005 19136009
19136012 19136013 19136014 19137001 19137003 19137004 19137008 19137011
19137013 19137020 19137022 19137028 19137029 19137050 19137051 19137052
19137056 19137057 19138004 19138008 19138010 19139022 19139026 19139032
19140014 19140016 19140040 19141004 19141008 19141019 19141029 19142005
19143008 19143009 19143010 19143011 19143012 19143013 19143014 19143015
19143016 19143017 19144019 19144038 19146007 19146016 19147008 19147009
19147010 19147014 19147015 19147016 19149035 19156032 19156041 19156044
19156045 19157013 19158009 19158013 19159025 19160018 19161019 19162002
19162005 19165018 19165020 19167026 19167042 19147007 19147029
```

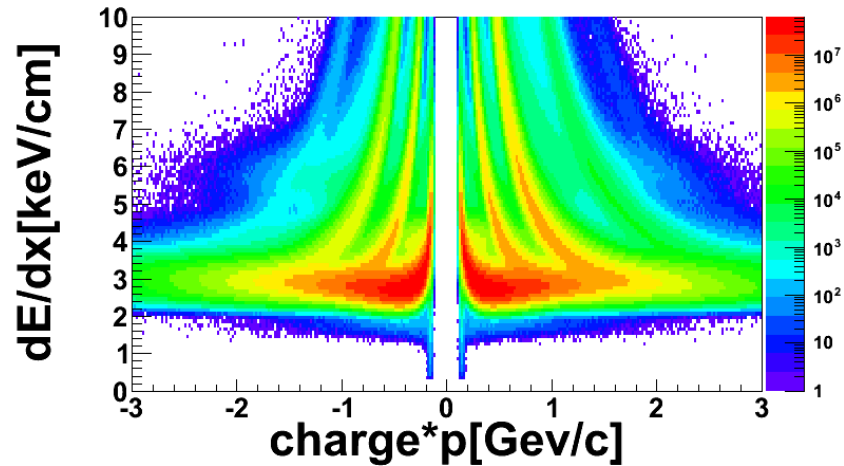
Refmult vs. TofMatch is used to reject the pileup events.

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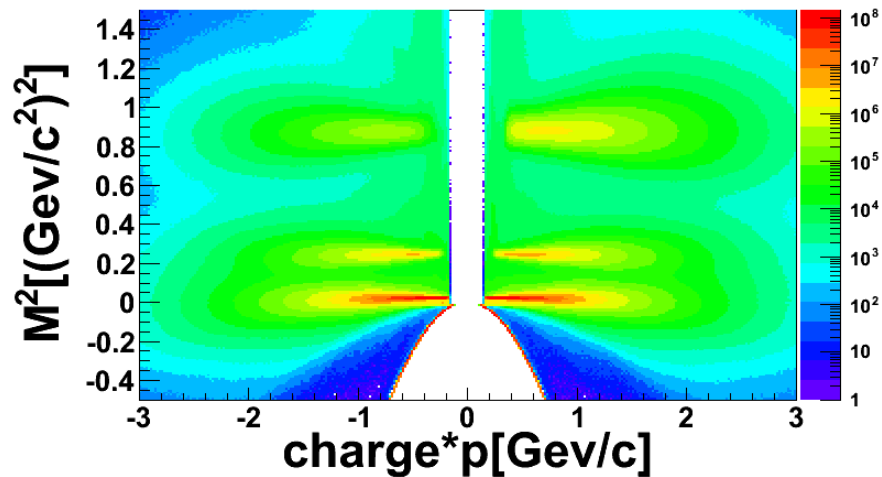


# Track cuts and $K^+$ and $K^-$ identification using TPC and TOF

## TPC



## TPC + TOF



## Track cuts:

- $p_T$  range: 0.4 to 1.6 GeV/c
- $|y| < 0.5$
- $n\text{HitsFit} \geq 15$
- $n\text{HitsFit}/n\text{HitMax} \geq 0.52$
- $n\text{Hitdedx} > 5$
- $\text{DCA} < 1 \text{ cm}$
- TPC:  $|n\sigma_{K\text{aon}}| < 2$  and  $|n\sigma_{\pi}| > 2$
- TOF:  $0.15 < m^2 < 0.4 \text{ GeV}^2/c^4$
- $0.4 < p_T < 1.6 \text{ GeV}/c$



## Track cuts to reconstruct $\Lambda$

In this analysis, we measure both  $K^+$ ,  $K^-$ ,  $\Lambda$ , and anti- $\Lambda$  for Net-( $K^+$   $\Lambda$ ) multiplicity distribution:

- Kaons ( $K^+$  and  $K^-$ ) are identified using TPC and TOF within  $0.4 < p_T < 1.6$  GeV/c
- Proton and pion are used for  $\Lambda$ /anti- $\Lambda$  reconstruction

Track cut:

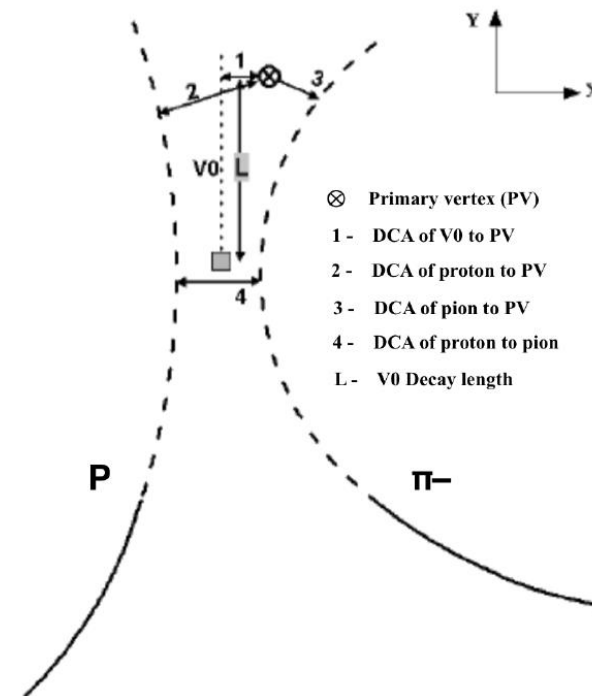
- $p_T > 0.05$  GeV/c
- $|\text{Eta}| < 1.0$
- $n\text{HitsFit} > 15$
- $n\text{HitsFit}/n\text{HitsMax} > 0.52$
- $N\text{sigma} < 2.0$

(Based on net- $\Lambda$  published results)

# Topological cuts for $\Lambda$ reconstruction

1. DCA of V0 to Primary Vertex (PV)
2. DCA of proton to PV
3. DCA of pion to PV
4. DCA of proton to pion
5. Decay Length (L)

DCA (P to PV)	>0.5cm
DCA ( $\pi$ to PV)	>1.5cm
DCA (P to $\pi$ )	<0.6cm
DCA (V0 to PV)	<0.5cm
Decay Length (L)	>3.0cm
Pointing away from PV r.p	>0
Pt	$0.4 < Pt(\text{GeV}/c) < 1.6$
Eta	$ \text{rap}  < 0.5$
LambdaMass	$1.112 < \text{LambdaMass} < 1.12$



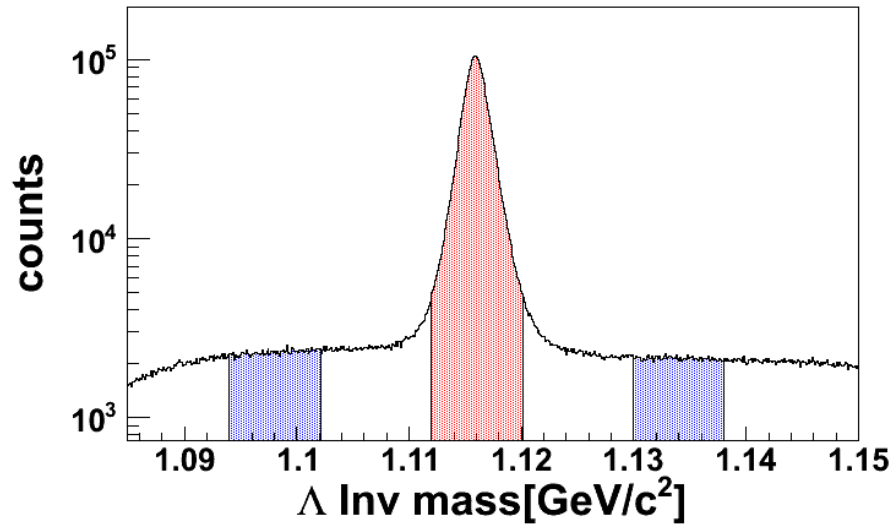
# $\Lambda$ and anti- $\Lambda$ reconstruction: Invariant Mass

Signal mass window: 1.112 - 1.12  $\text{GeV}/c^2$

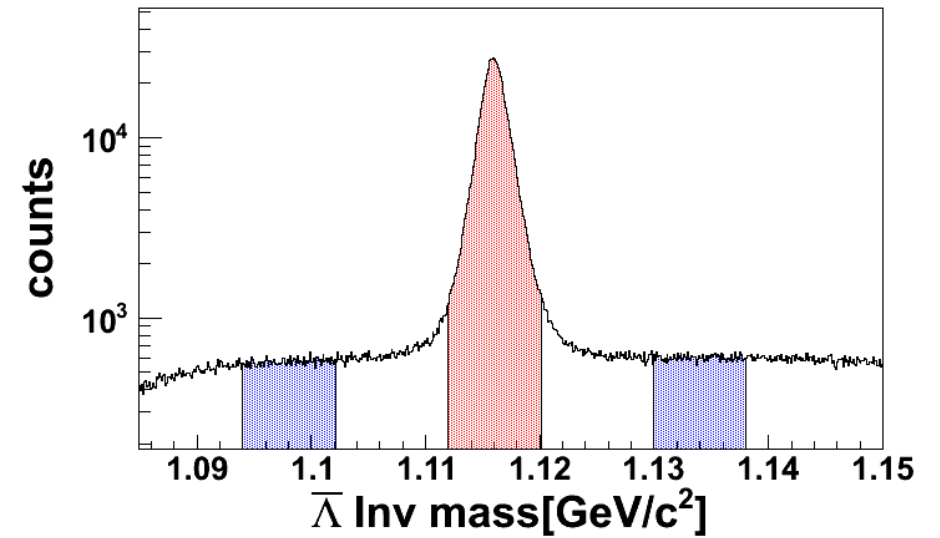
left side: 1.094 - 1.102  $\text{GeV}/c^2$

right side: 1.13 - 1.138  $\text{GeV}/c^2$

Centrality 0-5%



Centrality 0-5%



## Net-K Net- $\Lambda$ and Net-(K+ $\Lambda$ ) definition

$K^+$	contains $u\bar{s}$	strangeness is +1
$K^-$	contains $\bar{u}s$	strangeness is -1
$\Lambda$	contains $uds$	strangeness is -1
anti- $\Lambda$	contains $\bar{u}\bar{d}\bar{s}$	strangeness is +1

We plan to calculate net  $\bar{s}$

$$\text{Net-K} = \Delta N_K = N_{K^+} - N_{K^-}$$

$$\text{Net-}\Lambda = \Delta N = N_{\text{anti-}\Lambda} - N_{\Lambda}$$

$$\begin{aligned} \text{Net-(K+}\Lambda) &= \Delta N_{(K+\Lambda)} \\ &= (N_{K^+} + N_{\text{anti-}\Lambda}) - (N_{K^-} + N_{\Lambda}) \end{aligned}$$

$$N_{K^+} = \text{Total number of } K^+$$

$$N_{K^-} = \text{Total number of } K^-$$

$$N_{\Lambda} = \text{Total number of } \Lambda$$

$$N_{\text{anti-}\Lambda} = \text{Total number of anti-}\Lambda$$

## Track by track efficiency correction

$$\langle Q \rangle_c = \langle q_{(1,1)} \rangle_c$$

$$\langle Q^2 \rangle_c = \langle q_{(1,1)}^2 \rangle_c + \langle q_{(2,1)} \rangle_c - \langle q_{(2,2)} \rangle_c$$

$$\langle Q^3 \rangle_c = \langle q_{(1,1)}^3 \rangle_c + 3 \langle q_{(1,1)} q_{(2,1)} \rangle_c - 3 \langle q_{(1,1)} q_{(2,2)} \rangle_c + \langle q_{(3,1)} \rangle_c - 3 \langle q_{(3,2)} \rangle_c + 2 \langle q_{(3,3)} \rangle_c$$

$$\langle Q^4 \rangle_c = \langle q_{(1,1)}^4 \rangle_c + 6 \langle q_{(1,1)}^2 q_{(2,1)} \rangle_c - 6 \langle q_{(1,1)}^2 q_{(2,2)} \rangle_c + 4 \langle q_{(1,1)} q_{(3,1)} \rangle_c + 3 \langle q_{(2,1)}^2 \rangle_c$$

$$+ 3 \langle q_{(2,2)}^2 \rangle_c - 12 \langle q_{(1,1)} q_{(3,2)} \rangle_c + 8 \langle q_{(1,1)} q_{(3,3)} \rangle_c - 6 \langle q_{(2,1)} q_{(2,2)} \rangle_c$$

$$+ \langle q_{(4,1)} \rangle_c - 7 \langle q_{(4,2)} \rangle_c + 12 \langle q_{(4,3)} \rangle_c - 6 \langle q_{(4,4)} \rangle_c$$

where

$$q_{(r,s)} = q_{(a^r/p^s)} = \sum_{i=1}^M (a_i^r / p_i^s) n_i$$

We use  $n_i=1$ ,

$a_i$  equal to 1 or -1

$p_i$  is efficiency

$M$  is track number of one event

For detail you can read this paper:

<https://journals.aps.org/prc/abstract/10.1103/PhysRevC.95.064912>

# QM2022 Results

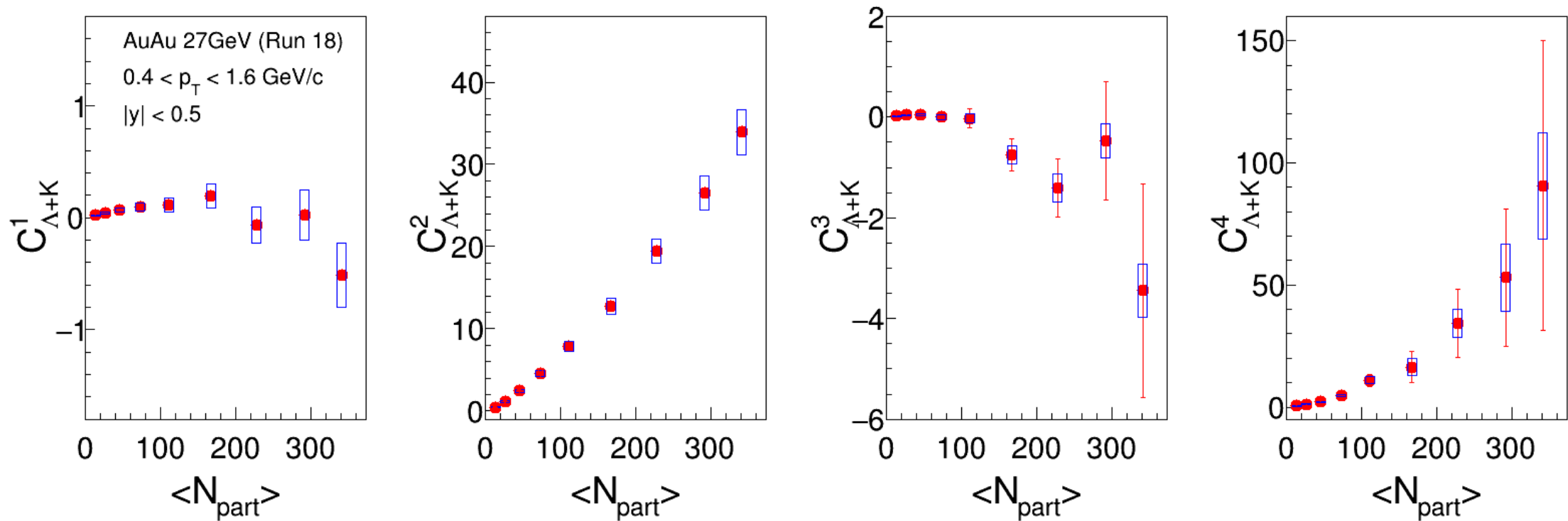
# Cumulants of Net-(K+ $\Lambda$ ) multiplicity distributions

$$\text{Net-(}\Lambda+\text{K)} \equiv \Delta N_{(\Lambda+\text{K})} = (N_{\text{anti-}\Lambda} + N_{\text{K}^+}) - (N_{\Lambda} - N_{\text{K}^-})$$

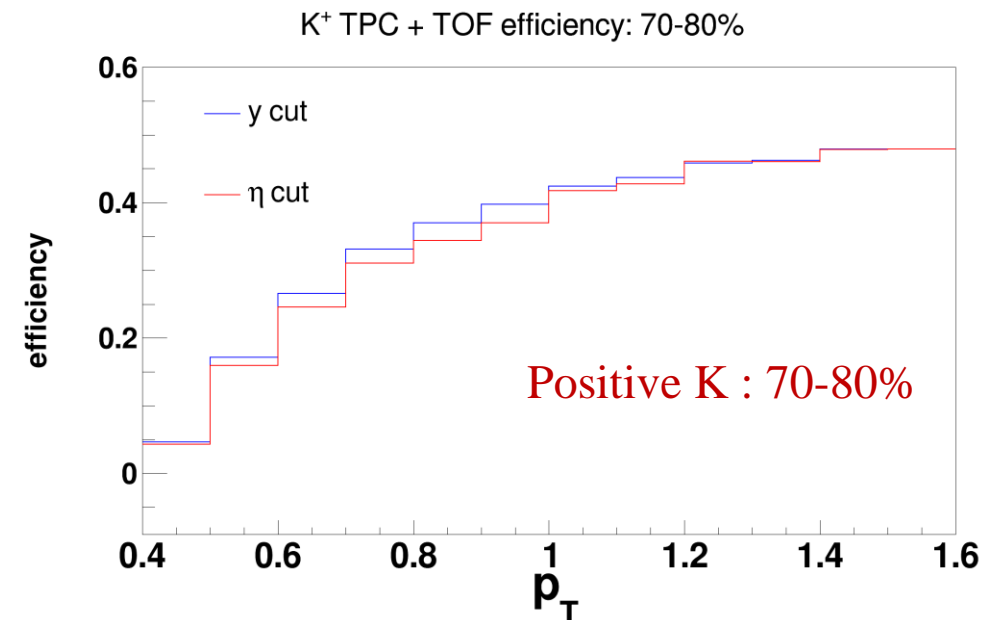
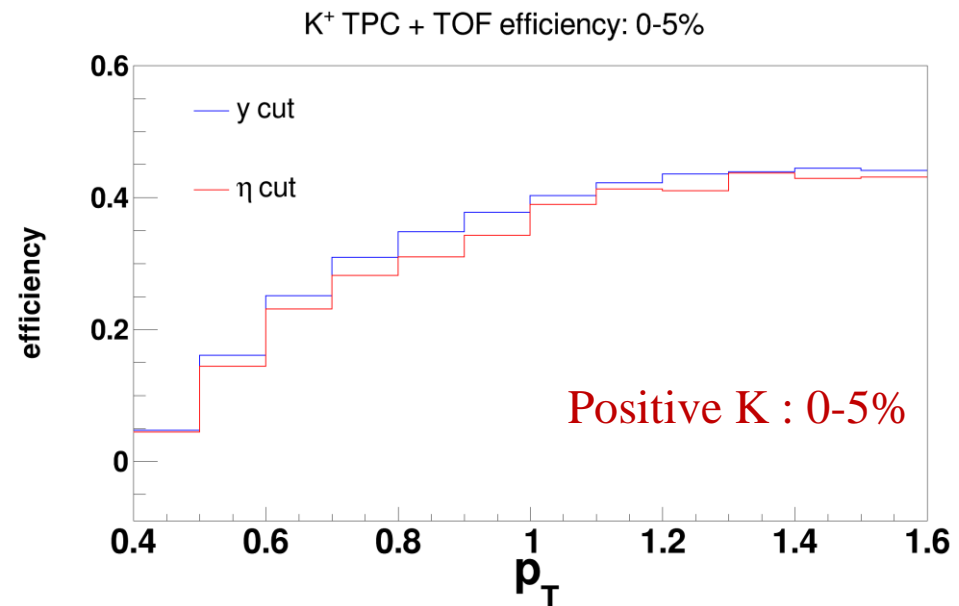
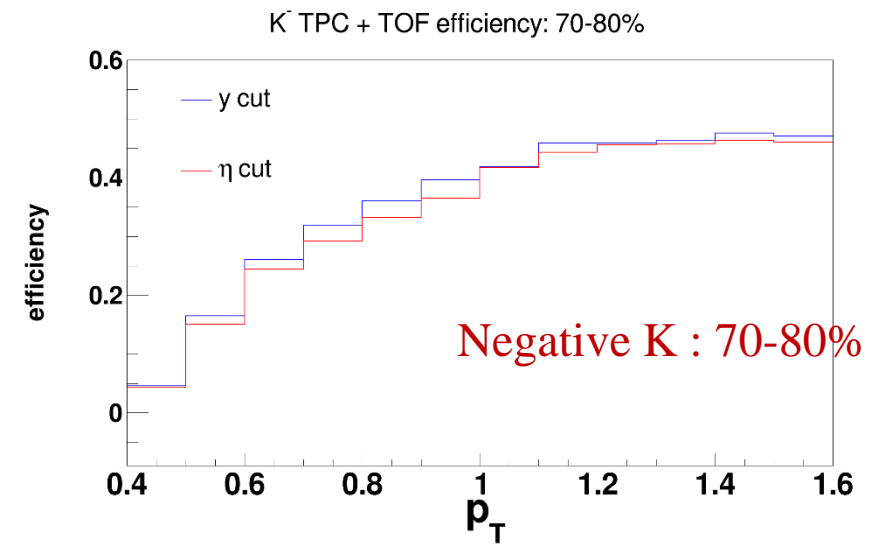
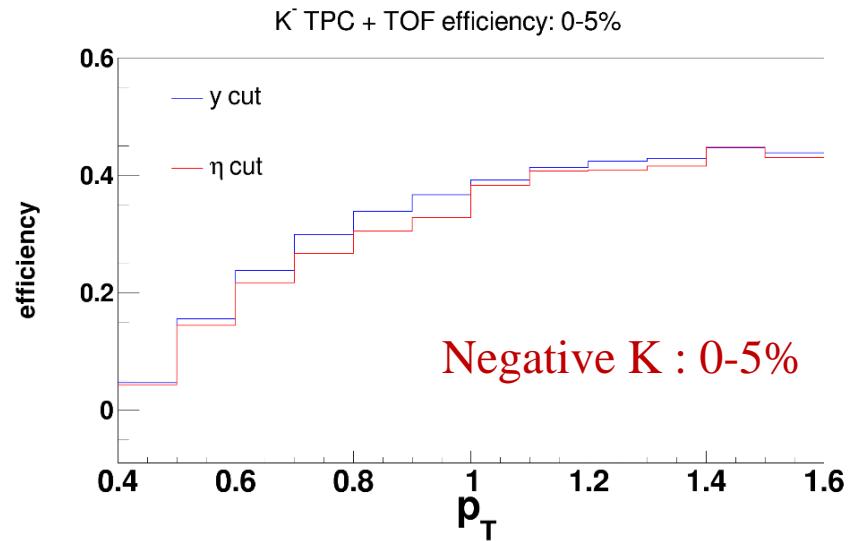
**I used pseudorapidity( $\eta$ ) to calculate TPC efficiency of kaon, but analysis was done with  $|y| < 0.5$**

Phase-space window:

- $0.4 < p_T < 1.6 \text{ GeV}/c$
- $|y| < 0.5$
- Track by track efficiency correction
- Centrality definition with Refmult2



# Comparison of kaon efficiency between $|\eta| < 0.5$ and $|y| < 0.5$ cut



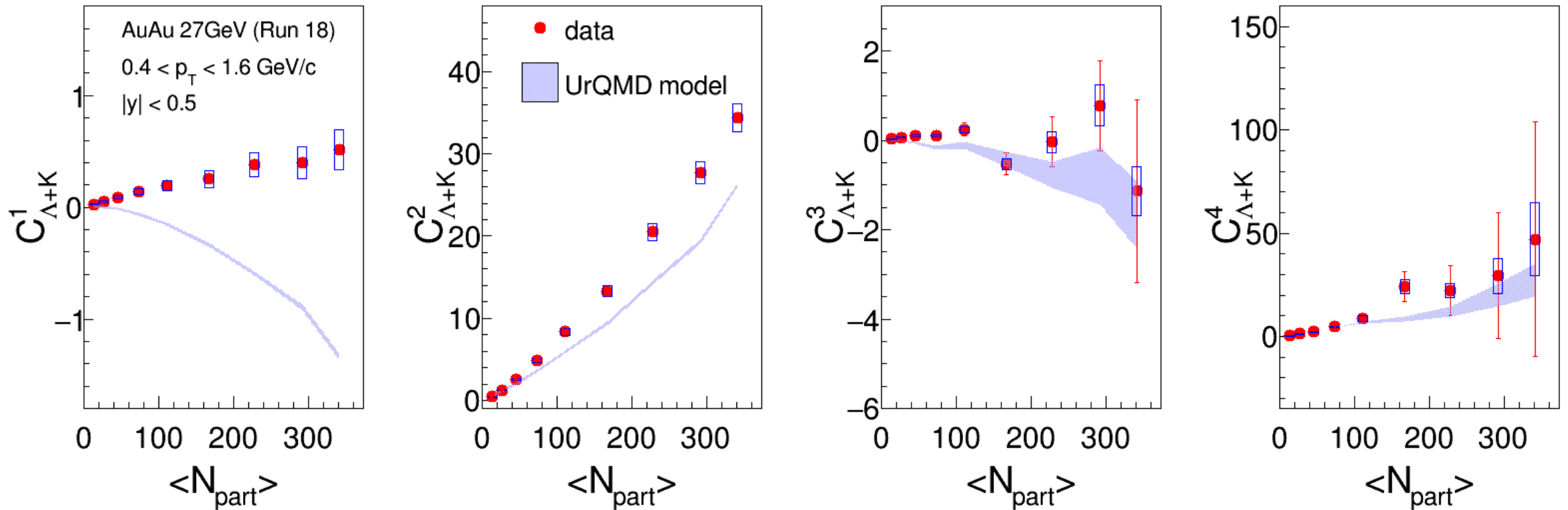


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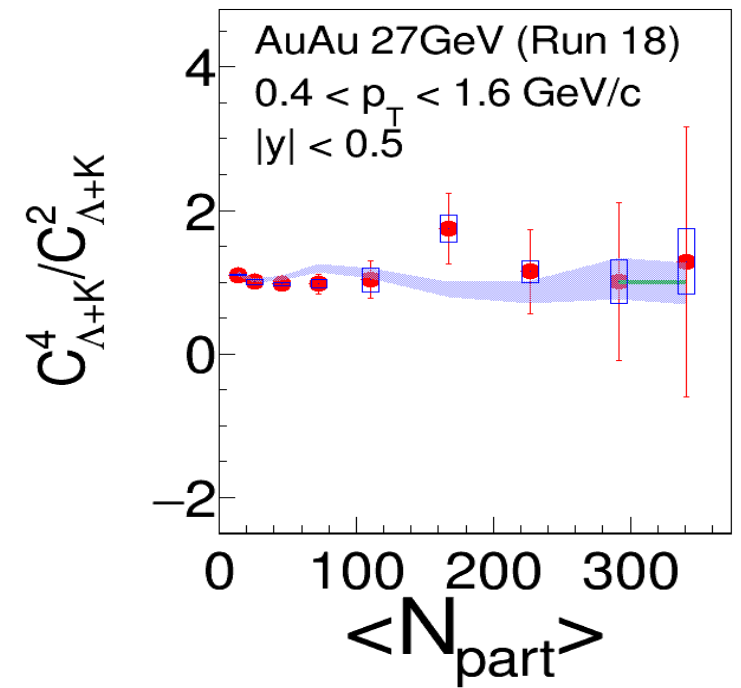
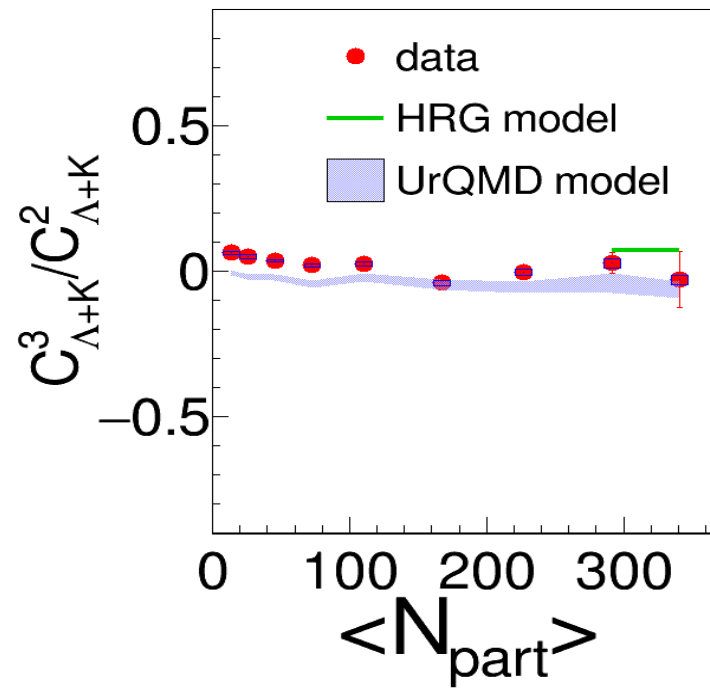
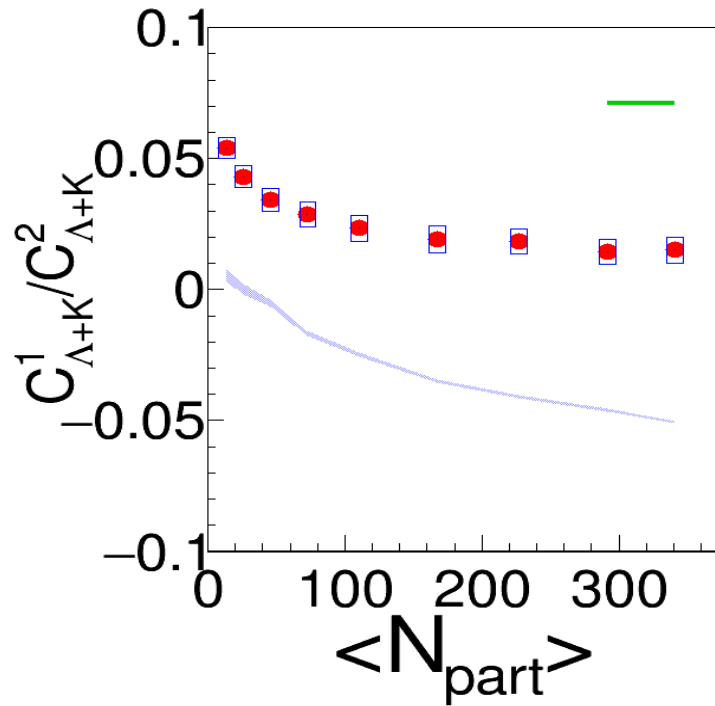


# Cumulants ratio of Net-(K+ $\Lambda$ ) multiplicity distributions

$$\text{Net-(}\Lambda+\text{K)} \equiv \Delta N_{(\Lambda+\text{K})} = (N_{\text{anti-}\Lambda} + N_{\text{K}^+}) - (N_{\Lambda} - N_{\text{K}^-})$$

Phase-space window:

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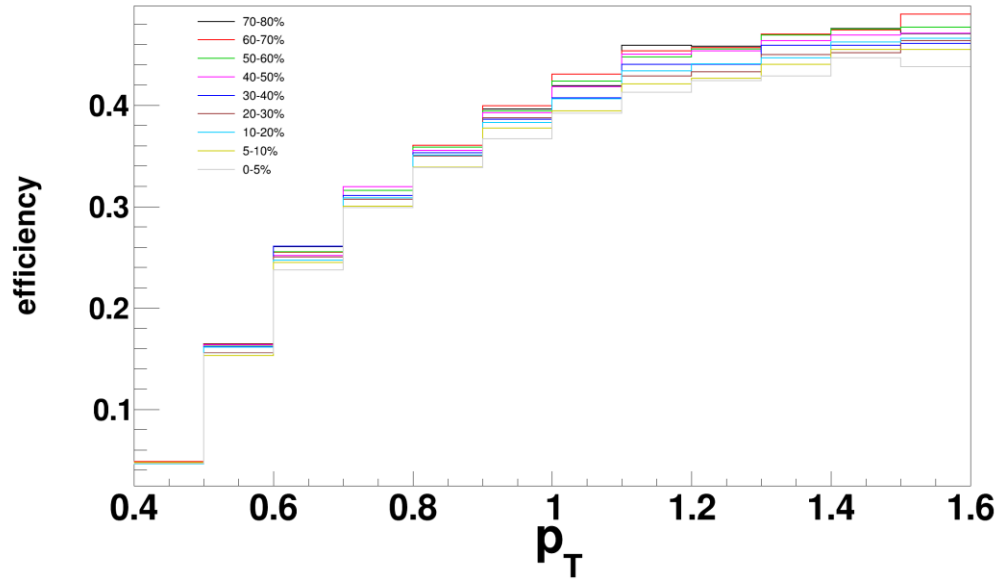
# Summary and Outlook

- First attempt to measure cumulants of net-(K+ $\Lambda$ ) multiplicity distributions using Run18 27 GeV
- HRG and UrQMD results are compared with the data
- $C_1/C_2$  deviates from the HRG and UrQMD calculations, whereas  $C_3/C_2$  and  $C_4/C_2$  agrees with both the models.

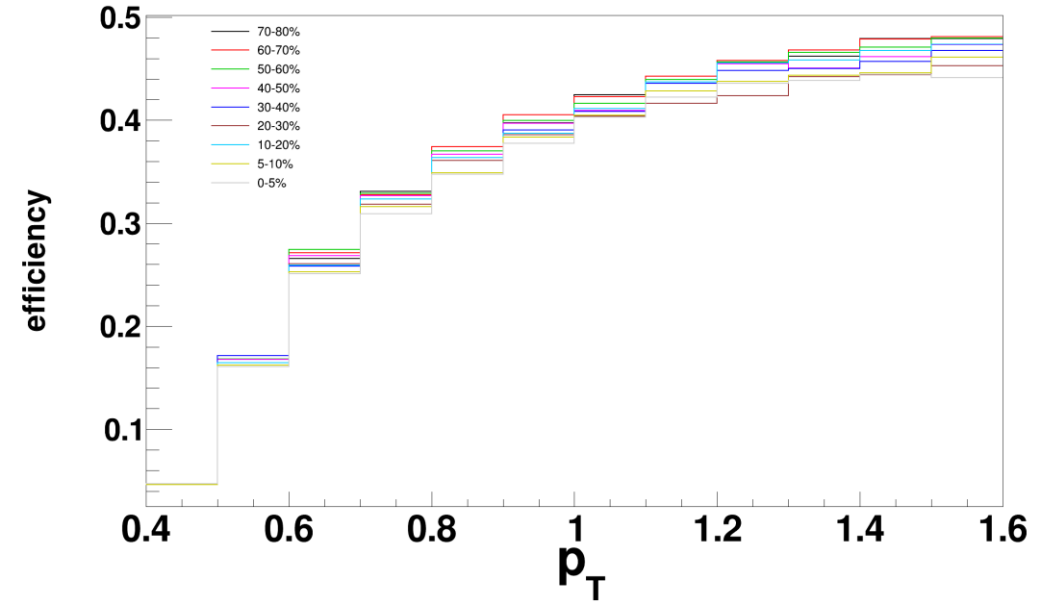
# Backup

# $P_T$ dependent kaon and lambda efficiency

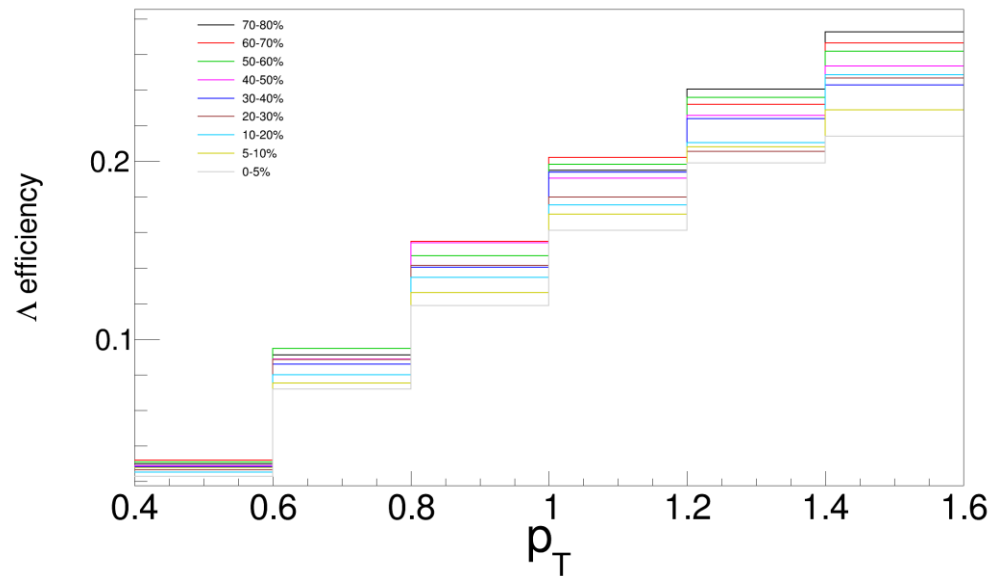
$K^-$  TPC + TOF efficiency



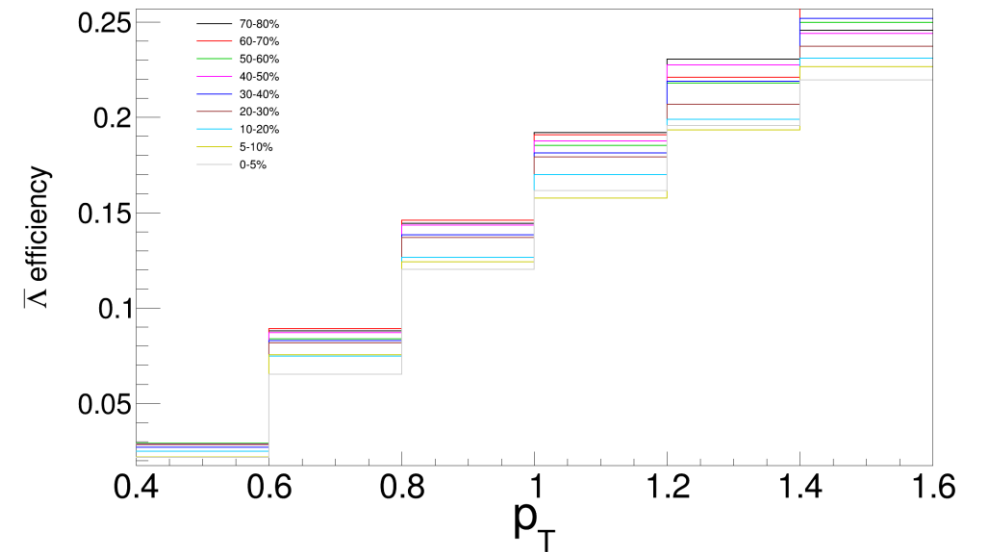
$K^+$  TPC + TOF efficiency



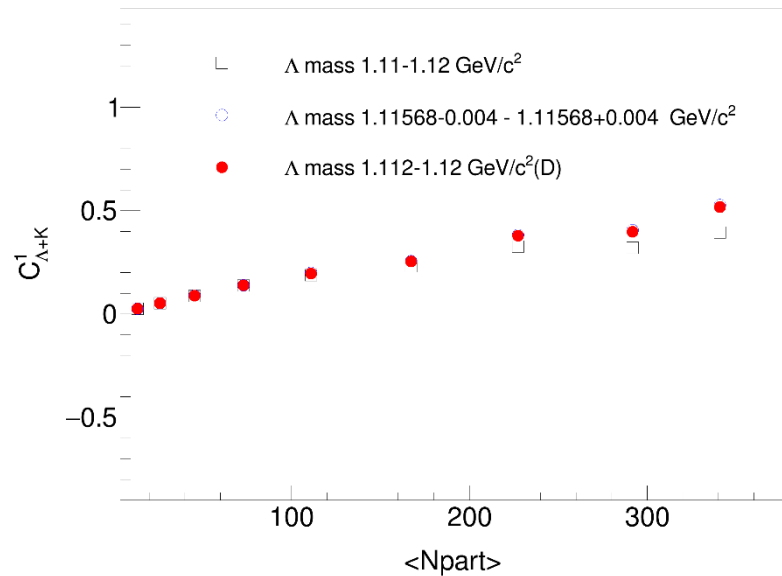
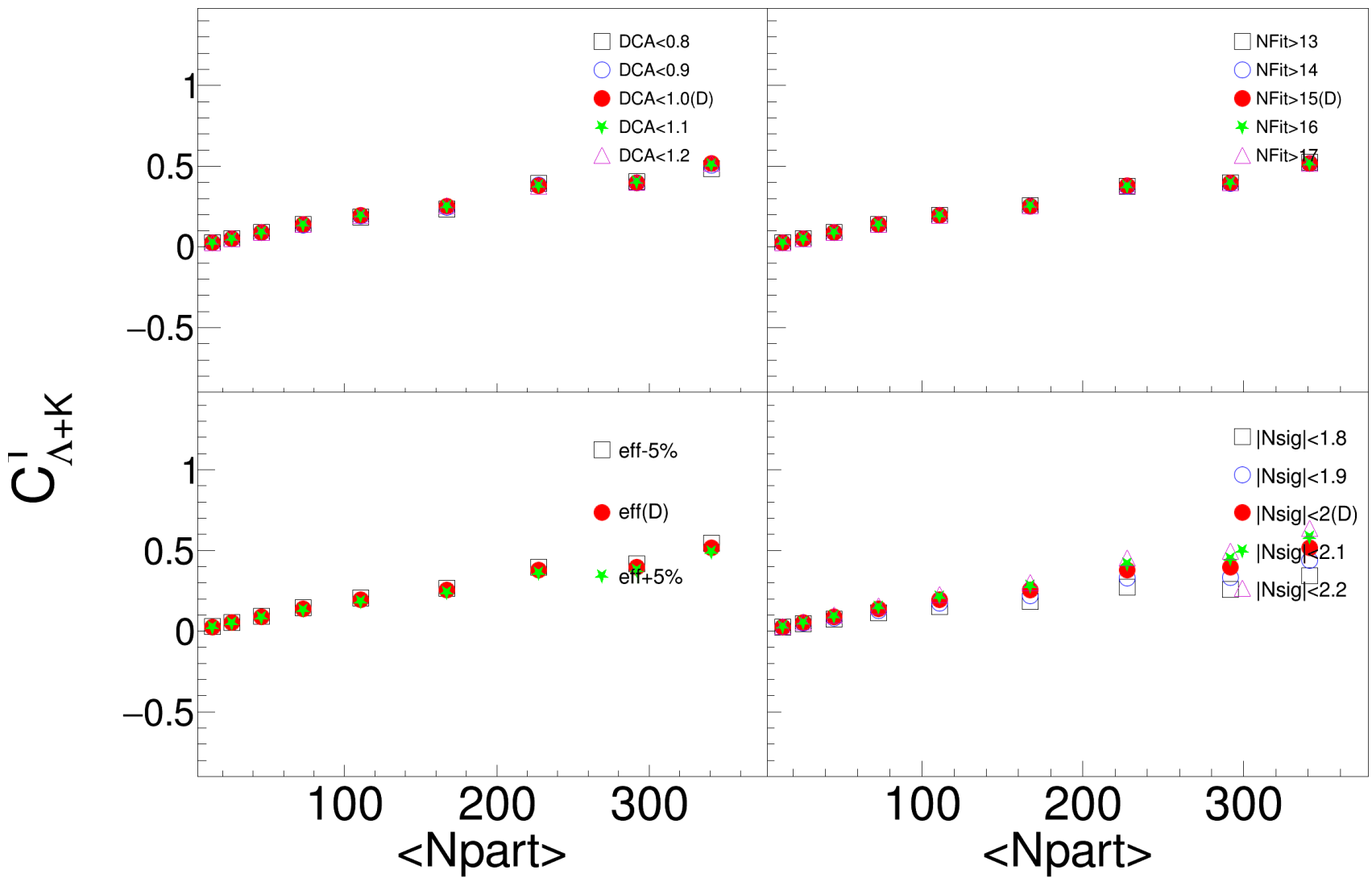
$\Lambda$  efficiency



$\bar{\Lambda}$  efficiency



# Systematic uncertainty estimation: DCA, nHits, efficiency, $|\sigma_{PID}|$ and lambda mass window variations



$$\sigma_{sys} = Y_{def} \sqrt{\sum_j R_j^2}$$

$$R_j = \sqrt{\frac{1}{n} \sum_i \left( \frac{Y_{i,j} - Y_{def}}{Y_{def}} \right)^2}$$

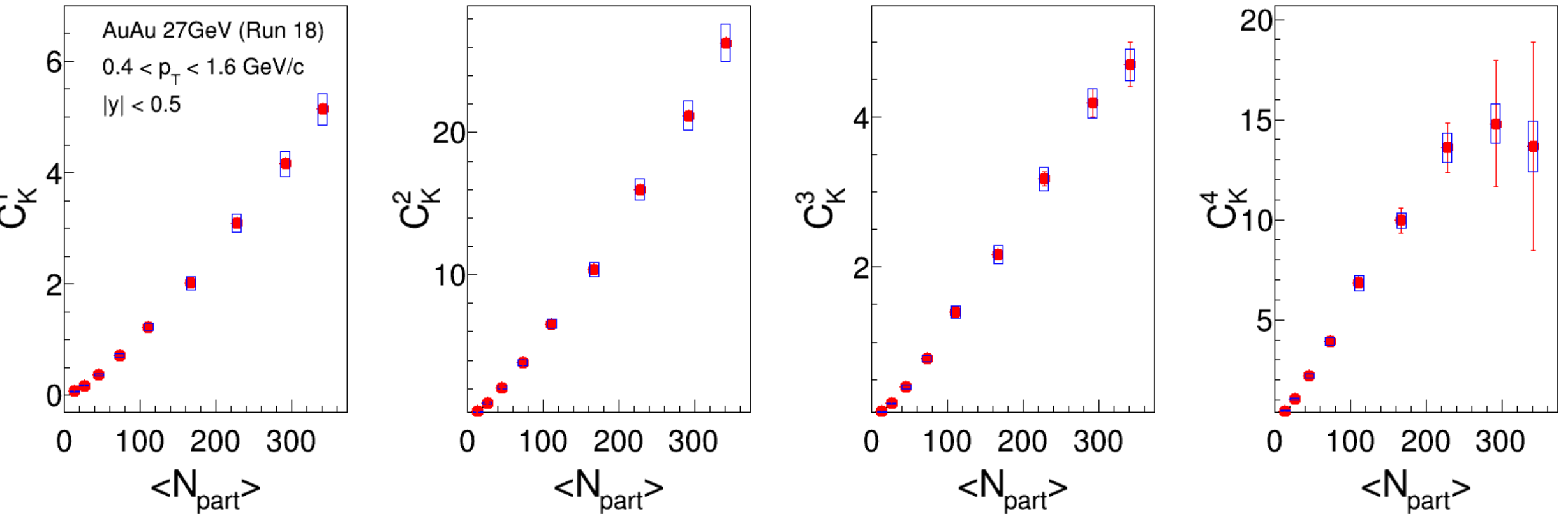
$Y_i$  represents  $i$ th change of the cut on  $j$ th variable

# Cumulants of Net-Kaon multiplicity distributions

$$\text{Net-K} \equiv \Delta N_K = N_{K^+} - N_{K^-}$$

Phase-space window:

- $0.4 < p_T < 1.6 \text{ GeV}/c$
- $|y| < 0.5$
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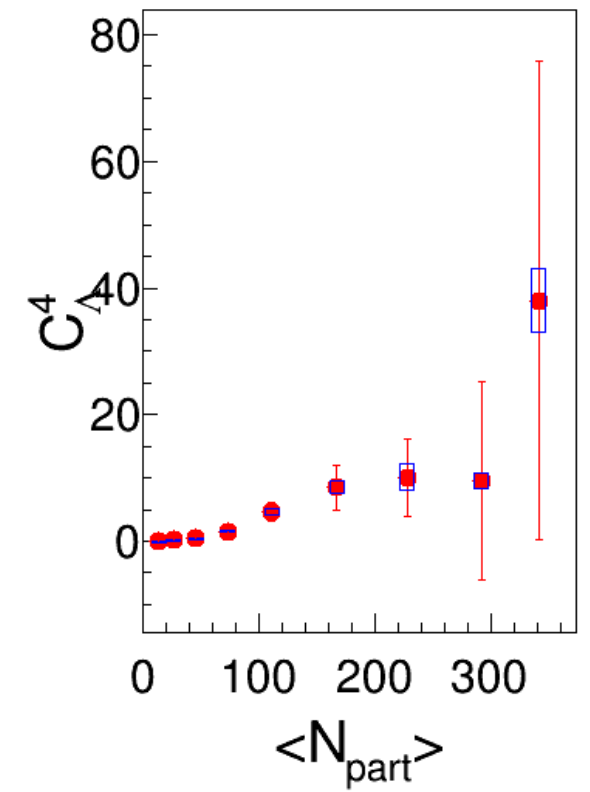
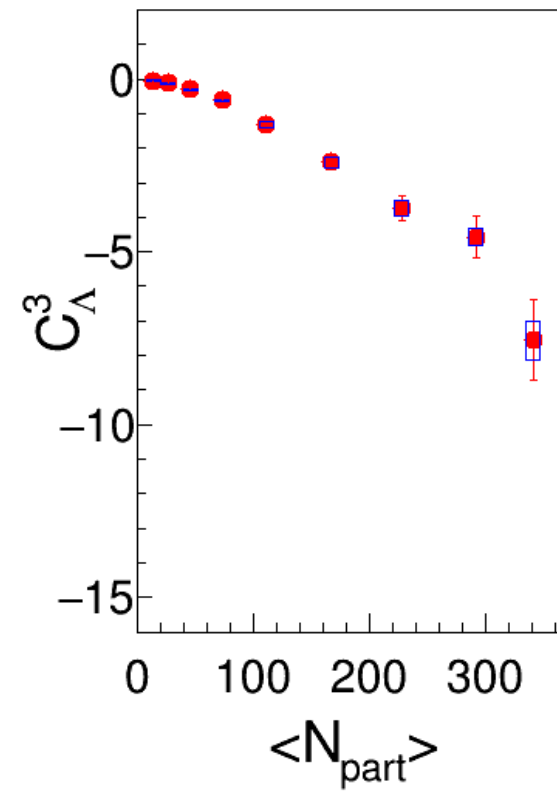
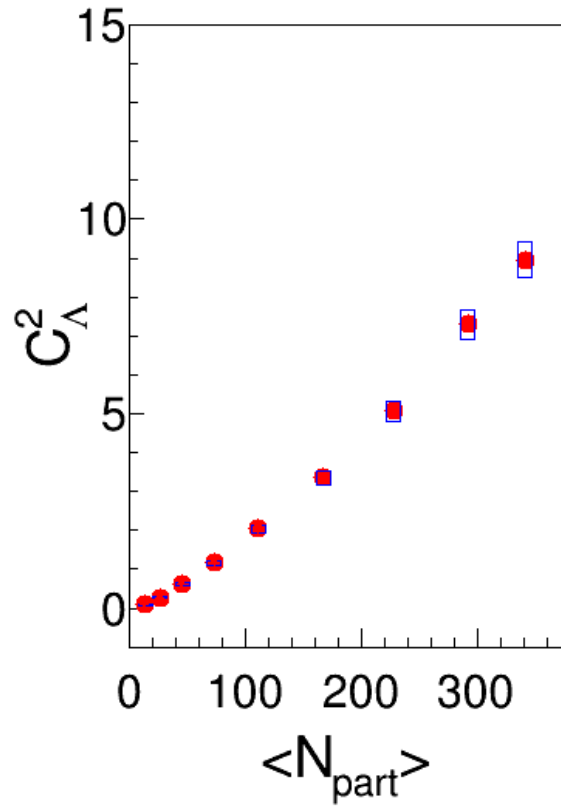
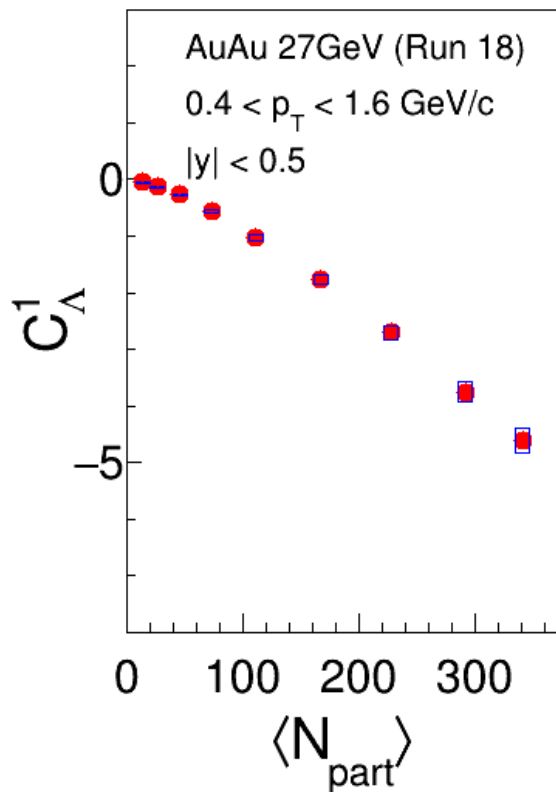


# Cumulants of Net- $\Lambda$ multiplicity distributions

$$\text{Net-}\Lambda \equiv \Delta N_{\Lambda} = N_{\text{anti-}\Lambda} - N_{\Lambda}$$

Phase-space window:

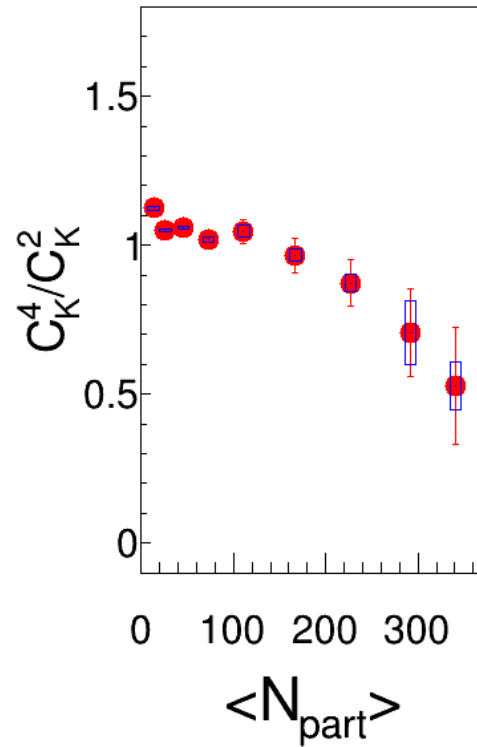
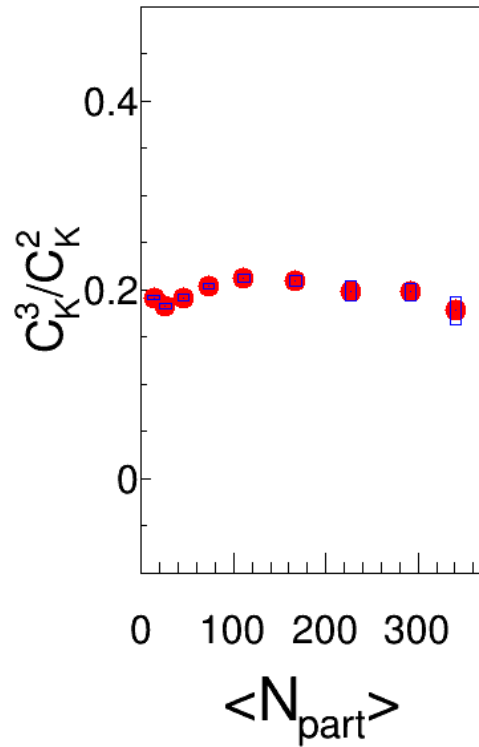
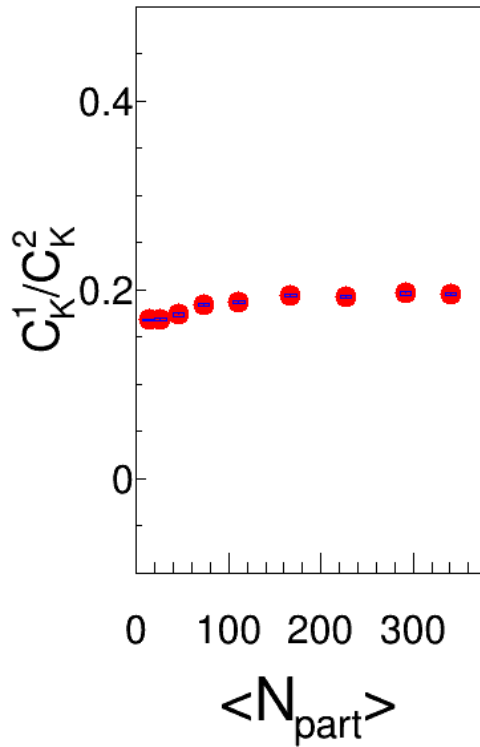
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# Cumulants ratio of Net-Kaon multiplicity distributions

$$\text{Net-K} \equiv \Delta N_K = N_{K^+} - N_{K^-}$$



Phase-space window:

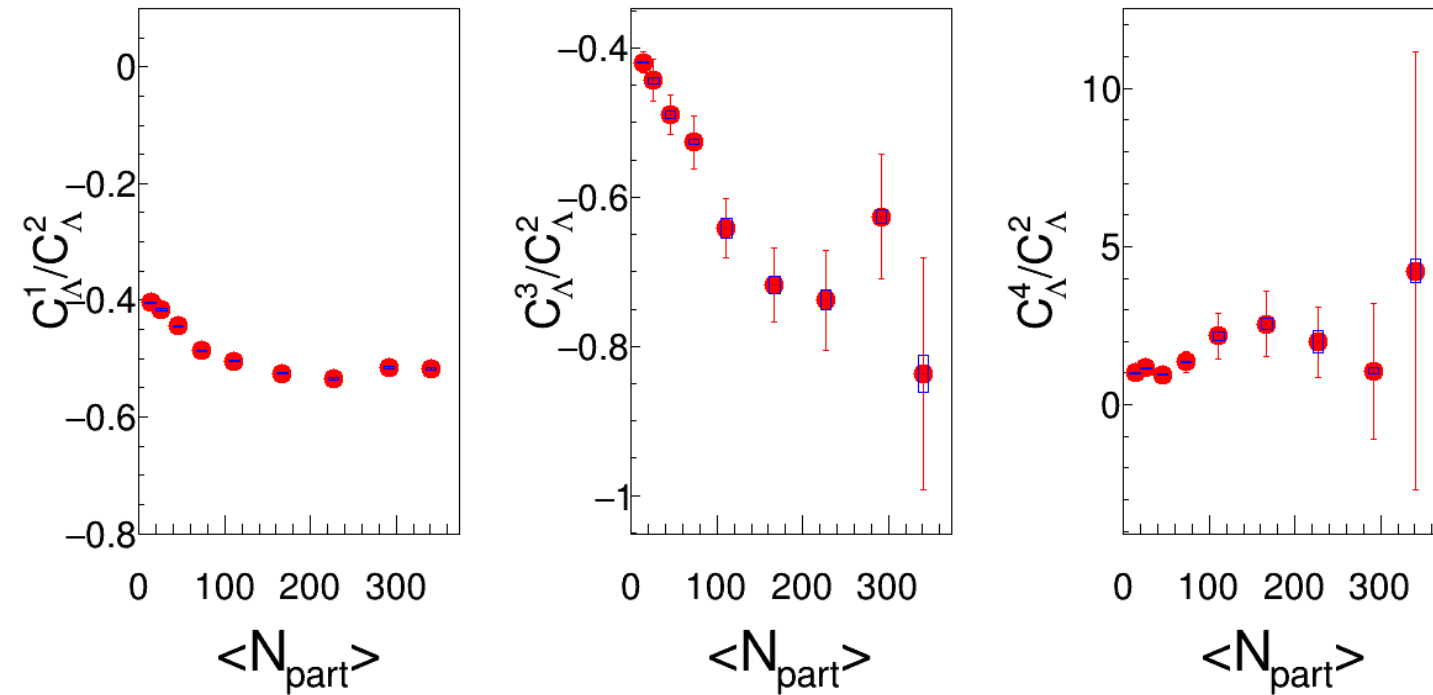
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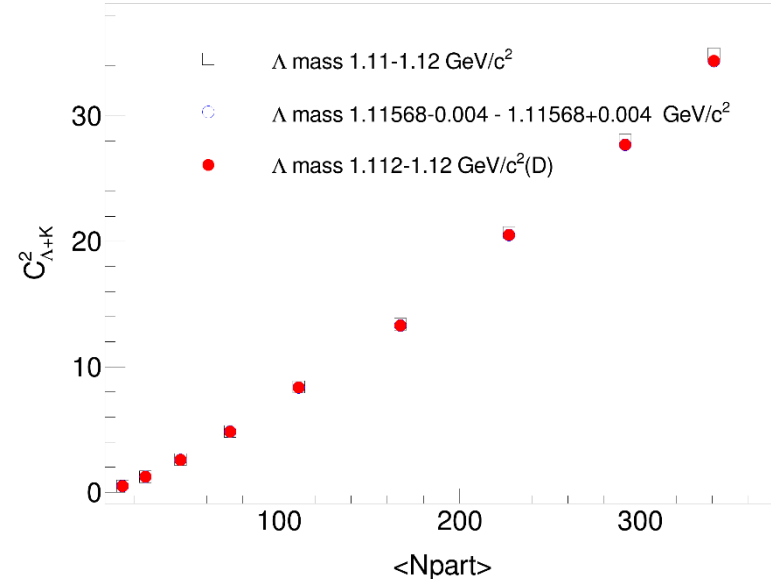
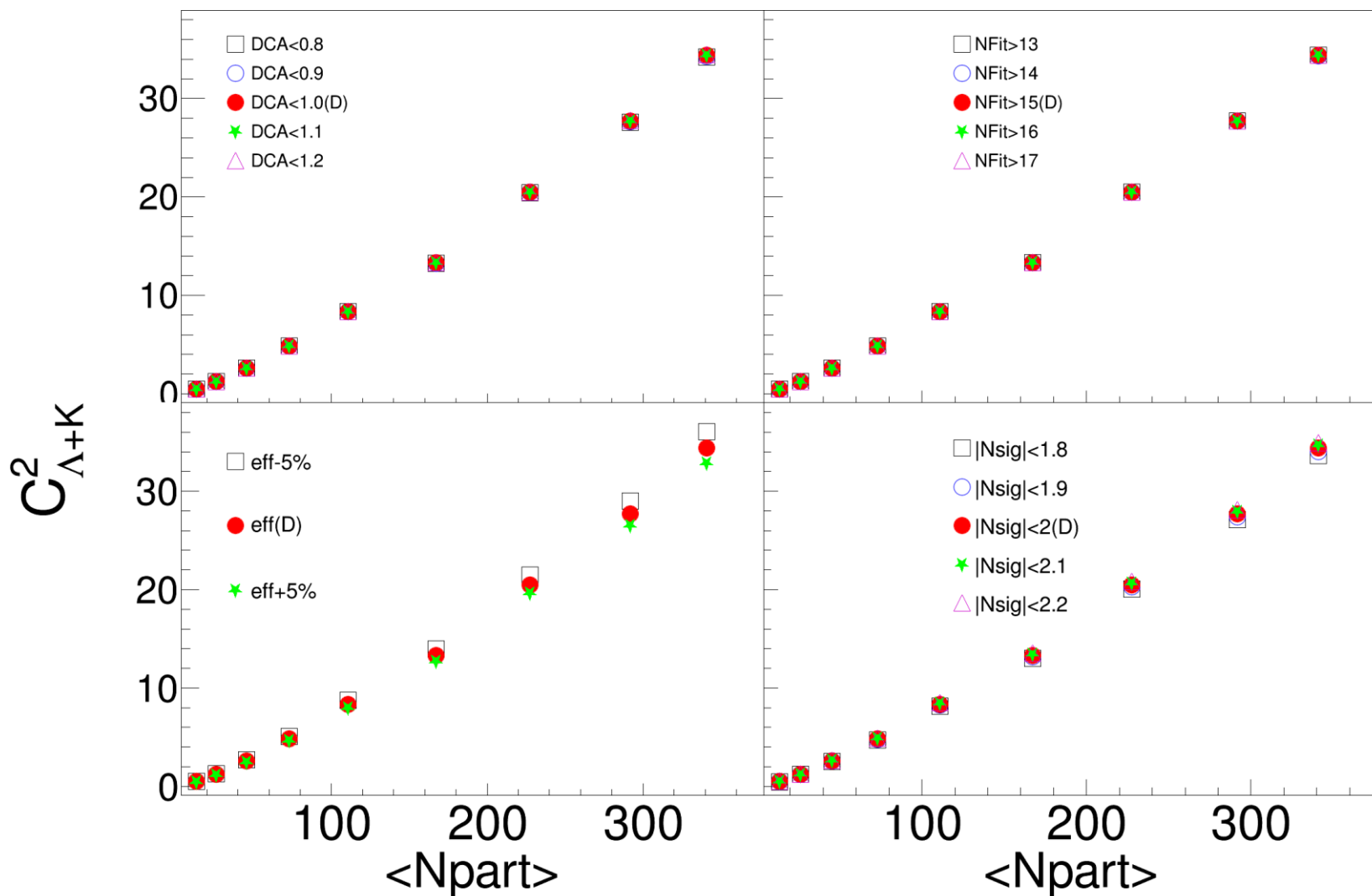
$$\text{Net-}\Lambda \equiv \Delta N_\Lambda = N_{\text{anti-}\Lambda} - N_\Lambda$$

Phase-space window:

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# Systematic uncertainty estimation: DCA, nHits, efficiency, $|\text{n}\sigma_{\text{PID}}|$ and lambda mass window variations

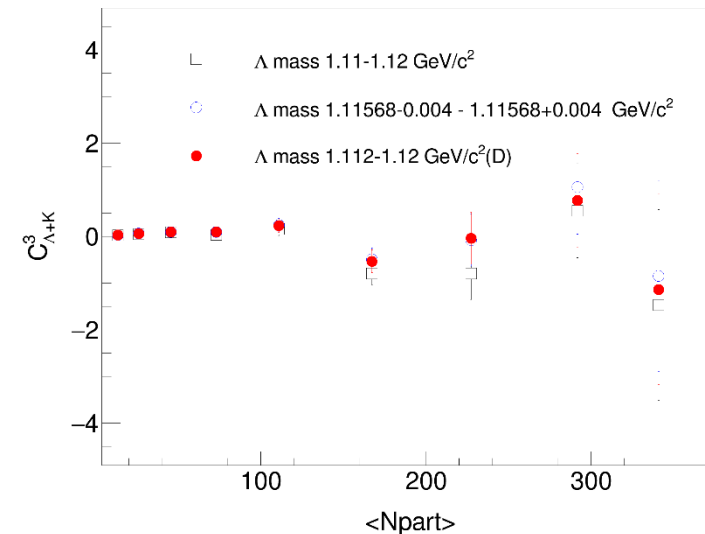
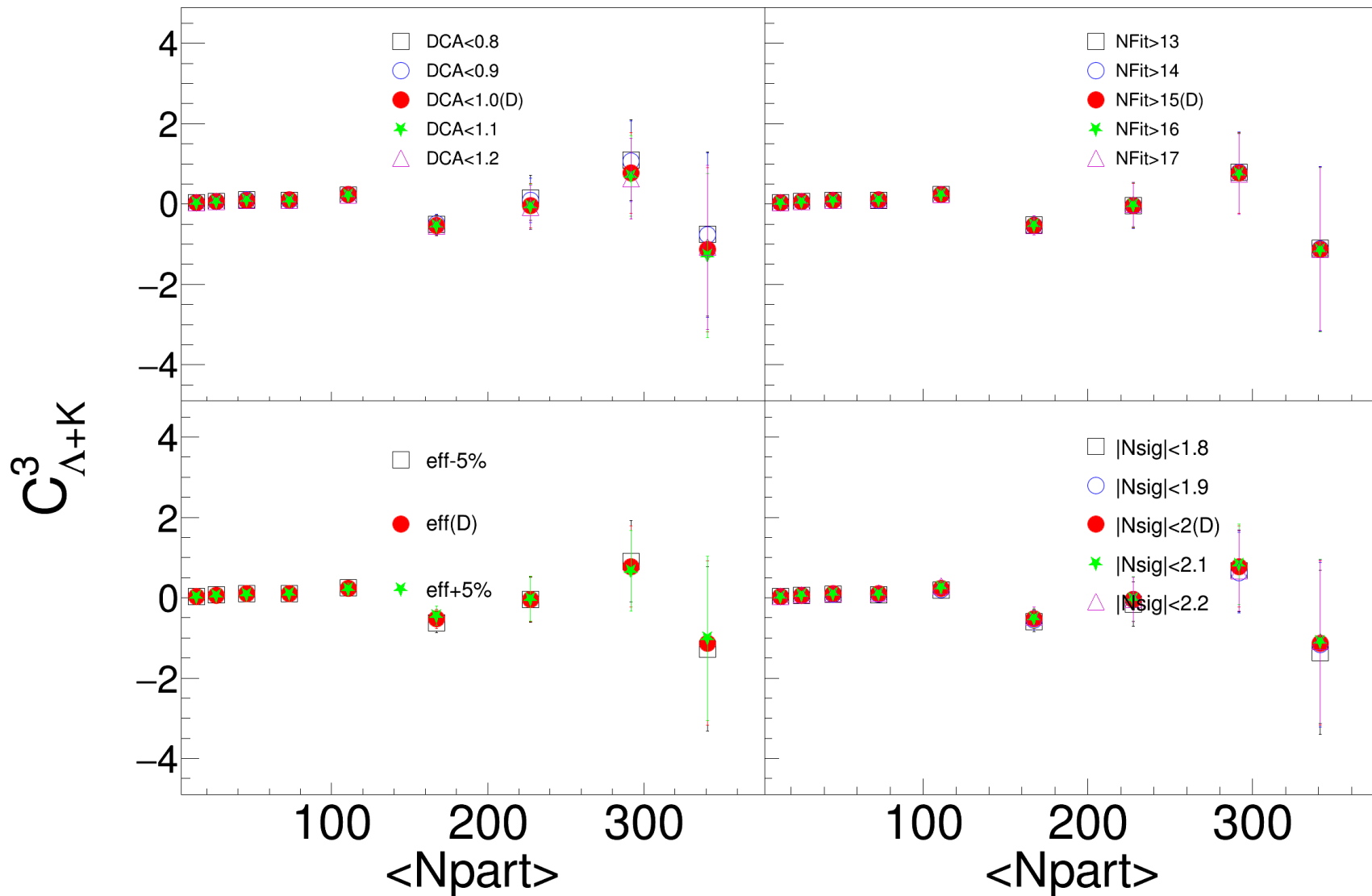


$$\sigma_{\text{sys}} = Y_{\text{def}} \sqrt{\sum_j R_j^2}$$

$$R_j = \sqrt{\frac{1}{n} \sum_i \left( \frac{Y_{i,j} - Y_{\text{def}}}{Y_{\text{def}}} \right)^2}$$

$Y_i$  represents  $i$ th  
change of the cut on  
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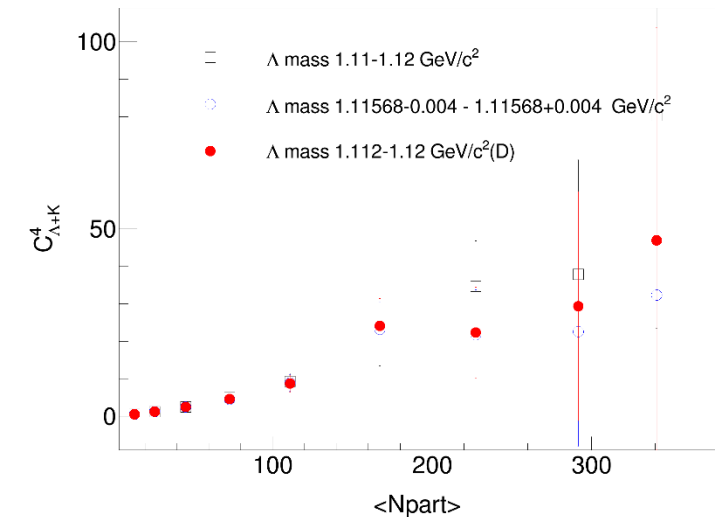
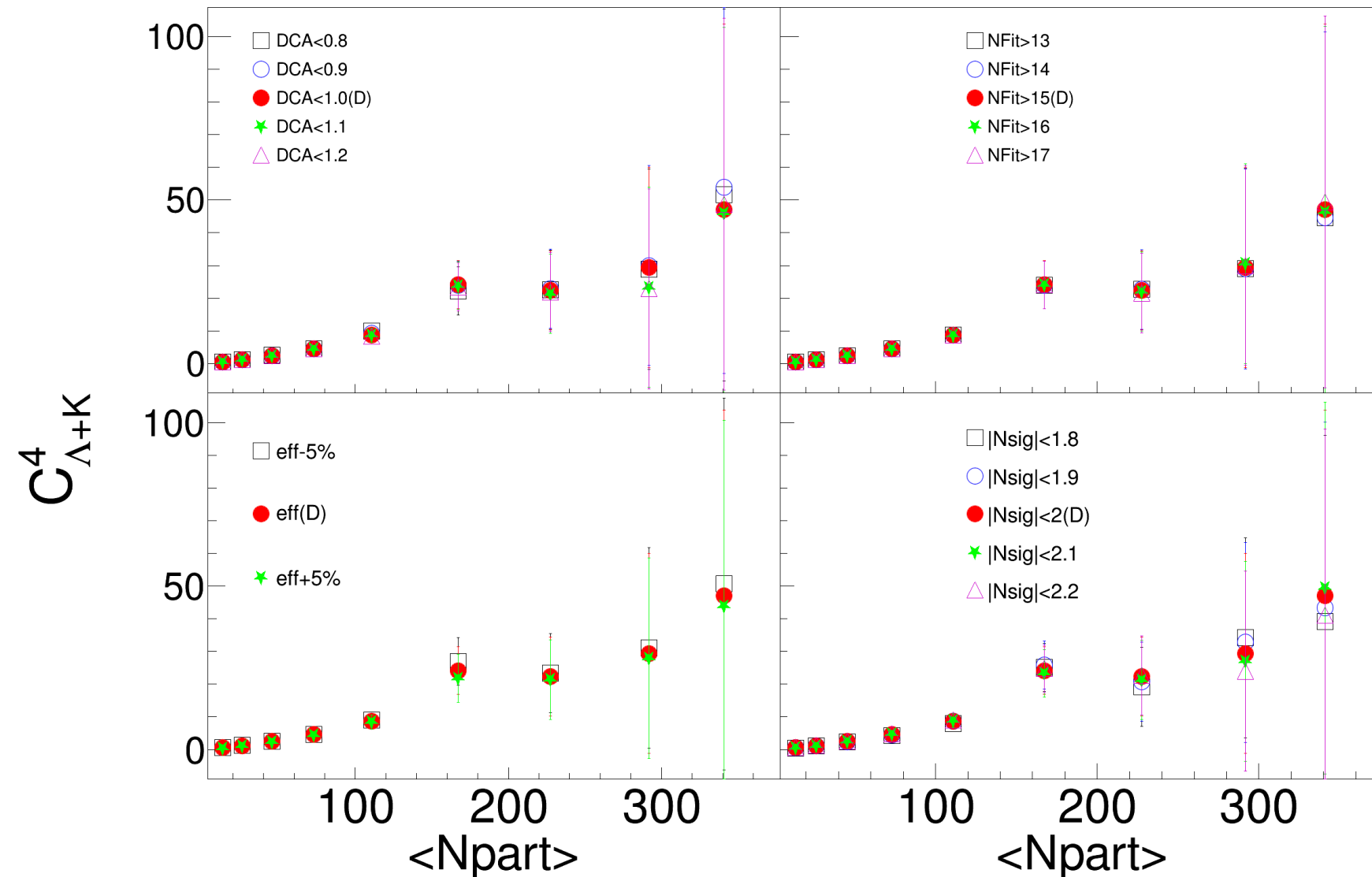


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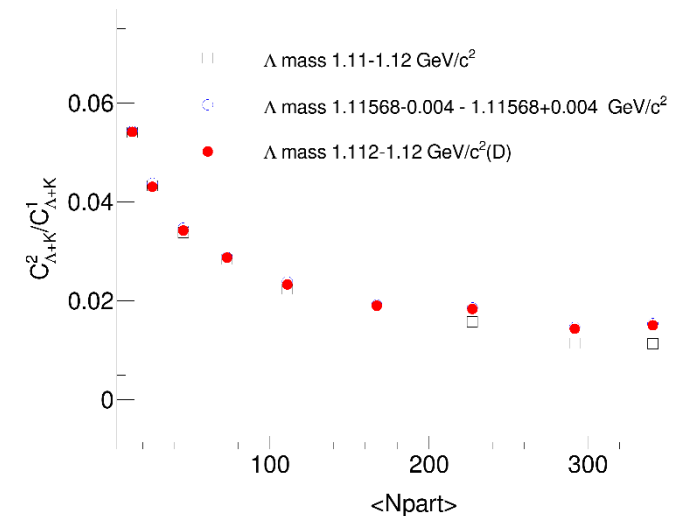
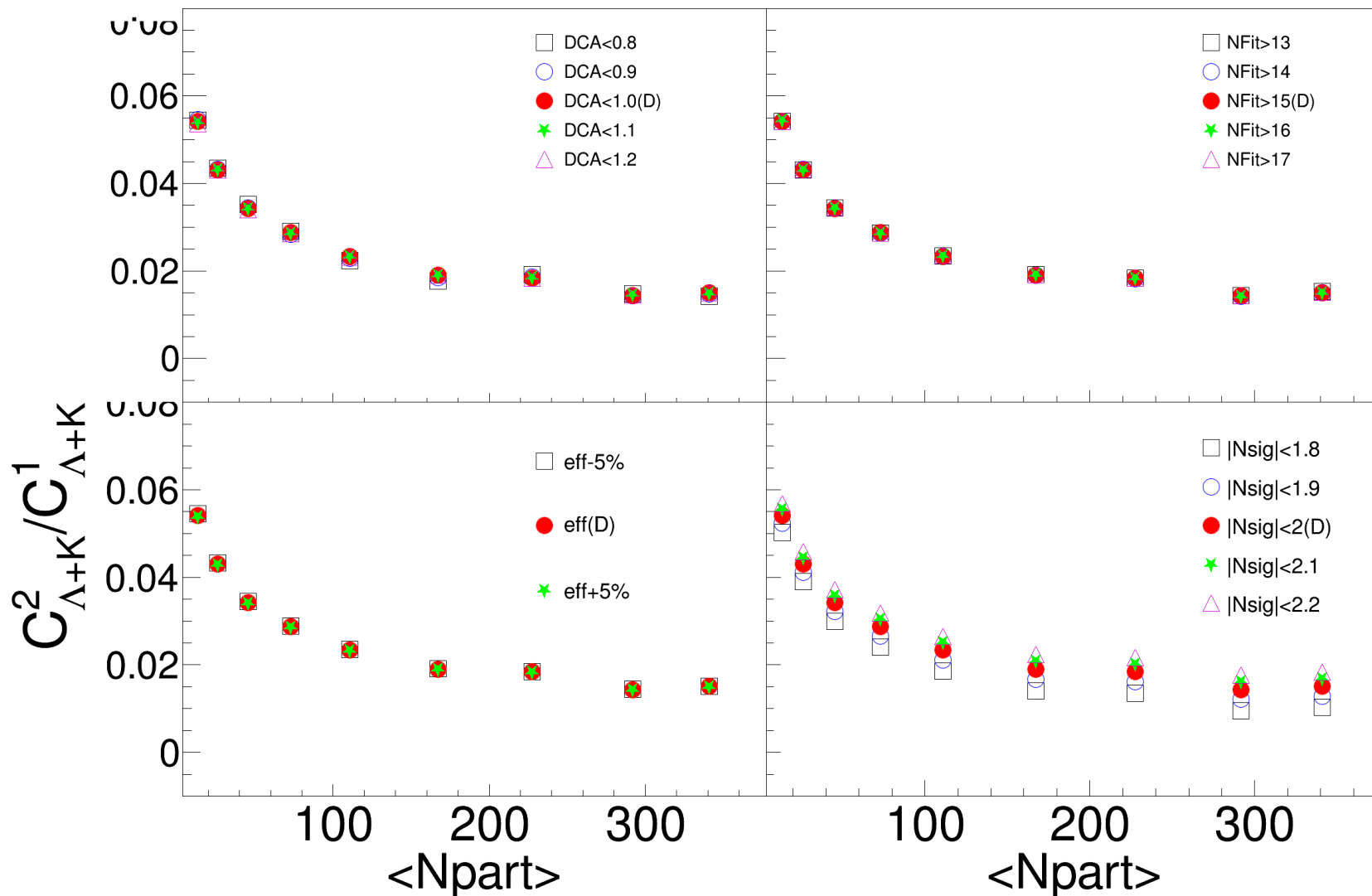


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$Y_i$  represents  $i$ th change of the cut on  $j$ th variable

# Systematic uncertainty estimation: DCA, nHits, efficiency, $|\text{n}\sigma_{\text{PID}}|$ and lambda mass window variations

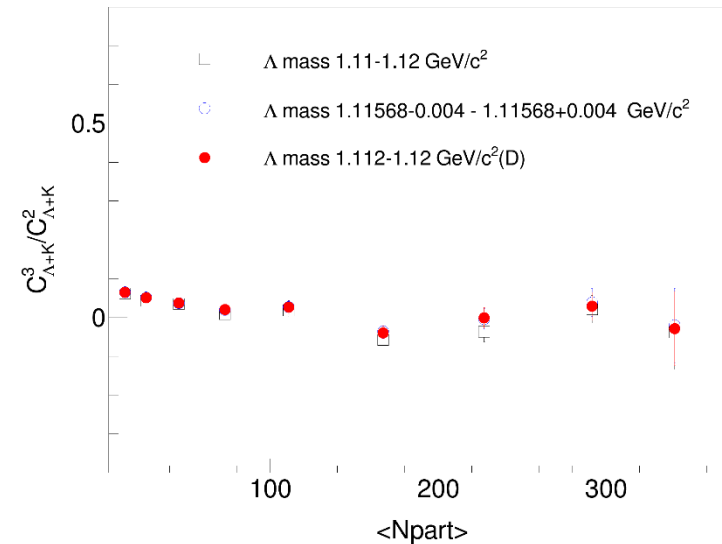
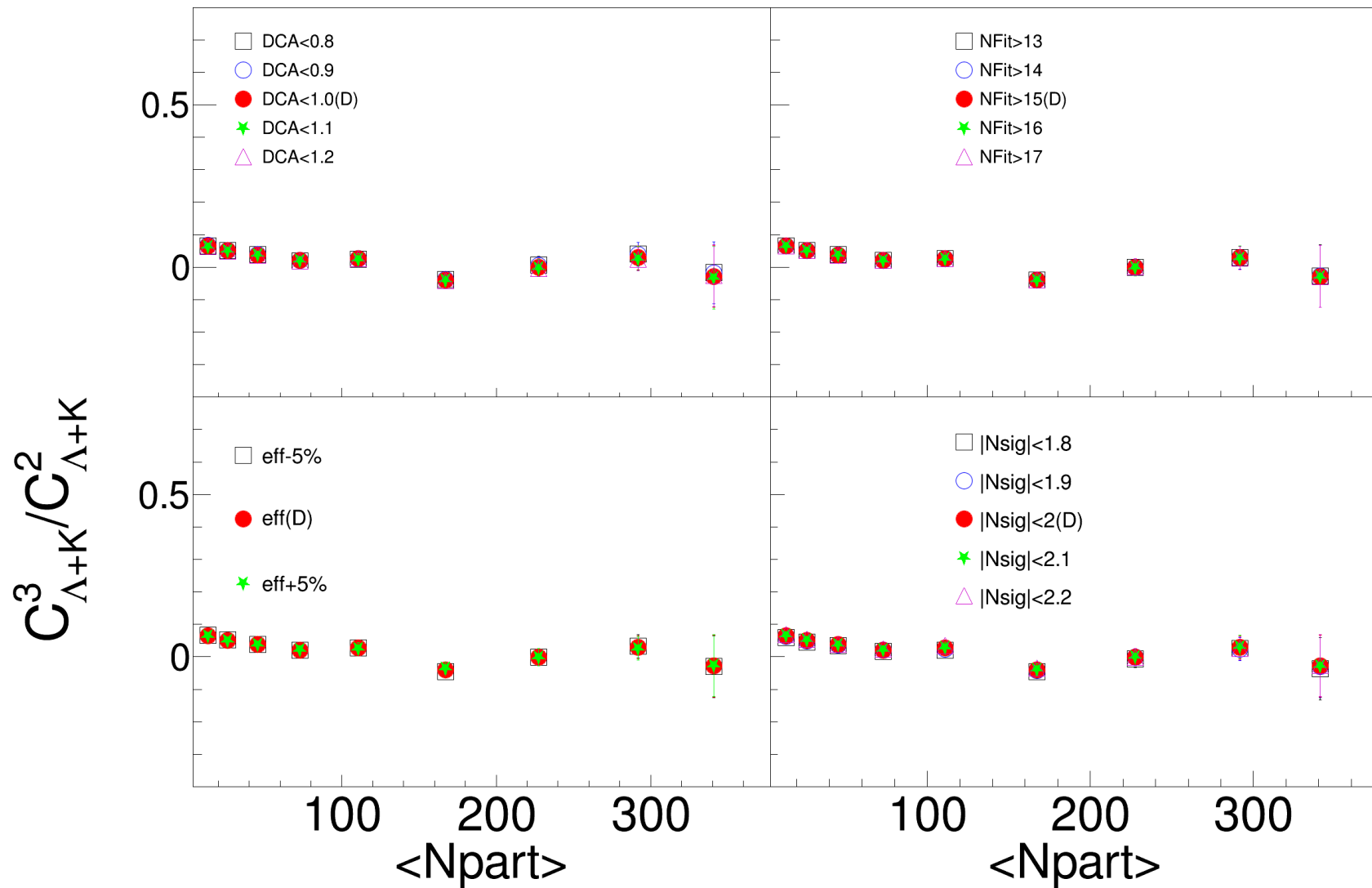


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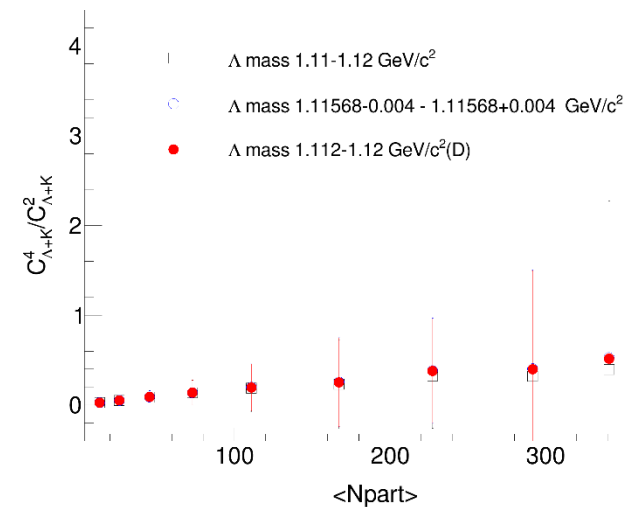
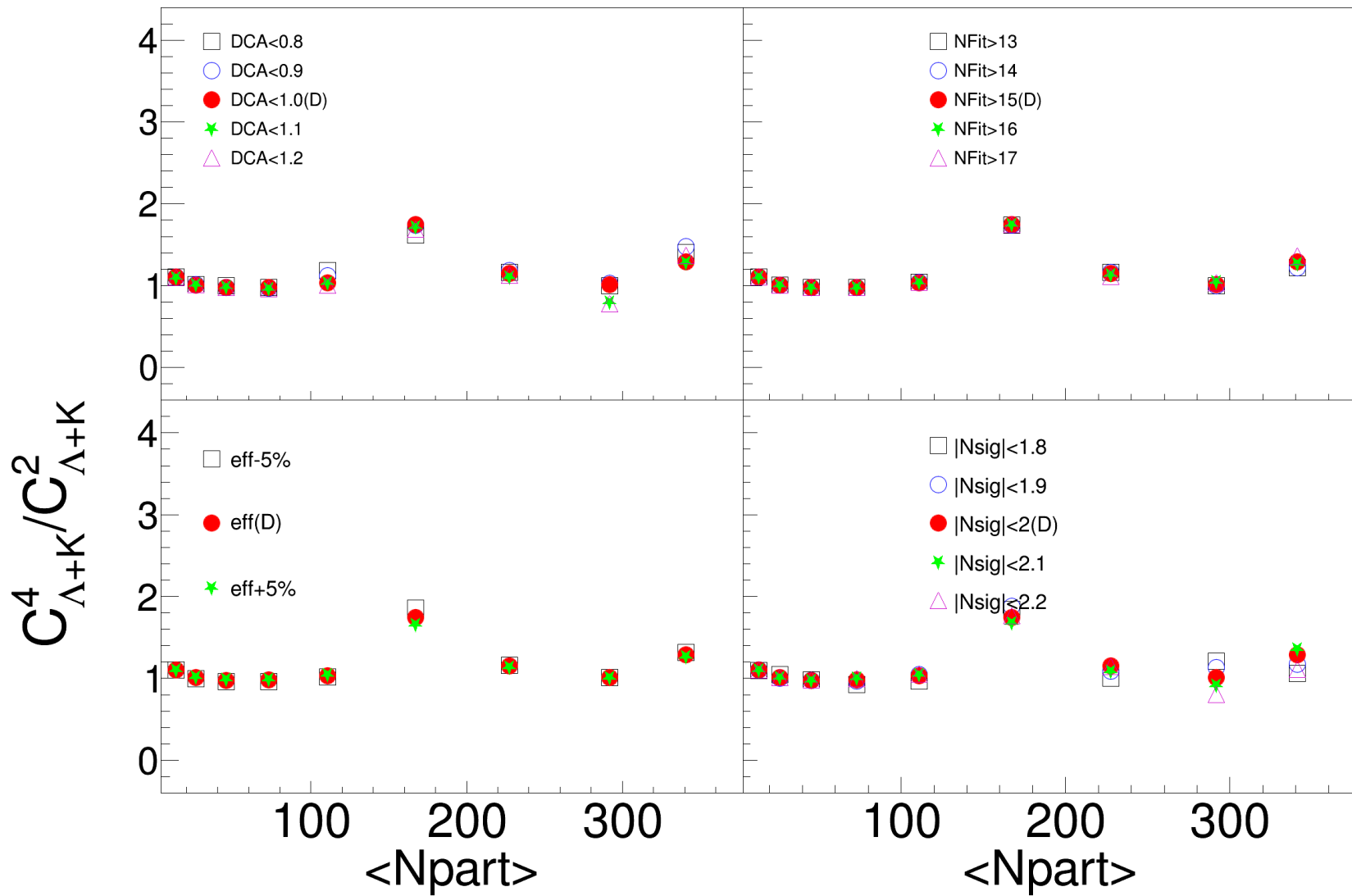


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# $P_T$ dependent kaon efficiency

I use the pseudorapidity cut when I calculate TPC efficiency of kaon

