

1 Accessing the Temperature of the Quark-Gluon Plasma at 2 Different Stages

3 In a Quark-Gluon Plasma (QGP) ^{1,2}, the fundamental building blocks of matter can be
4 found at the most extreme temperature and density ^{3,4} conditions. It is believed to have
5 existed in the early stages of the Universe ⁵⁻⁷, in supernova explosions ⁸, and in the core
6 of neutron stars ^{9,10}. Ultra-relativistic heavy-ion collisions, in which quarks and gluons are
7 liberated from confinement within nucleons, can recreate a QGP. The thermodynamic and
8 hydrodynamic properties of the QGP, such as temperature, baryon chemical potential, and
9 viscosity, have been under intense theoretical investigations in lattice Quantum Chromo-
10 dynamics (QCD) calculations ^{11,12} and in experiments utilizing the world's most powerful
11 supercomputers and particle accelerators, respectively ^{13,14}. Thermal lepton pairs (e^+e^-
12 and $\mu^+\mu^-$) from QGP radiation are ideal, penetrating probes of the true temperature of
13 the emitting source, since they do not suffer from strong final state interactions nor from
14 blue-shift effects through the collective motion of the rapidly expanding system ¹⁵⁻¹⁷. The
15 invariant mass spectra of thermal e^+e^- pairs over a large kinematic range and different
16 beam energies at the Relativistic Heavy Ion Collider (RHIC) have been studied. We ex-
17 tract from intermediate invariant mass pairs the temperature of the QGP radiation averaged
18 over the early space-time evolution. From low-mass pairs, which are dominated by the de-
19 cays from in-medium ρ^0 vector mesons, we extract the temperature averaged over the later
20 stage of the evolution. The average temperature from the low-mass region is measured to
21 be $(1.90 \pm 0.20) \times 10^{12}$ Kelvin. It is close to the chemical freeze-out temperature derived

22 **in the Statistical Hadronization Model** ¹⁸ **and the transition temperature from lattice QCD**
23 **calculations** ^{11,12}. **The temperature from intermediate mass pairs is significantly higher, and**
24 **averaged to be** $(3.72 \pm 0.49) \times 10^{12}$ **Kelvin. These measurements provide direct experimen-**
25 **tal access to the QGP temperature and deliver the experimental evidence that the ρ^0 hadron**
26 **undergoes a significant in-medium broadening effects when it is produced around the phase**
27 **boundary between QGP and hadronic matter.**

28 **1 Introduction**

29 The state of QCD matter is typically characterized by its temperature and baryon chemical potential
30 as depicted in Fig. 1. The baryon chemical potential μ_B , a measure of the free energy change due to
31 the increase of baryon number in a fixed volume in the system, can be extracted from yields among
32 many hadrons at given beam energy in the heavy-ion collisions ¹¹⁻¹⁴. Dielectrons, typically defined
33 as e^+e^- pairs, are excellent thermometers of the extremely hot and dense QCD matter ¹⁹ created in
34 high energy heavy-ion collisions. Electrons are members of a class of fundamental particles called
35 leptons that do not undergo strong interactions. Consequently, they have minimal interactions with
36 the predominantly strongly-interacting particles throughout the evolution of the system in both its
37 initial quark-gluon and the final hadronic state. Similar to other blackbody radiation processes, the
38 higher the temperature, the harder the dielectron energy and mass spectra. In a collision where
39 the system cools as it expands, different ranges of the dielectron energy and spectra would be
40 dominated by the radiation at the different stages of the evolution. QGP bulk matter consists of
41 thermalized quarks and gluons under the most extreme conditions and its temperature can reach

42 a few hundreds of MeV, where $100 \text{ MeV} = 1.16 \times 10^{12} \text{ K}$. It radiates both photons and lepton
43 pairs which can be harvested by experiments as thermometer ^{1,20,21}. Photons have been used
44 to measure the QGP temperature at the Relativistic Heavy Ion Collider (RHIC) and the Large
45 Hadron Collider (LHC) in the last two decades ²²⁻²⁵. However, heavy-ion collisions at these ultra-
46 relativistic energies result in a rapid bulk expansion with a complicated flow profile. The local flow
47 velocity is a significant fraction of the speed of light and alters the energy spectrum of photons.
48 This blue-shift effect makes the extraction of a true “blackbody” radiation temperature from the
49 detected photon energy spectrum very complex, if not impossible, and overly reliant on model
50 assumptions ¹⁷. On the contrary, electron pairs from the thermal emission provide an additional
51 degree of freedom for the reconstruction of a Lorentz-invariant quantity: its invariant mass ^{15,16}.
52 The invariant mass spectrum of thermal dielectrons, by definition, is immune to the blue-shift effect
53 and is therefore able to provide a true measurement of the temperature of the QGP at different
54 stages of the evolution. At the early stage of the QGP evolution, thermal dielectrons are predicted
55 to be dominantly produced via the annihilation among quarks, anti-quarks and gluons. When the
56 system cools down, the liberated quarks and gluons begin the hadranization process into baryons
57 and mesons at the phase transition. The resulting strongly-interacting partonic and hadronic mixed
58 medium still exhibits certain bulk thermodynamic and hydrodynamic properties and continues to
59 expand and cool down. At this stage and later on, the dielectrons are mostly from the decays of
60 ρ^0 vector meson produced inside the medium. The dense hadronic medium continuously creates
61 ρ^0 through intense hadronic collisions while the vector meson also decays spontaneously with
62 a lifetime of 1 fm/c or less. The collisional and in-medium broadening effects on the ρ^0 spectral

63 function lead the dielectron spectra to approach a thermal distribution ²⁶⁻²⁹. Therefore, the thermal
 64 dielectron invariant mass spectra from the decay of the in-medium ρ^0 vector meson are considered
 65 as an excellent experimental probe of the dissolving hadronic spectral functions close to the QCD
 phase boundary.

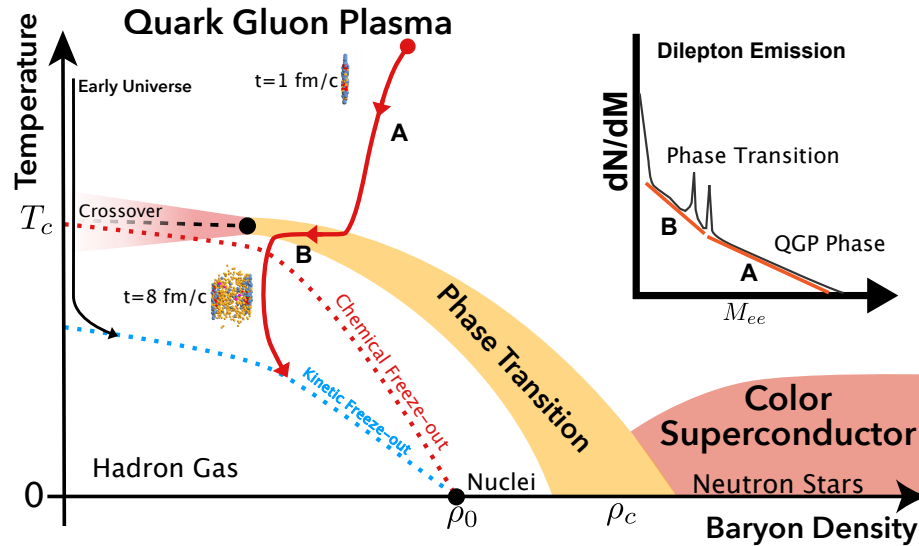


Figure 1: (Color online) A schematic view of e^+e^- pair production and QCD phase diagram.

The diagram illustrates the matter properties in baryon density (x-axis) and temperature (y-axis) with landmarks of normal nuclear density, neutron stars, and phase transition to QGP. A heavy-ion collision creates the QGP at high density and temperature shortly after the initial impact and the system evolves along the arrow toward phase boundary and hadronization. The insert depicts the dilepton spectrum with low-mass and intermediate-mass ranges corresponding to the dominant emission contribution from the transition and the QGP phases, respectively.

66

67 In the past two decades, measurements of the thermal dilepton (e^+e^- and $\mu^+\mu^-$) production
 68 in heavy-ion collisions have been an essential scientific program to several experiments conducted

69 at SIS18 ^{30,31}, Super Proton Synchrotron (SPS) ^{32–36}, RHIC ^{37–41} and LHC ⁴² at a wide range of
 70 colliding beam energies. The measured dilepton spectra in the low-mass region at both SPS and
 71 RHIC provide strong experimental evidence that the spectral function of the in-medium ρ^0 vector
 72 meson is significantly broadened without dropping its pole mass. Furthermore, the effective tem-
 73 perature (T_{eff}), an inverse slope parameter of the dimuon transverse-momentum spectrum, was
 74 extracted from NA60 data in In+In collisions at $\sqrt{s_{NN}} = 17.3$ GeV ³⁶. T_{eff} is measured to in-
 75 crease linearly as a function of the dimuon mass up to $M_{\mu^+\mu^-} < 1$ GeV/ c^2 , and then decrease
 76 toward higher mass. This feature is consistent with the expectation that the momentum of the
 77 low-mass dimuons from the in-medium ρ^0 decay are shifted toward higher momentum when emit-
 78 ted from the hadronic medium with a large radial flow while the higher mass thermal dimuons
 79 are mainly from a partonic medium at an earlier stage of the collision. The HADES experiment
 80 recently showed that the dielectron mass spectrum exhibits a near-exponential fall-off in the low-
 81 mass region in Au+Au collisions at $\sqrt{s_{NN}} = 2.42$ GeV ³¹. The average temperature extracted from
 82 this exponential spectrum was determined to be 71.8 ± 2.1 MeV. Although its kinematic reach is
 83 below ρ^0 pole mass, it indicates that the ρ^0 resonance spectrum is significantly altered and that
 84 frequent interactions among the baryons in the dense hadronic medium could produce a seemingly
 85 thermalized system. These previous measurements and knowledge at lower beam energies provide
 86 the necessary baselines for temperature measurements at different stages of the collisions at higher
 87 energies.

88 In this article, we present dielectron spectra in Au+Au collisions at beam energies from
 89 $\sqrt{s_{NN}} = 19.6$ to 200 GeV using data collected from the STAR Detector at RHIC from year 2010

90 to year 2018 including two high-statistic datasets at $\sqrt{s_{NN}} = 19.6$ and 54.4 GeV. The temperature
91 of hot nuclear matter from the thermal dielectrons in the low-mass and intermediate-mass regions
92 are extracted. These results provide access to the thermodynamic properties at both the early stage
93 of the QGP phase as well as the late stage near the phase transition to the hadronic matter.

94 **2 Experiment**

95 The thermal dielectrons in this study are measured with the STAR experiment at RHIC. The most
96 relevant STAR detectors for this study are depicted in Fig. 2 (top panel) with a typical event display
97 from the collisions. The charged particles produced in collisions leave ionization trails inside
98 STAR's Time Projection Chamber (TPC). The curvature of a particle trajectory in the magnetic
99 field is used to derive its rigidity (the momentum p divided by the charge q) and the ionization
100 energy loss (dE/dx) deposited along the track inside the gas of the TPC is used to identify the
101 particle species. This measurement of the dE/dx as a function of the particle rigidity (p/q) is
102 illustrated in Fig. 2 (bottom-left panel). In addition, the velocity (β) and mass [$m^2 = p^2(1/\beta^2 -$
103 $1)$] of a charged particle originating from the collision point can be measured by the time-of-
104 flight detector (TOF) surrounding the outer barrel of the TPC. The electrons of interest have the
105 characteristics of the dE/dx relativistic rise and the low electron mass as shown in Fig. 2 (bottom-
106 right panel). This combination of two powerful particle identification tools enables the STAR
107 detector to provide excellent electron identification with a hadronic background rejection power of
108 1:10000 and better. The excellent electron identification and large fiducial acceptance make such
109 difficult measurement possible. The identified electrons and positrons from the same event are

110 paired to reconstructed pair mass and transverse momentum. However, more than 99% of these
111 pairs are from random combinations (combinatorial background), which need to be subtracted to
112 obtain the raw inclusive dielectron signals. After correcting for the pair reconstruction efficiency
113 and acceptance, the fully corrected inclusive dielectron signals can be calculated. The black dots in
114 top two panels of Figure. 3 show the fully corrected inclusive dielectron invariant mass spectrum.
115 More details on the measurements can be found in Method section.

116 The measured dielectrons are accumulative contributions from various stages of the evolution
117 of the heavy-ion collisions. These include dielectrons from the thermal QCD medium of the colli-
118 sion as well as the non-thermal physics sources, commonly referred to as “cocktails”. At the initial
119 impact of the collision, dielectrons can be produced through the annihilation of valence quarks
120 and sea anti-quarks between colliding target and projectile nuclei (Drell-Yan process). After the
121 hot medium has disintegrated at the very late stage, the dielectrons can also be produced from the
122 decays of long-lived hadrons (Dalitz decays: $\pi^0, \eta, \eta' \rightarrow \gamma e^+ e^-$ and $\omega \rightarrow \pi^0 e^+ e^-, \phi \rightarrow \eta e^+ e^-$;
123 two body decays: $\omega, \phi, J/\psi \rightarrow e^+ e^-$ or the semi-leptonic decays of open charm hadrons). The
124 contributions from these physics backgrounds can be well determined via the cocktail simulation
125 techniques and are shown as the dashed curves in the top two panels of Fig. 3. The black curves
126 show the sum of all physics background contributions (Cocktail Sum). The fully corrected data ex-
127 ceeds the Cocktail Sum substantially over a large mass region, indicating clear contributions from
128 thermal dielectrons. To quantify the thermal contributions, the excess dielectron mass spectrum
129 are obtained by subtracting the Cocktail Sum from the fully corrected data. Further details about
130 the cocktail simulations can be found in the Method section.

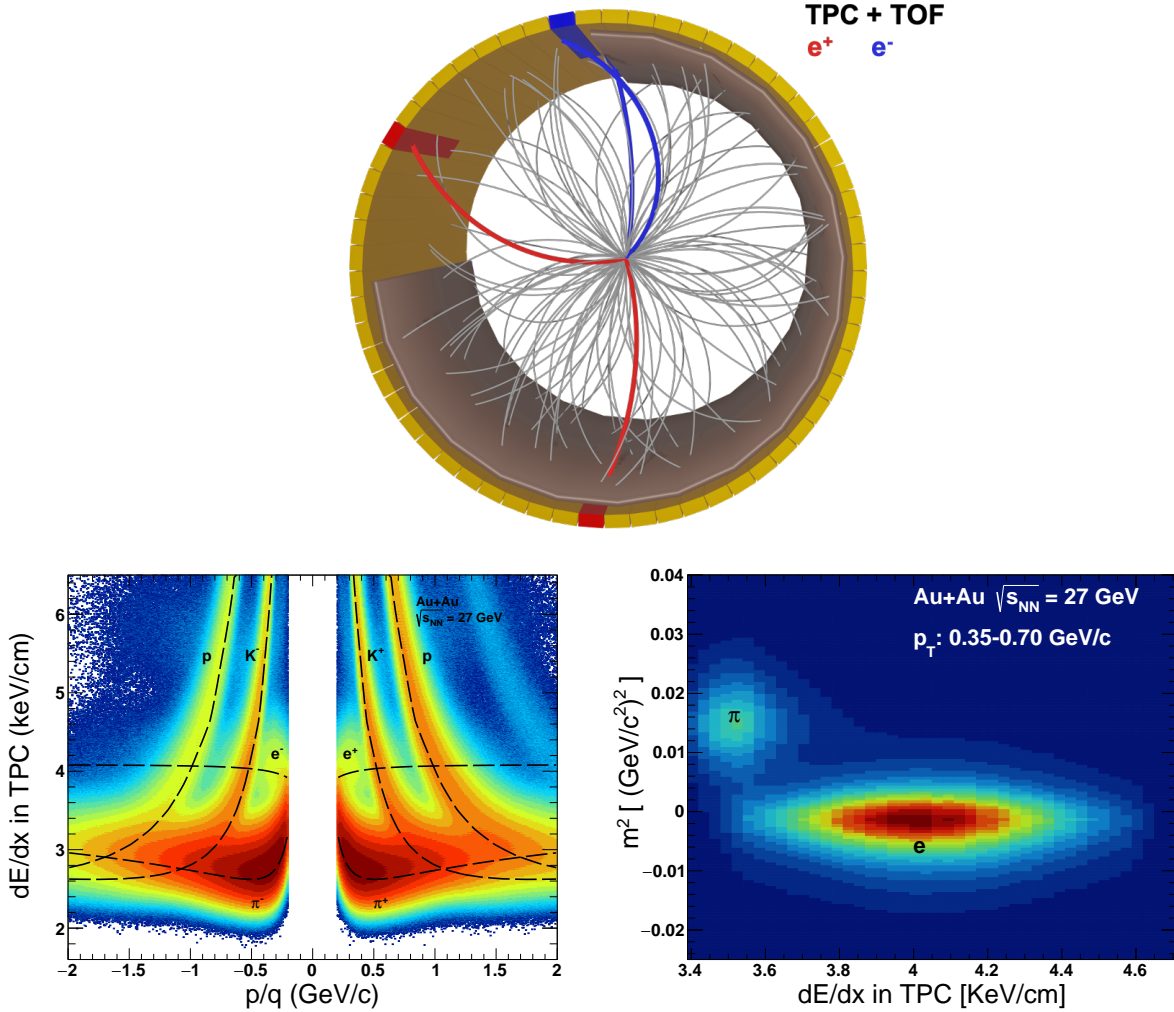


Figure 2: (Color online) **A schematic display of a Au+Au collision reconstructed with the STAR detector.** Top panel shows that charged particles ionize the gas in the STAR TPC, forming three-dimensional tracks (gray lines) that curve under the magnetic field of the detector. As tracks exit the outer radius of TPC, they leave signals (red and blue trays) in the time-of-flight (TOF) detector. Electron (blue lines) and positron (red lines) tracks are identified based on the normalized ionization energy loss (dE/dx) and the mass square (m^2) derived from the velocity (β) by TOF and momentum (p) from TPC. The bottom-left panel shows the dE/dx as a function of momentum and the bottom-right panel shows the m^2 v.s. dE/dx distribution, respectively.

131 3 Results and Discussions

132 The measured invariant-mass spectra of the thermal dielectron (excess dielectron) are shown in the
133 bottom two panels of Fig. 3. The spectra are normalized by the charge multiplicity dN_{ch}/dy in
134 order to compare the measurements among different colliding species and beam energies. The left
135 panel of Fig. 3 shows the results in the low-mass region (LMR), and it is observed that the STAR
136 data from both 54.4 GeV and 27 GeV Au+Au collisions are consistent with each other within
137 the entire mass region. Additionally, the STAR data at LMR also show good agreement with the
138 dimuon spectrum from In+In collisions at $\sqrt{s_{NN}} = 17.3$ GeV while those at IMR at STAR are sys-
139 tematically higher than that at lower energy. This may indicate that the thermal dileptons at LMR
140 from these three measurements are radiated sources with similar temperature and density while
141 there is an indication that the dileptons from IMR are from sources with different temperature.
142 To quantify the temperature of the thermal source responsible for LMR radiation, a function that
143 combines the in-medium resonance structure and the structure-less shape is used to fit the mea-
144 sured mass spectrum. The in-medium resonance shape is described by a relativistic Breit-Wigner
145 function, BW , multiplied by the Boltzmann factor $PS = exp(-M/T)$ to account for the phase
146 space^{43,44}. In this function, $BW = MM_0\Gamma/[(M_0^2 - M^2)^2 + M_0^2\Gamma^2]$, M is the invariant mass of
147 the pair, $\Gamma = \Gamma_0 \times (M_0/M) \times [(M^2 - 4m^2)/(M_0^2 - 4m^2)]^{3/2}$ is the width, Γ_0 and M_0 are width
148 and pole mass of ρ^0 meson while the m is the mass of the decayed lepton. If the ρ^0 is completely
149 dissolved inside the medium, its mass structure spreads out and approaches a smooth distribution
150 similar to the the quark-antiquark continuum (QGP thermal radiation) which can be described by
151 $M^{3/2} \times exp(-M/T)$ as pointed out in ref.^{16,31}. The extracted temperatures (T_{LMR}) from LMR

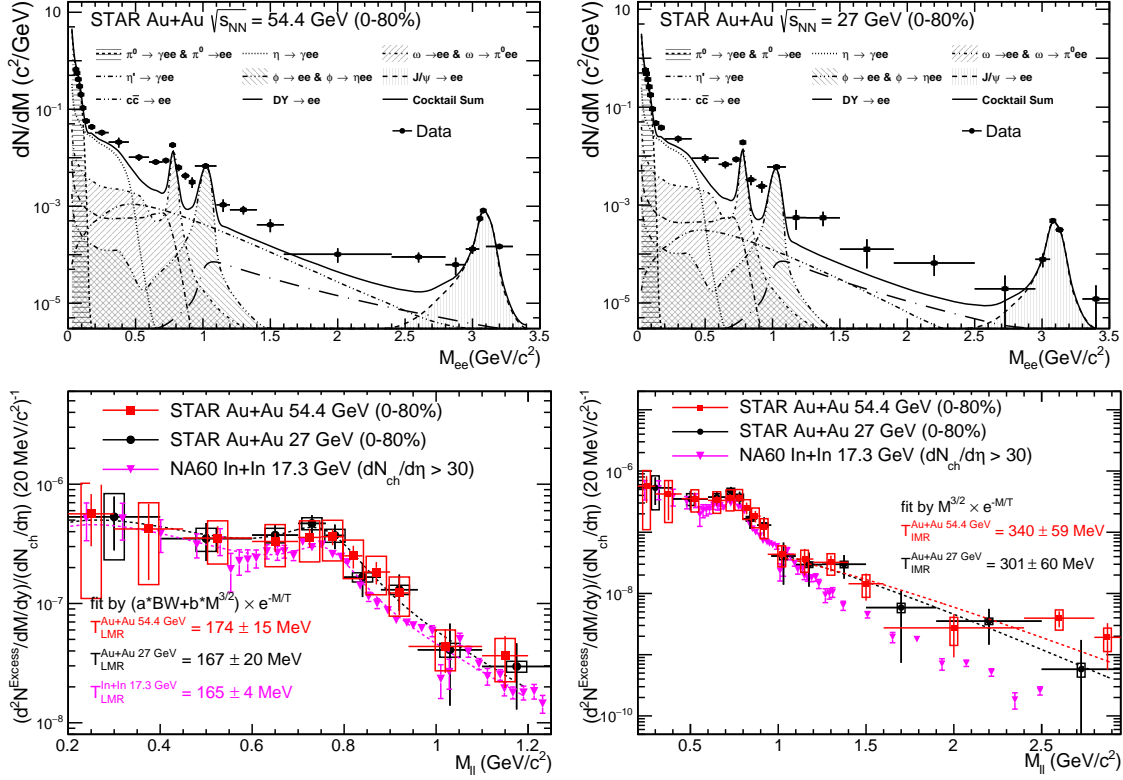


Figure 3: (Color online) **Dielectron invariant mass spectrum.** Top two panels show the fully corrected inclusive dielectron mass spectrum (black dots) compared to the physics background (dashed and shaded lines) in Au+Au collisions at $\sqrt{s_{NN}} = 54.4$ GeV and 27 GeV. Bottom two panels show the thermal dielectron mass spectrum from 54.4 GeV (red dots) and 27 GeV (black dots) compared to the NA60 thermal dimuon data (blue inverted triangles). Vertical bars and boxes around data points represent the statistical and systematic uncertainties, respectively.

152 thermal dielectron mass spectrum are 167 ± 20 MeV and 174 ± 15 MeV for the Au+Au collisions
 153 at $\sqrt{s_{NN}} = 27$ and 54.4 GeV, respectively. The similar fit to NA60 data gives a temperature of
 154 165 ± 4 MeV. The extracted temperatures from the LMR thermal dileptons of different collision
 155 energies and species are consistent with each other, and suggestive that they are radiated from
 156 thermal sources with similar temperature. In the intermediate mass region (IMR, $1 < M < 2.9$
 157 GeV/ c^2), data between 27 GeV and 54.4 GeV Au+Au collisions are consistent within uncertainty
 158 and slightly higher than the data from NA60. The mass spectrum in this mass region is smoothly
 159 distributed, and the temperature is extracted using the continuum shape $M^{3/2} \times \exp(-M/T)$, as
 160 predicted in ref. ¹⁶. The extracted temperatures T_{IMR} for the 27 GeV and 54.4 GeV Au+Au col-
 161 lisions are 301 ± 60 MeV and 340 ± 59 MeV, respectively. When fitting to the thermal dimuon
 162 spectra of NA60 data in this mass region, the temperature is 246 ± 15 MeV. These temperatures re-
 163 flect an average over a certain period of the space-time evolution of the hot medium. The extracted
 164 temperature for the low-mass region is significantly lower than that of the intermediate-mass re-
 165 gion. This observation is consistent with the expectation that LMR thermal dileptons are emitted
 166 at a later stage of the medium evolution around phaser transition while those at the IMR are mainly
 167 from the earlier stage with much higher temperature.

168 Figure. 4 summaries the temperature measured as a function of the baryonic chemical poten-
 169 tial. The chemical freeze-out temperature T_{ch} and baryonic chemical potential μ_B can be well
 170 determined via analyzing the hadron production yields with the statistical thermal models ¹⁸.
 171 The chemical freeze-out temperatures extracted from the statistical thermal models (SH, GCE,
 172 SCE) ^{18,45} are shown as solid dots and open circles in the figure. Theoretical studies of lattice

173 QCD at the small μ_B predict a crossover type of phase transition with continuous, smooth but
 174 rapid increase of thermodynamic quantities in a narrow region around the critical temperature
 175 $T_C = 156 \pm 5$ MeV at $\mu_B = 0$. It decreases slightly towards higher μ_B as shown in the green band
 176 in the figure. In the meanwhile, we also extracted the temperatures based on the low-mass thermal
 177 dielectron spectra published with the STAR BES-I data in Au+Au collisions at different collision
 178 energies of $\sqrt{s_{NN}} = 19.6, 37, 62.4, 200$ GeV^{38,40}. A temperature was extracted with the contin-
 179 uous shape of $M^{3/2} \times \exp(-M/T)$. This simplification was determined by the limited statistics
 180 in those measurements and that the resonance structures of the in-medium ρ^0 were removed due
 181 to the over-subtraction of ω meson and ϕ meson contributions in that analysis approach^{38,40}. Fu-
 182 ture BES-II data with high statistics may be more sensitive to the different functional forms. The
 183 extracted T_{LMR} are shown as open blue squares in the figure, and are in good agreement with the
 184 new STAR results from data at collisions beam energies of 27 GeV and 54.4 GeV as well as the
 185 result (blue rhombus) extracted from NA60 data. Moreover, all the temperatures are found to stay
 186 around the phase transition temperature T_C and the chemical freeze-out temperature T_{ch} .

187 It has been a long-standing challenge and open issue on the phenomenological observation
 188 that the temperature (T_{ch}) extracted from the chemical yields of the final-state hadrons coincides
 189 with the QCD phase transition temperature (T_C) from the Lattice QCD¹⁸. Can the present dilep-
 190 ton measurements provide new insight in resolving such an issue? Stable hadrons emerge from the
 191 chemical freeze-out at that instant and their yields are an integration over the whole volume of the
 192 system. Therefore, the extracted temperature by definition could not be higher than the hadroniza-
 193 tion and phase transition temperature. In principle, yields of the low-mass thermal dileptons are

194 accumulative from the QGP stage to the kinetic freeze-out. Therefore, the yield is an integration
195 over the whole system volume and over the entire evolution time duration. In comparison of the
196 dilepton yields normalized by the total number of charged particles from heavy-ion collisions to
197 the expected yields from the hadronic channel in $p + p$ collisions and from the thermal model pre-
198 dictions, we further found that the dielectron yields is more than a factor of 5 larger than those two
199 baseline yields (see Method and BES-I ^{38,40}). The high yields of dileptons, the strong in-medium
200 broadening of ρ spectral function and the coincidence of three temperatures (T_C , T_{ch} and T_{LMR})
201 suggest that the low-mass thermal dileptons be dominantly emitted over a long period of time at
202 high density with a constant temperature. Such scenario is possible if it happens around a phase
203 transition and/or the softest point of an equation of state. This in turn provides a direct experi-
204 mental tool for accessing the temperature at the vicinity where the deconfinement phase transition
205 occurs - one of the most fundamental landmarks of the QCD phase diagram.

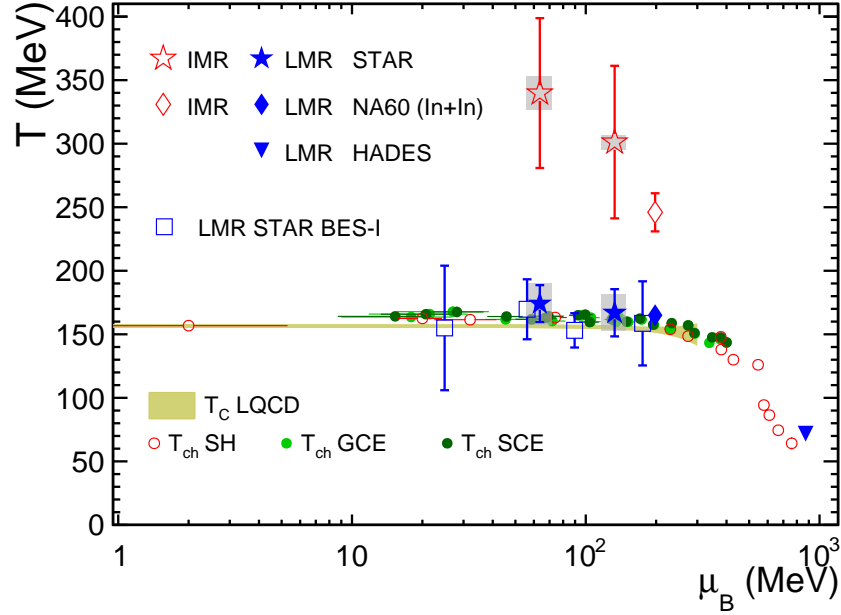


Figure 4: (Color online) **Temperatures vs. baryonic chemical potential.** Temperatures extracted from in-medium ρ ; (Blue solid stars) dominant region and QGP (open red stars) dominant region from STAR data are compared to the temperatures extracted from NA60 data (Blue rhombus and open red rhombus) and HADES data (blue invert triangle). Chemical freeze-out temperatures extracted from the statistical thermal models (GCE, SCE, SH) are shown as solid dots and open circles. The QCD critical temperature T_C at finite chemical baryon density predicted by lattice QCD calculations are shown as green band. Vertical bars and shaded boxes around data points represent the statistical and systematic uncertainties, respectively.

206 **4 Summary**

207 In this study, we present the first direct measurements of the temperature of the strongly interacting
208 hot QCD matter created in Au+Au collisions at RHIC via the thermal dielectrons. Our measure-
209 ments reveal that the extracted temperatures from the low-mass thermal dielectrons are consistently
210 close to the QCD phase transition temperature derived in lattice QCD calculations and the chemical
211 freeze-out temperature deduced from statistical hadronization models. This finding provides the
212 first direct experimental evidence that the in-medium ρ^0 vector meson is predominantly produced
213 around the phase boundary of QCD matter created in heavy-ion collisions at both RHIC and SPS.
214 The temperature extracted from the intermediate mass thermal dielectrons is $(3.72 \pm 0.49) \times 10^{12}$
215 Kelvin much higher than the phase transition temperature, consistent with the expectation that their
216 dominant emission source is the deconfined QCD matter, the QGP. This work provides important
217 experimental thermodynamic measurements to map the QCD phase diagram and understand the
218 properties of matter under extreme conditions.

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