

PWG preview: Differential  
measurements of  $\phi$ -meson global  
spin alignment in Au+Au collisions  
at RHIC  
(Addressing Comments)

Gavin Wilks ([gwilks3@uic.edu](mailto:gwilks3@uic.edu))

University of Illinois at Chicago

02/07/2023

# General Information

- Paper title: Differential measurements of  $\phi$ -meson global spin alignment in Au+Au collisions at RHIC
- PAs: Diyu Shen (Fudan), Xu Sun (IMP), Aihong Tang (BNL), [Gavin Wilks \(UIC\)](#), Zhenyu Ye (UIC)
- Targeted journal: Physical Review Letters
- Webpage: <https://drupal.star.bnl.gov/STAR/blog/gwilks3/Differential-Measurements-phi-meson-Global-Spin-Alignment-Paper-Proposal>
- Previous presentation: [https://drupal.star.bnl.gov/STAR/system/files/PWG\\_Preapproval\\_v5.pdf](https://drupal.star.bnl.gov/STAR/system/files/PWG_Preapproval_v5.pdf)

# Comments from convenors

- Explore polynomial background as a source of systematic error.
- Add plots for systematic variations.
- Add  $\rho_{00}$  values for each stage of correction.
- Look at yield vs  $\cos\theta^* = [-1,1]$  for possible asymmetries.
- Investigate effect from rapidity spectra shape in simulation.

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# Polynomial residual background

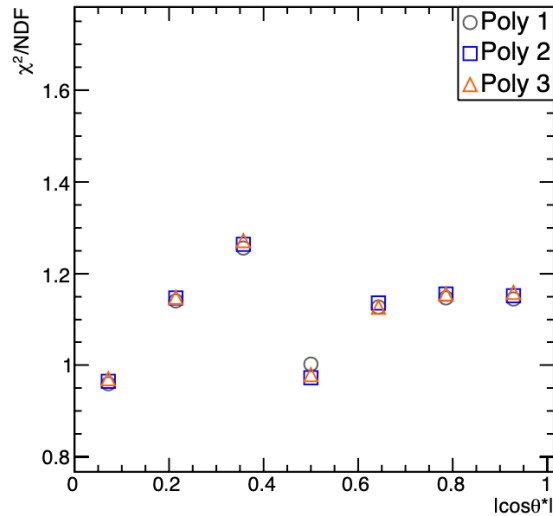
## *Updates*

- Default polynomial background changed to poly1 from poly3.
- Consider poly2 as a systematic variation
- $\chi^2/\text{ndf}$  is similar for each Poly{1,2,3}; therefore, we prefer to use the lowest order polynomial.

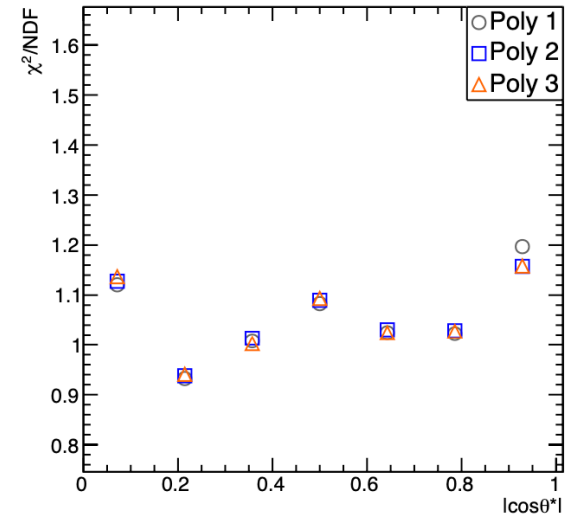
# Polynomial residual background

Example of  $\chi^2/\text{ndf}$  for individual Breit-Wigner+PolyN fits over  $|\cos\theta^*|$ .

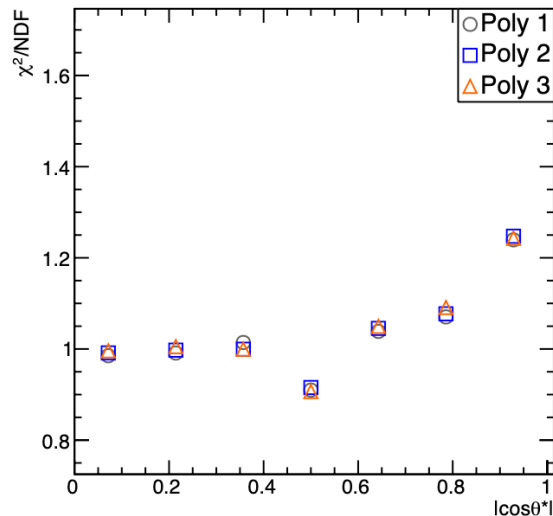
$p_T = [1.2, 1.8] \text{ GeV/c}$



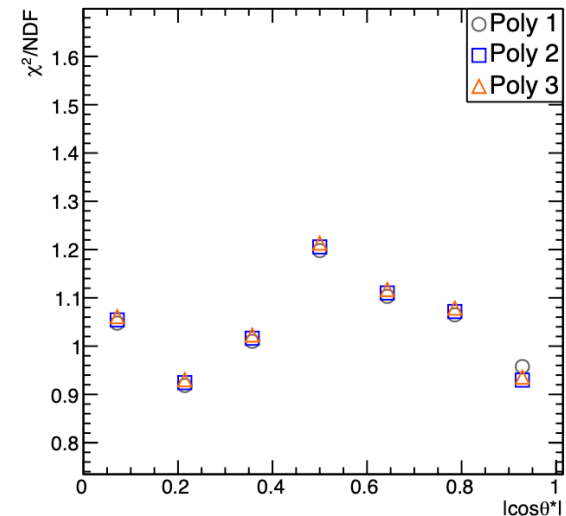
$p_T = [1.8, 2.4] \text{ GeV/c}$



$p_T = [2.4, 3.0] \text{ GeV/c}$



$p_T = [3.0, 4.2] \text{ GeV/c}$



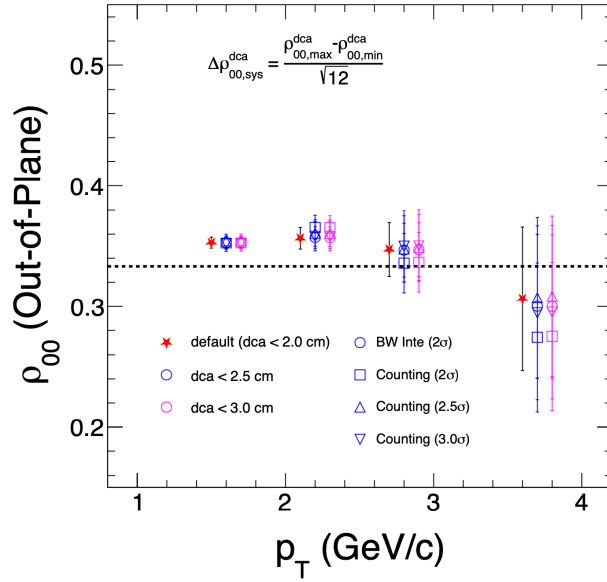
# Systematic Uncertainties

Red marks the default value

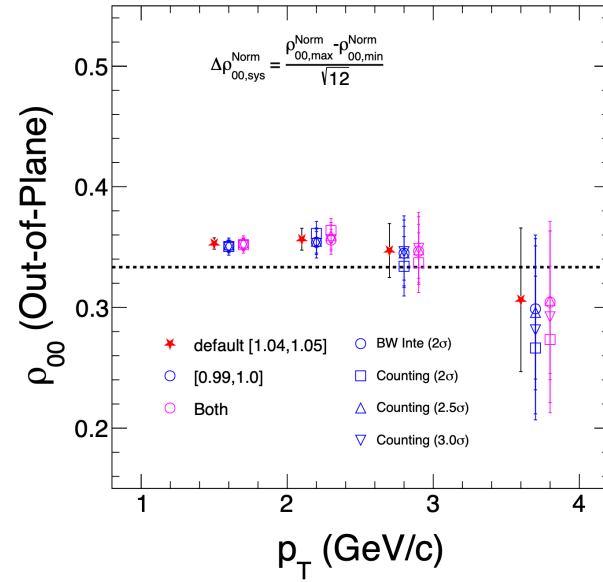
- $n\sigma_K$ : 2.0, 2.5, 3.0
- dca : 2.0, 2.5, 3.0
- Background normalization range: [1.04, 1.05] , [0.99, 1.0] , average of both
- Yield extraction method: bin counting, integration
- Yield extraction range:  $2.0\sigma$ ,  $2.5\sigma$ ,  $3.0\sigma$
- Polynomial residual background: polynomial 1, polynomial 2
- Difference between negative and positive rapidity bins for rapidity dependent study. Default is statistical error weighted mean of positive and negative bin.

# $p_T$ dependence 14.6 GeV EP Order 1

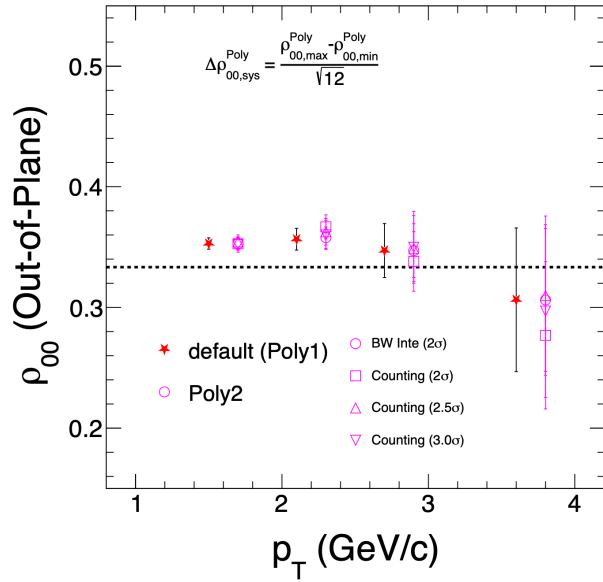
DCA Cuts Systematics @ AuAu 14.6 GeV EP Order 1



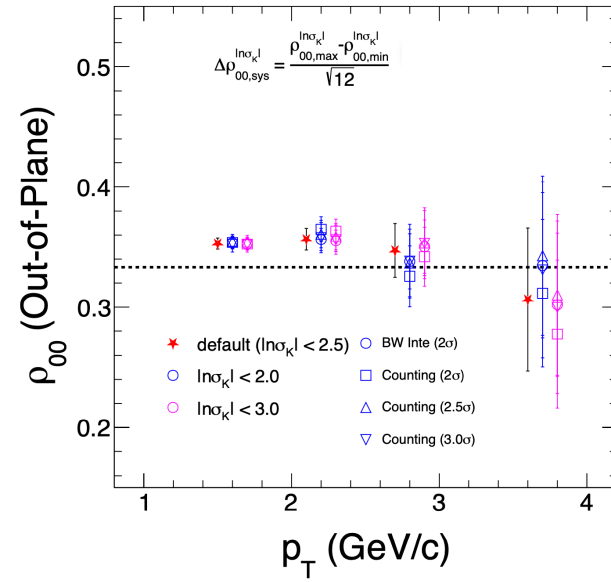
Normalization Systematics @ AuAu 14.6 GeV EP Order 1



Residual Background Systematics @ AuAu 14.6 GeV EP Order 1



$\ln\sigma_k$  Cuts Systematics @ AuAu 14.6 GeV EP Order 1



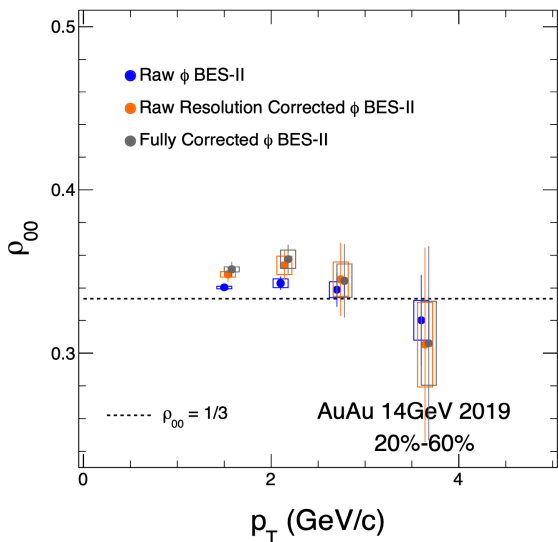


# Comments from convenors

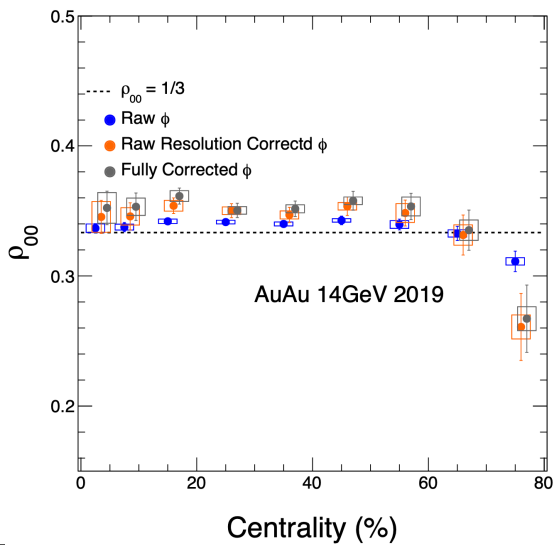
- Explore polynomial background as a source of systematic error.
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EP Order 1

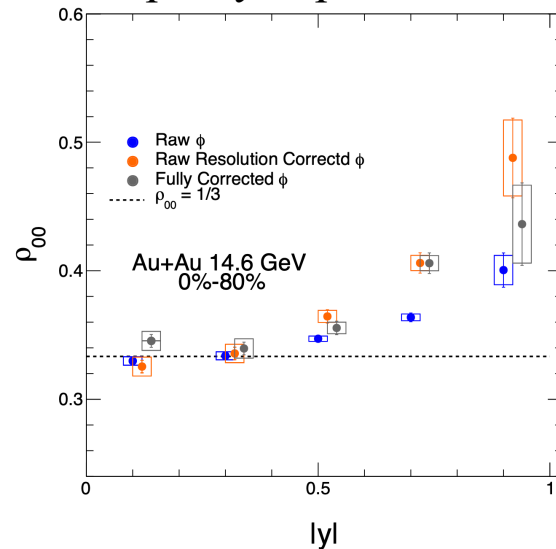
$p_T$  dependence



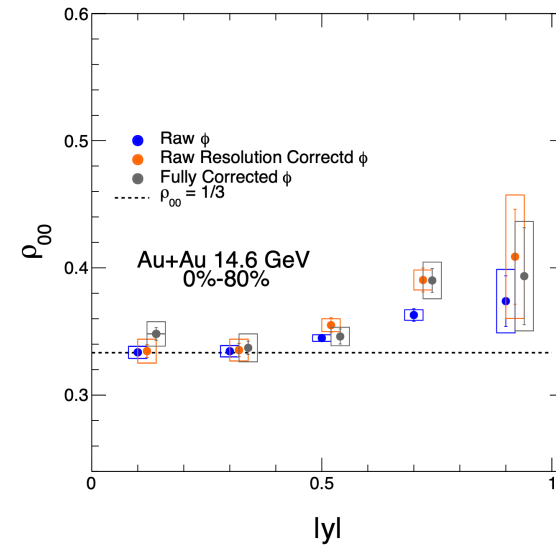
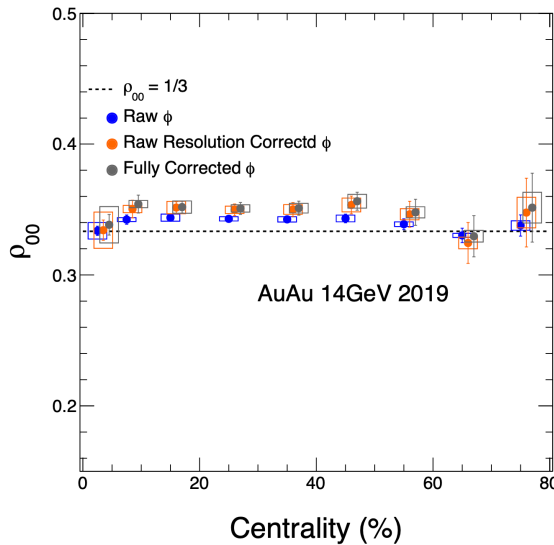
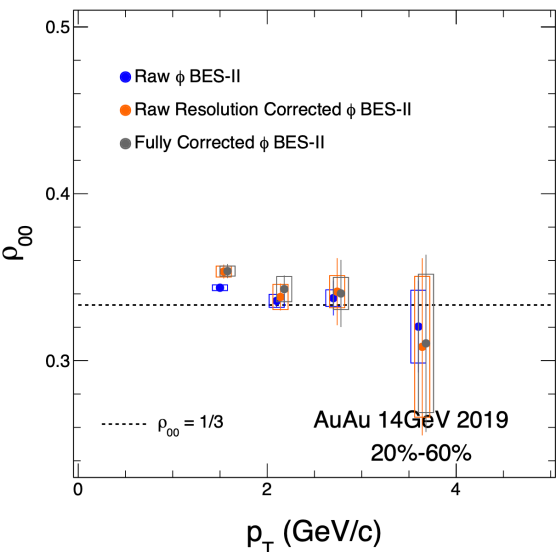
centrality dependence



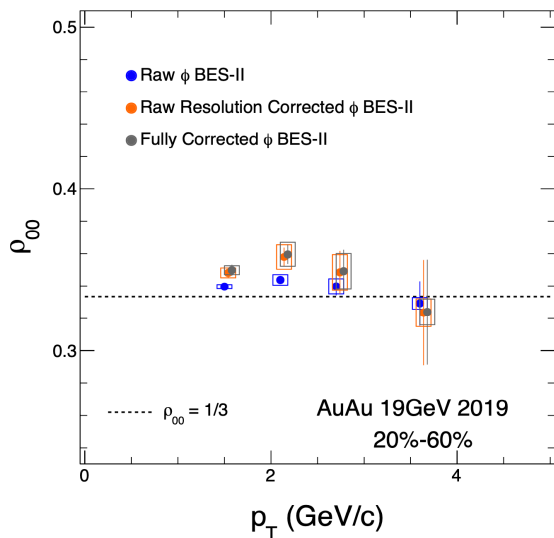
rapidity dependence



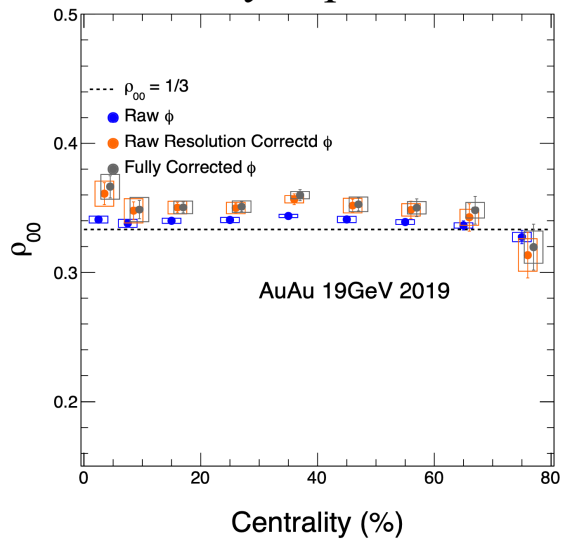
EP Order 2



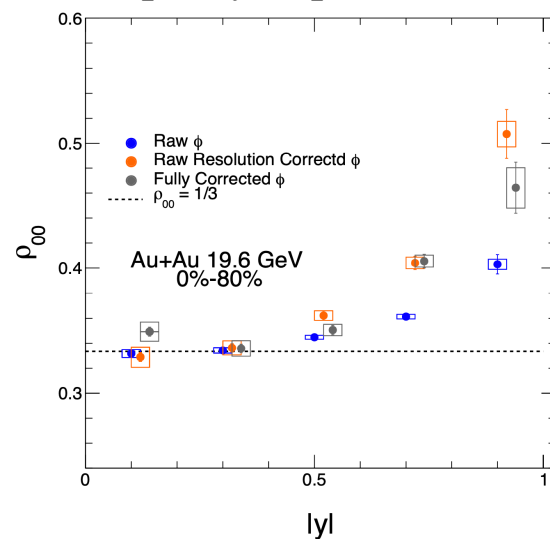
EP Order 1

 $p_T$  dependence

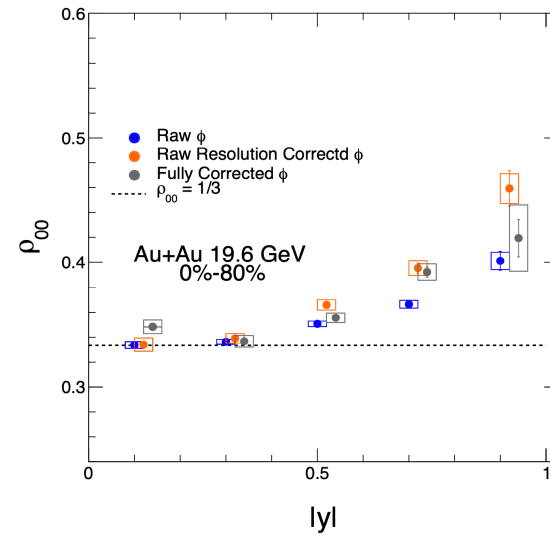
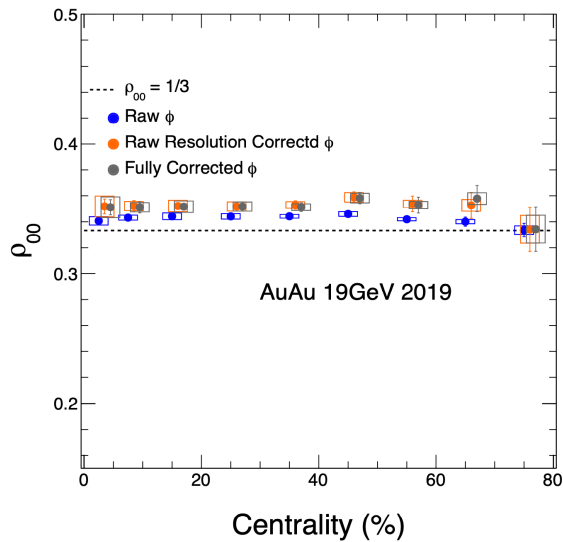
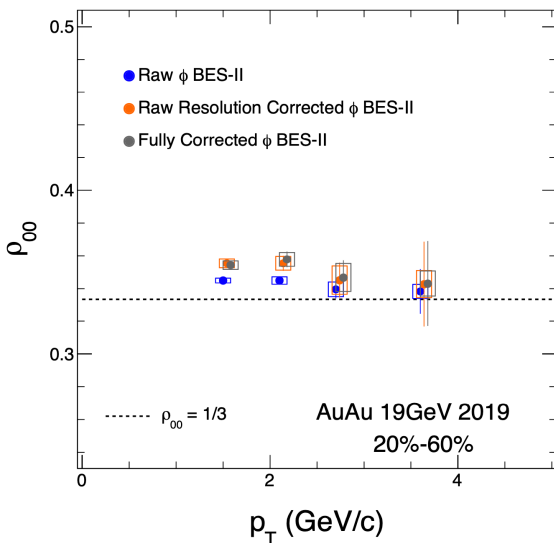
## centrality dependence



## rapidity dependence



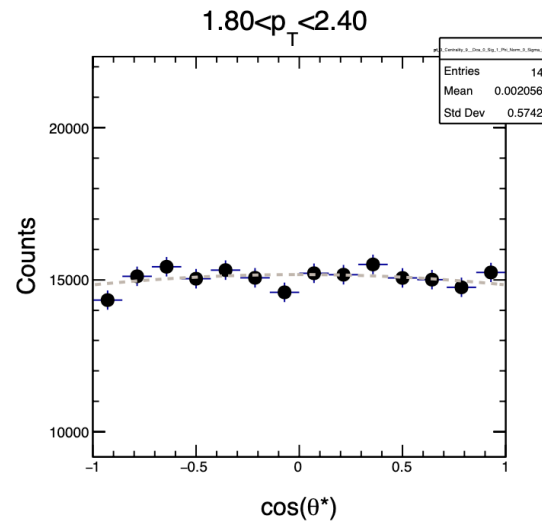
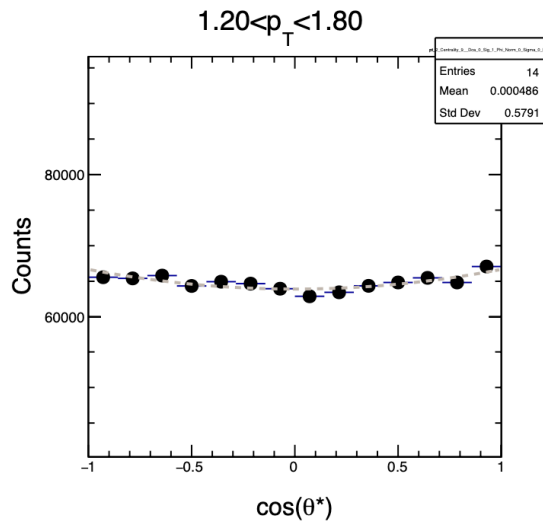
EP Order 2



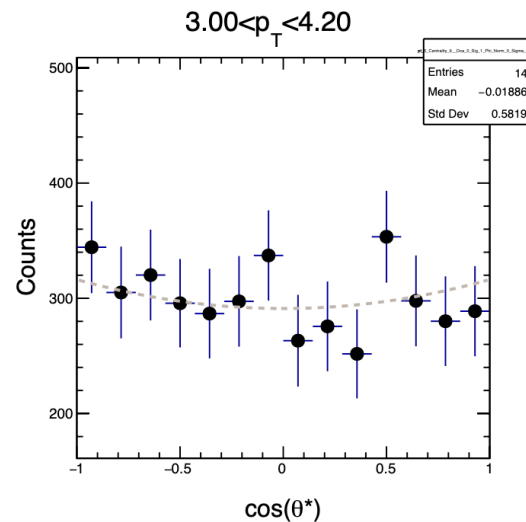
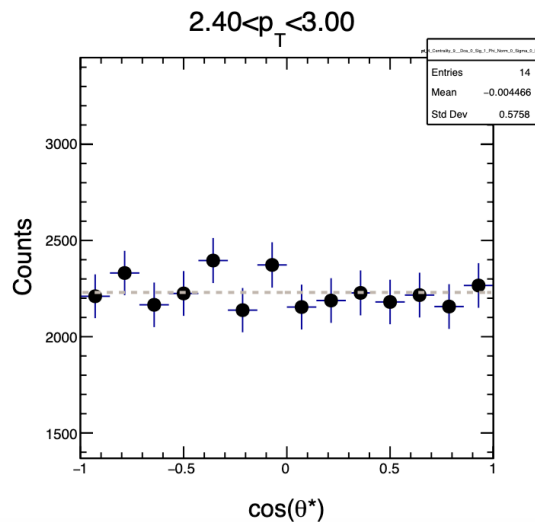
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- Investigate effect from rapidity spectra shape in simulation.

# Signed $\cos(\theta^*)$ distributions



- No apparent asymmetry in the  $\cos(\theta^*)$  distribution.

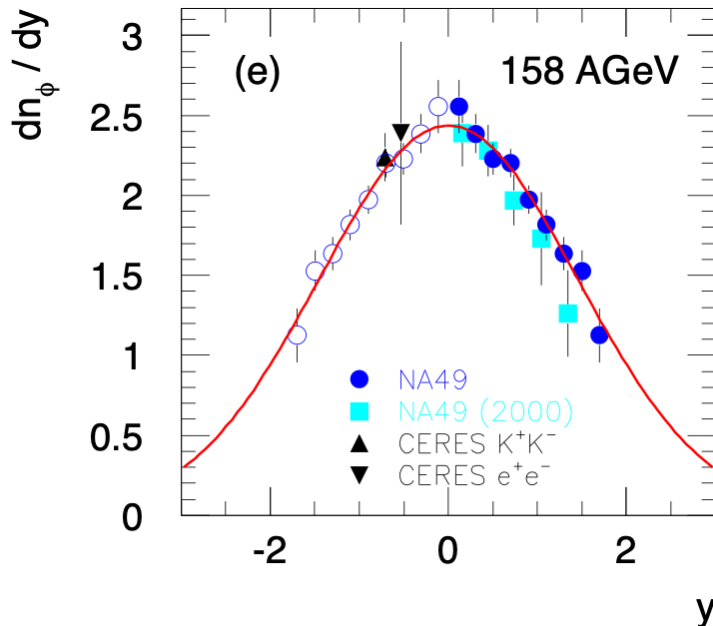


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# Rapidity Dependence in Simulation

- In current analysis, we assume flat rapidity in sim.
- Investigate rapidity spectra input to efficiency x acceptance simulation.
- Use results from Pb+Pb data at NA49 at 17.3 GeV



[PhysRevC.78.044907](#)

Pb+Pb collisions (0-5% centrality)

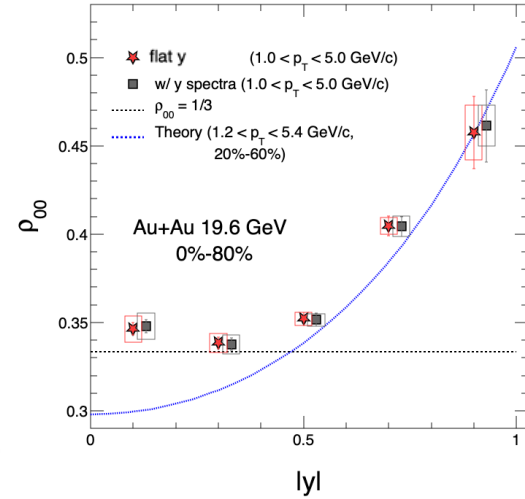
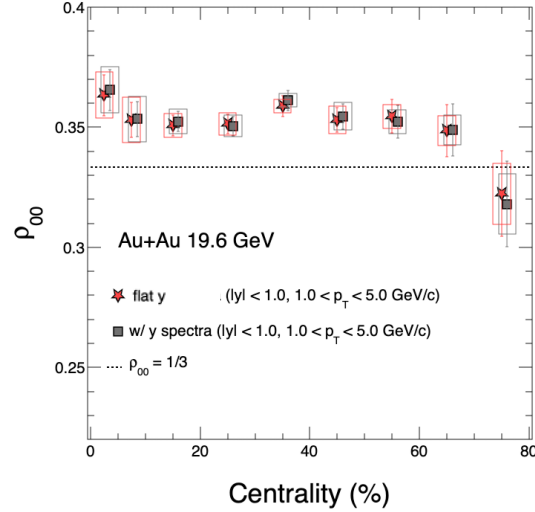
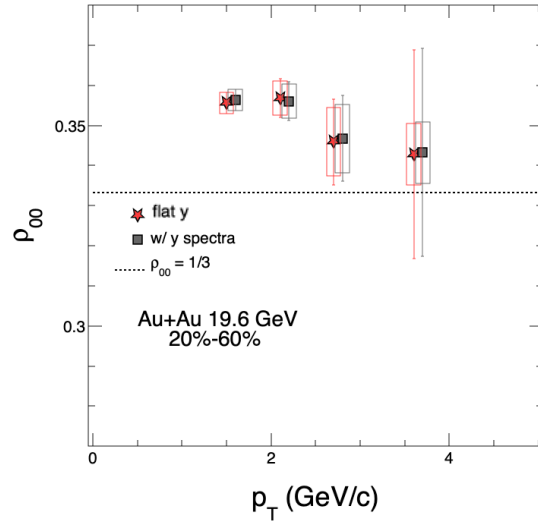
158 AGeV  $\rightarrow \sqrt{s_{NN}} = 17.3$  GeV

$$\frac{dn}{dy} \propto e^{-\frac{y^2}{2\sigma_y^2}} .$$

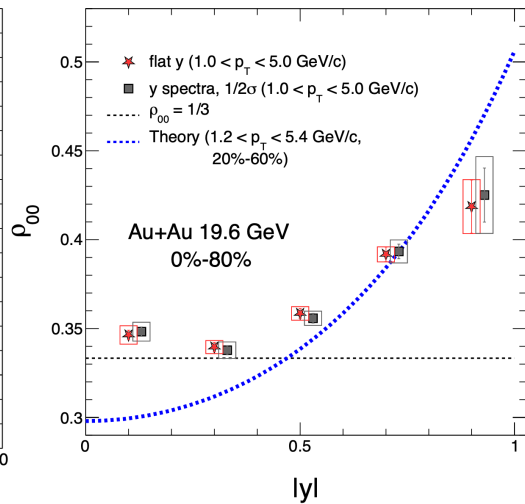
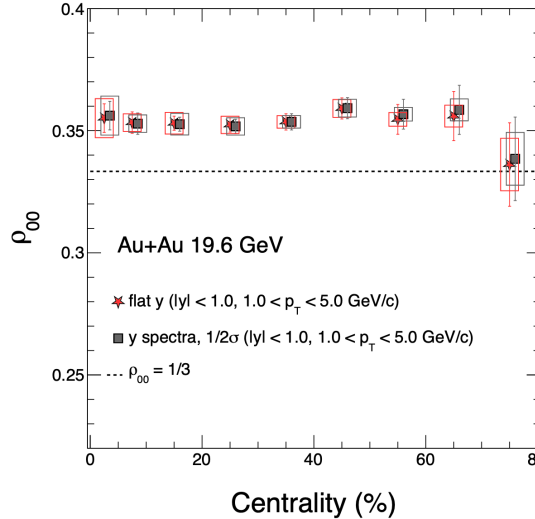
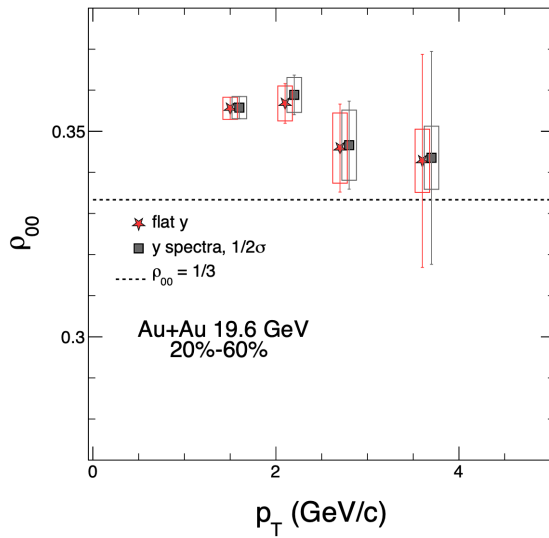
$$\sigma_y = 1.451$$

# Rapidity Dependence in Simulation

$$\sigma_y = 1.451$$



$$\sigma_y = 1.451 * 1/2$$



Non-flat rapidity input to simulation does not significantly affect the final  $\rho_{00}$ .



# Other Comments

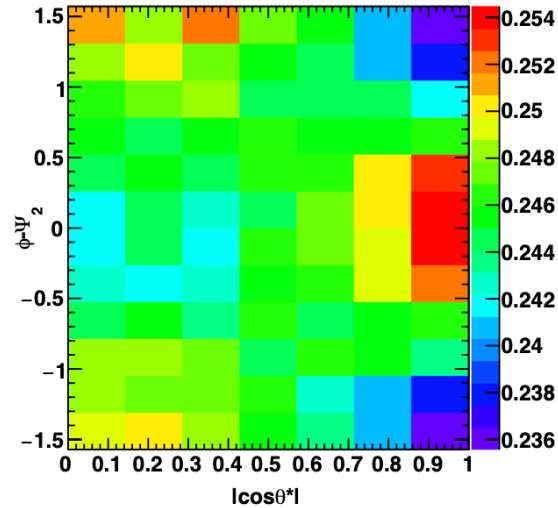
- Did you try to get an efficiency for phi reconstruction as a function of the relative angle of one of the daughters to the phi momentum?
  - We did not perform this study as this does not apply to the method that we are using.
- What values of phi  $v_2(p_T)$  were used?
  - We used preliminary  $\phi$ -meson  $v_2(p_T)$  results for 14.6 GeV and published  $v_2(p_T)$  results for 19.6 GeV from Physical Review C 93 014907.
- How large is the effect of elliptic flow "entanglement" with the efficiency to rho00 calculations?

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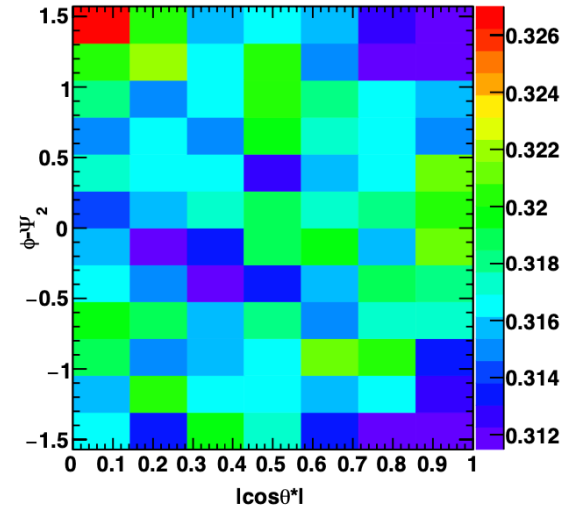
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# EP Dependent Efficiency x Acceptance (pT)

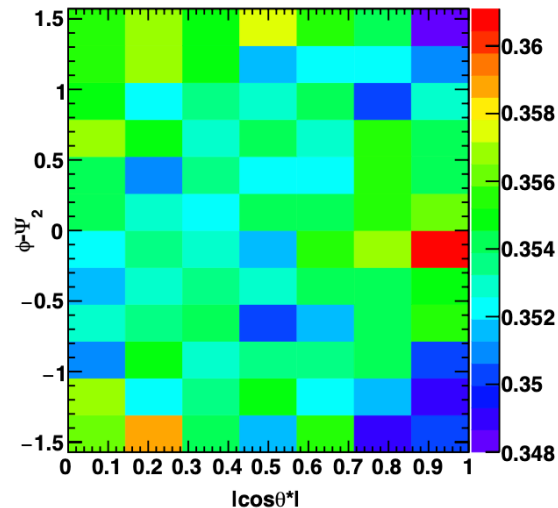
1.2 <math>p\_T</math> < 1.8, Cent 20-60



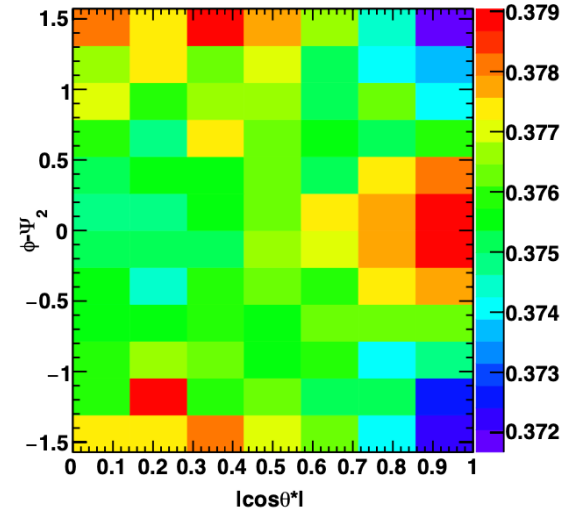
1.8 <math>p\_T</math> < 2.4, Cent 20-60



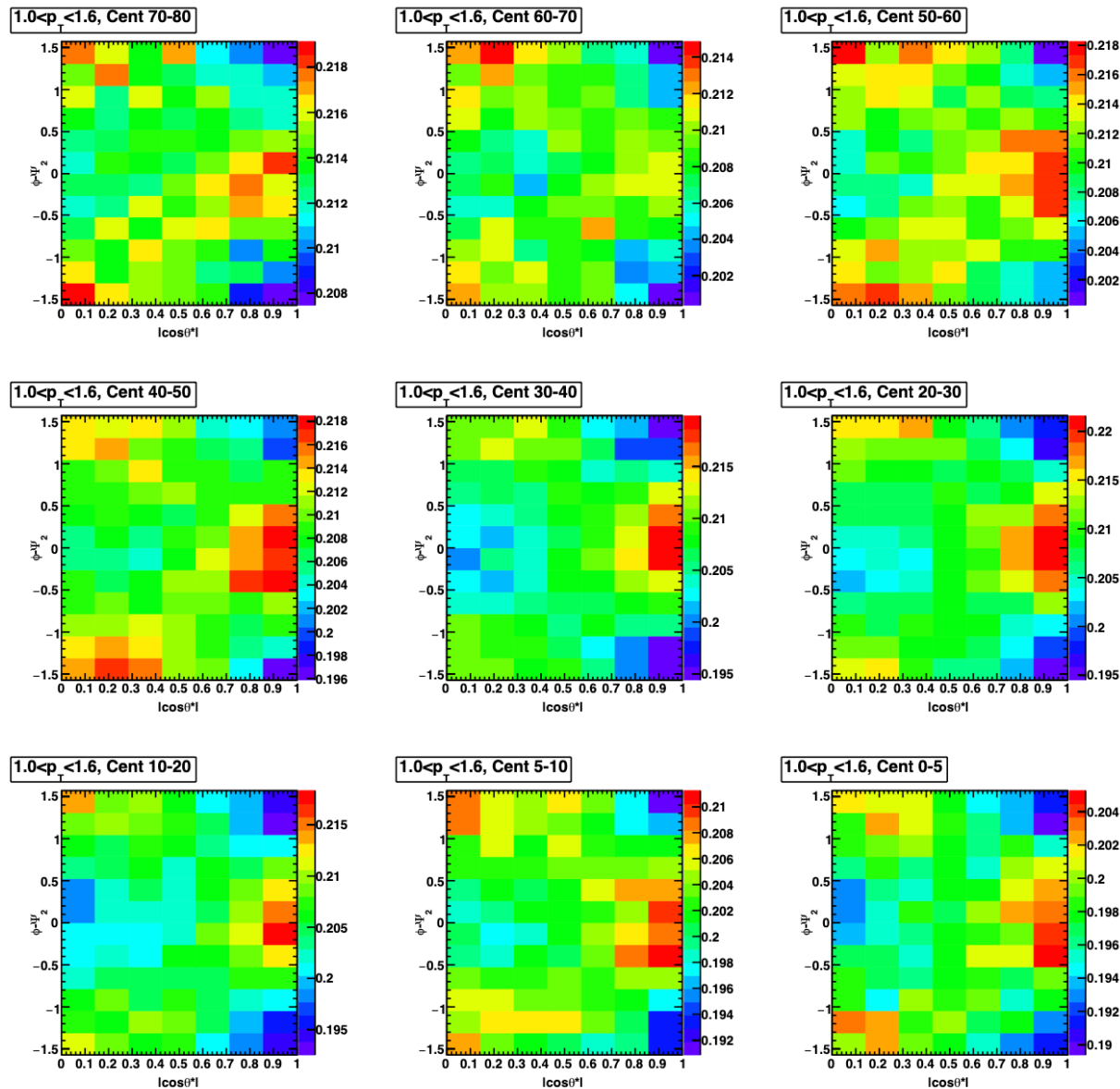
2.4 <math>p\_T</math> < 3.0, Cent 20-60



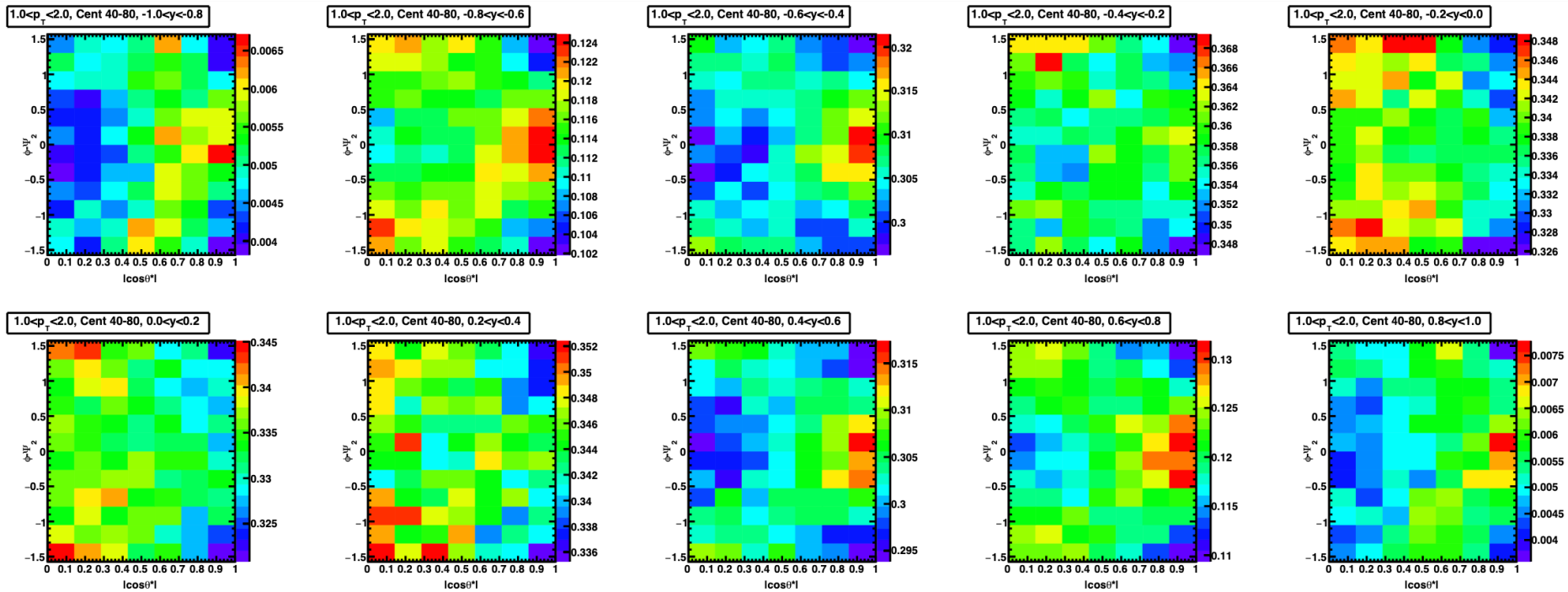
3.0 <math>p\_T</math> < 4.2, Cent 20-60



# EP Dependent Efficiency x Acceptance (Cent)



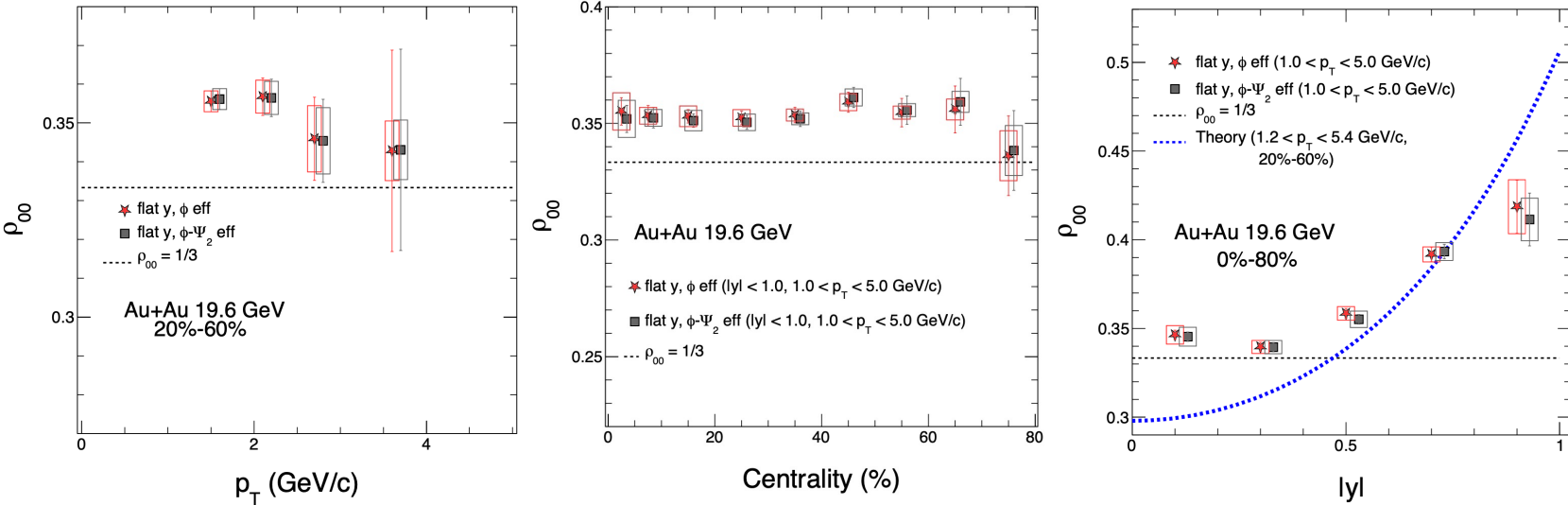
# EP Dependent Efficiency x Acceptance (y)



# EP dependent efficiency and elliptic flow

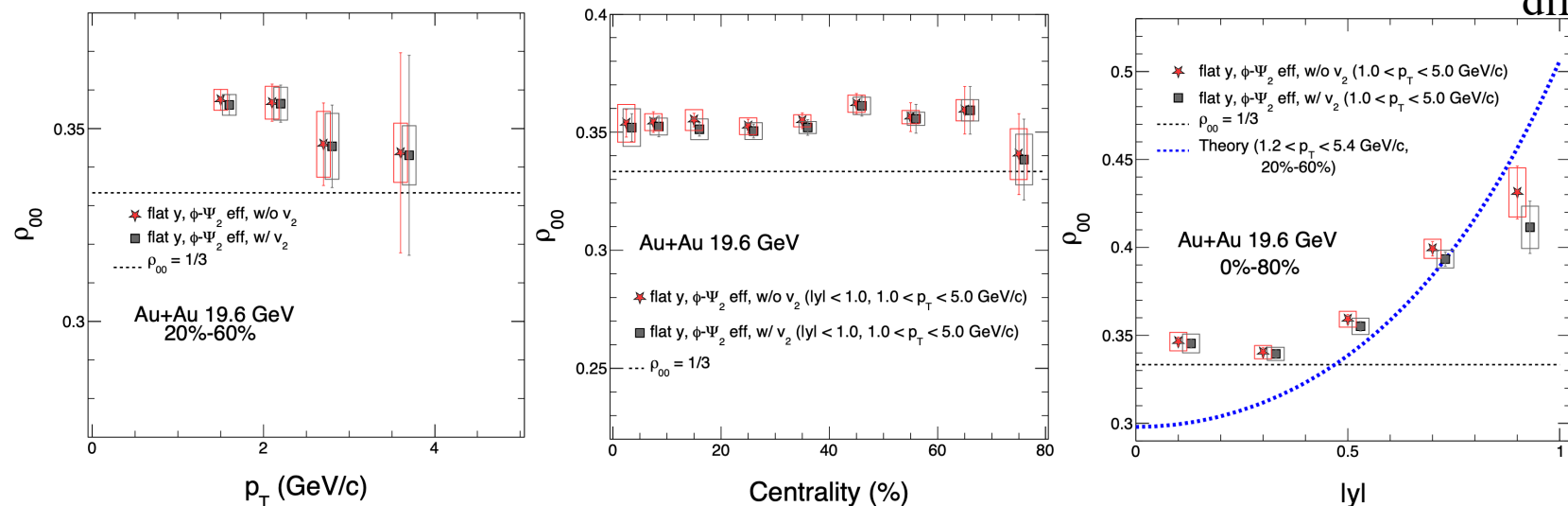
Comparing  $\phi$  dependent efficiency to  $\phi$ - $\Psi_2$  efficiency input to simulation.

No significant difference.

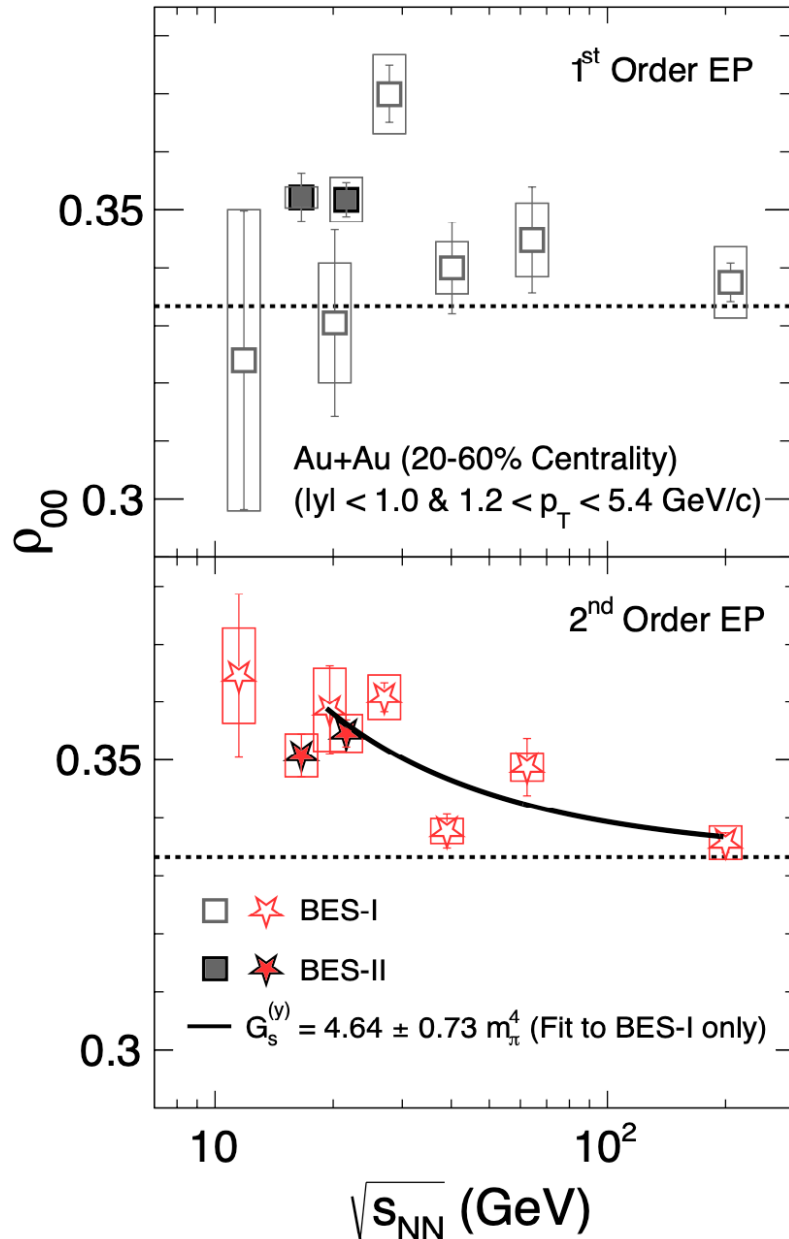


Comparing  $\phi$ - $\Psi_2$  efficiency w/ and w/o elliptic flow input to simulation.

No significant difference.



# Updated Figures

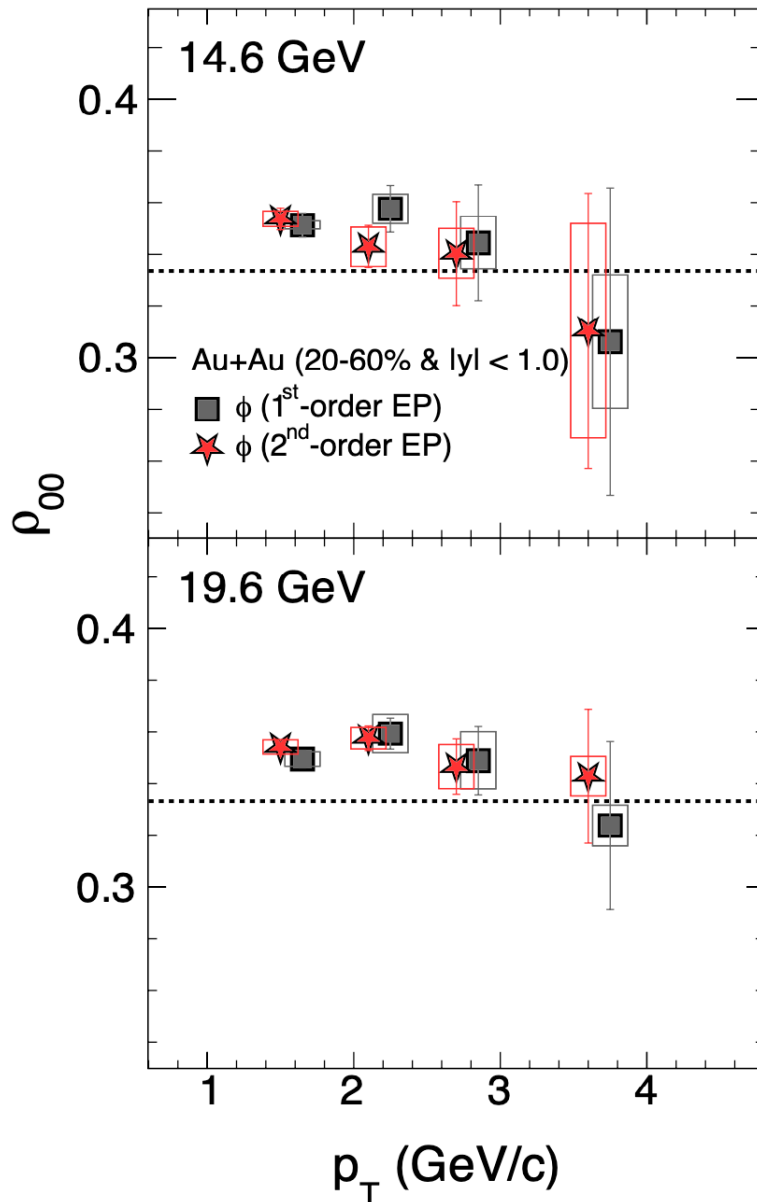


# Figure 1.

Collision energy ( $\sqrt{s_{NN}}$ ) dependent  $\rho_{00}$  for 20-60% centrality Au+Au collisions using first (top) and second (bottom) order event planes. The BES-II results are slightly shifted horizontally. The vertical lines are statistical uncertainties and boxes represent systematic uncertainties. A fit to BES-I measurements between  $\sqrt{s_{NN}} = 19.6$  to 200 GeV is shown as a solid black curve, based on theoretical model in [2-6].  $G_s^{(y)}$  is the fitted parameter and is displayed with uncertainty. The black dashed line represents  $\rho_{00} = 1/3$ .

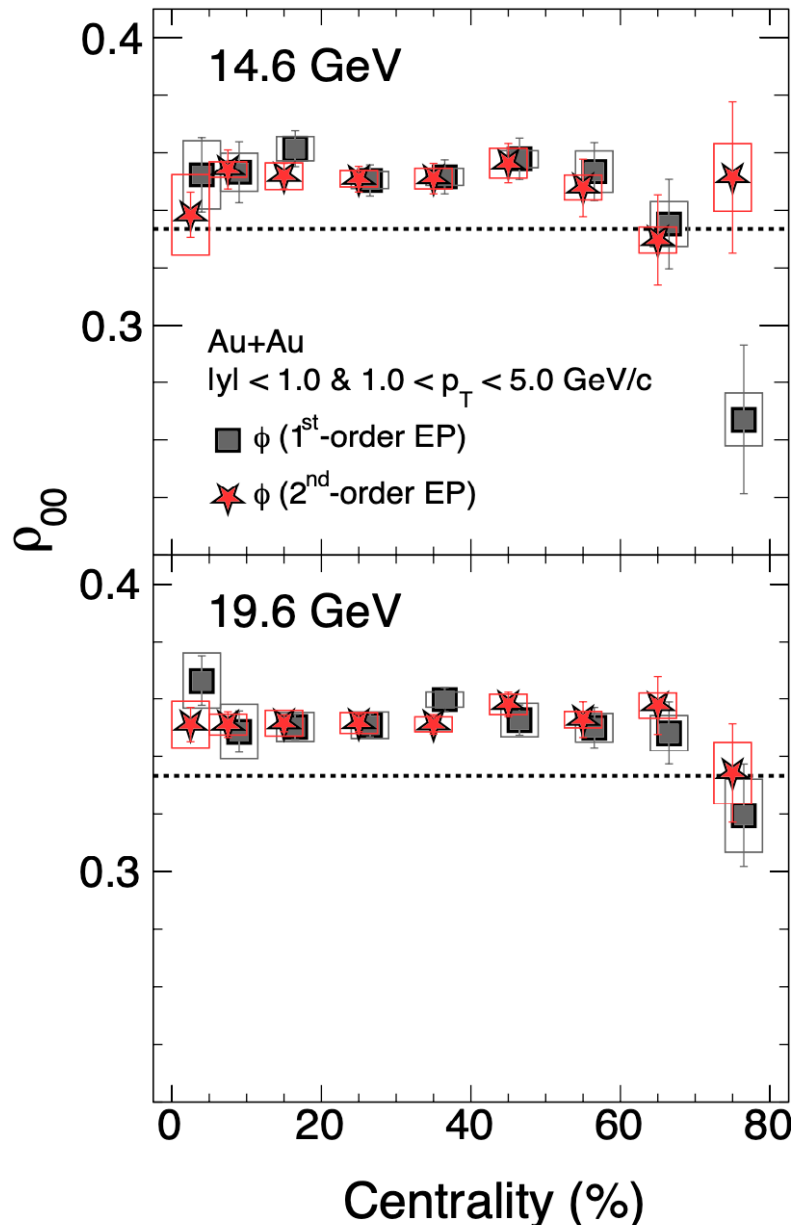


# Figure 2.



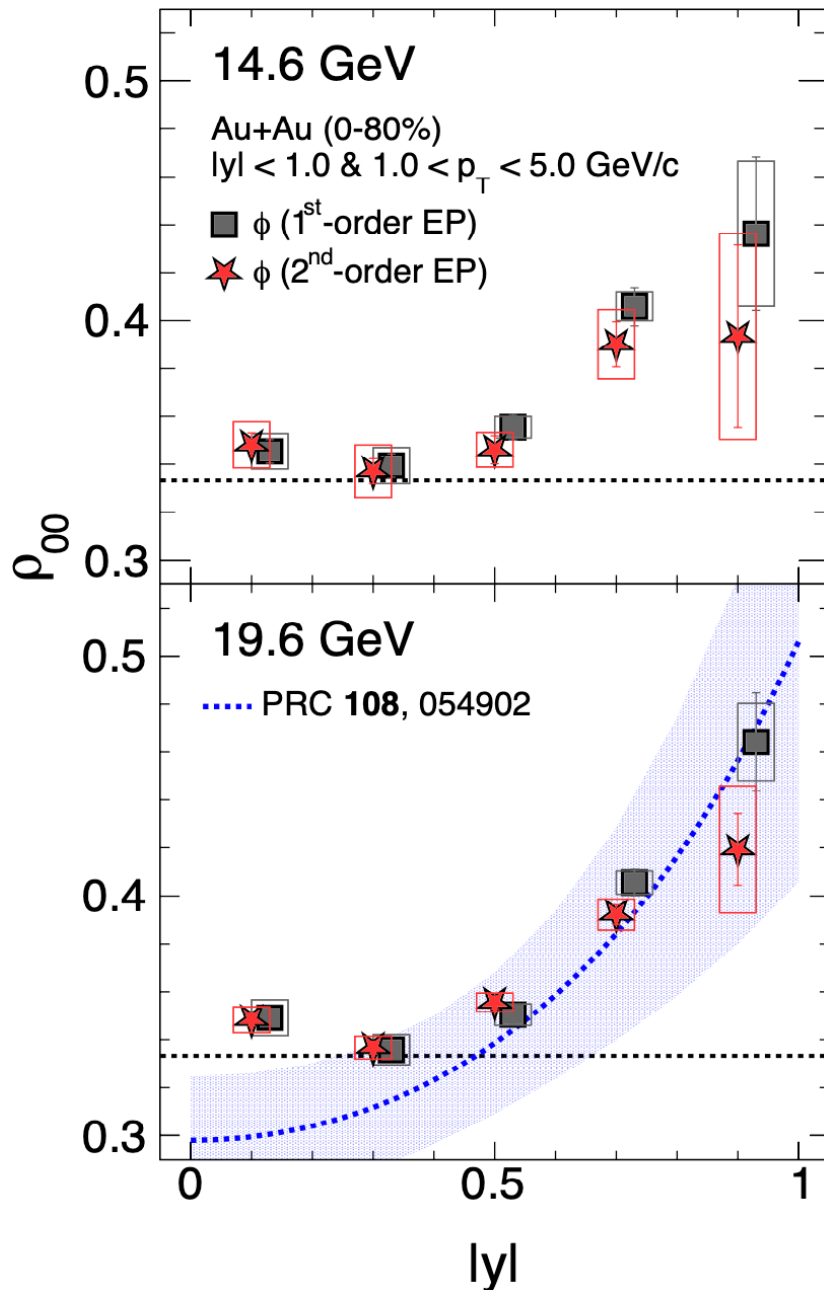
Transverse momentum ( $p_T$ ) dependent  $\rho_{00}$  with respect to the first and second order event planes for 20-60% centrality Au+Au collisions at  $\sqrt{s_{NN}} = 14.6$  (top) and 19.6 (bottom) GeV. The first order event plane results are slightly shifted horizontally. The vertical lines are statistical uncertainties and boxes represent systematic uncertainties. The black dashed line represents  $\rho_{00} = 1/3$ .

# Figure 3.



Centrality dependent  $\rho_{00}$  with respect to the first and second order event planes for Au+Au collisions at  $\sqrt{s_{NN}} = 14.6$  (top) and 19.6 (bottom) GeV. The first order event plane results are slightly shifted horizontally. The vertical lines are statistical uncertainties and boxes represent systematic uncertainties. The black dashed line represents  $\rho_{00} = 1/3$ .

# Figure 4.



Rapidity ( $|y|$ ) dependent  $\rho_{00}$  for 0-80% centrality Au+Au collisions at  $\sqrt{s_{NN}} = 14.6$  (top) and 19.6 (bottom) GeV. Results for  $\rho_{00}$  calculated with respect to the first and second order event plane are shown. The first order event plane results are slightly shifted horizontally. The vertical lines are statistical uncertainties and boxes represent systematic uncertainties. The theoretical prediction from [7] for 20-60% centrality and  $p_T = [1.2, 5.4]$  GeV/c is shown as a dashed blue line with a shaded band representing its uncertainty. The black dashed line represents  $\rho_{00} = 1/3$ .

X.L. Sheng et al. PRL **131**, 042304 (2023).

# Summary

- We change from residual background poly3 to poly1.
  - Residual background is now considered source of systematic.
- No concerning asymmetry in signed  $\cos(\theta^*)$  distributions.
- Non-flat rapidity input to simulation has a negligible effect on the final  $\rho_{00}$ .
- $\varphi$ - $\Psi_2$  dependent efficiency on/off and  $v_2$  on/off has a negligible effect on the final  $\rho_{00}$ .
- A larger more complete document will be put together with all our studies and finding.

# BACKUP

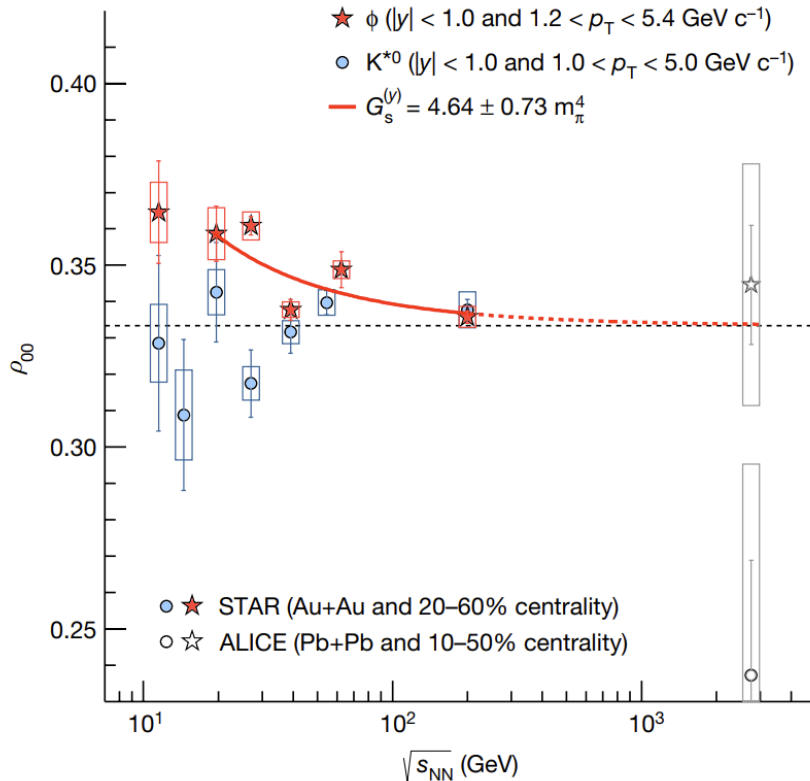
# Abstract

In this Letter, we report differential measurements of  $\phi$ -meson global spin alignment ( $\rho_{00}$ ) in Au+Au collisions at  $\sqrt{s_{NN}} = 14.6$  and 19.6 GeV in the second phase of the Beam Energy Scan at RHIC (BES-II) using the STAR detector. Following the STAR observation of  $\rho_{00} > 1/3$  for the  $\phi$ -meson at  $\sqrt{s_{NN}} \leq 62.4$  GeV from BES-I [1], this study aims to clarify the source of this  $\rho_{00}$  signal in the  $\phi$ -meson phase space using increased statistics available from BES-II. The first rapidity ( $y$ ) dependent  $\rho_{00}$  results for  $\phi$ -mesons are shown for  $\sqrt{s_{NN}} = 14.6$  and 19.6 GeV, in addition to new centrality and transverse momentum ( $p_T$ ) dependent measurements. After developments of a theoretical model with a connection to strong force fields [2-6], predictions of the rapidity dependence at  $\sqrt{s_{NN}} = 19.6$  GeV were calculated in [7] and are consistent with our measurements. The results reported in this Letter help solidify our understanding of  $\rho_{00}$  as a proxy measurement of vector meson fields, crucial components of the nuclear force.

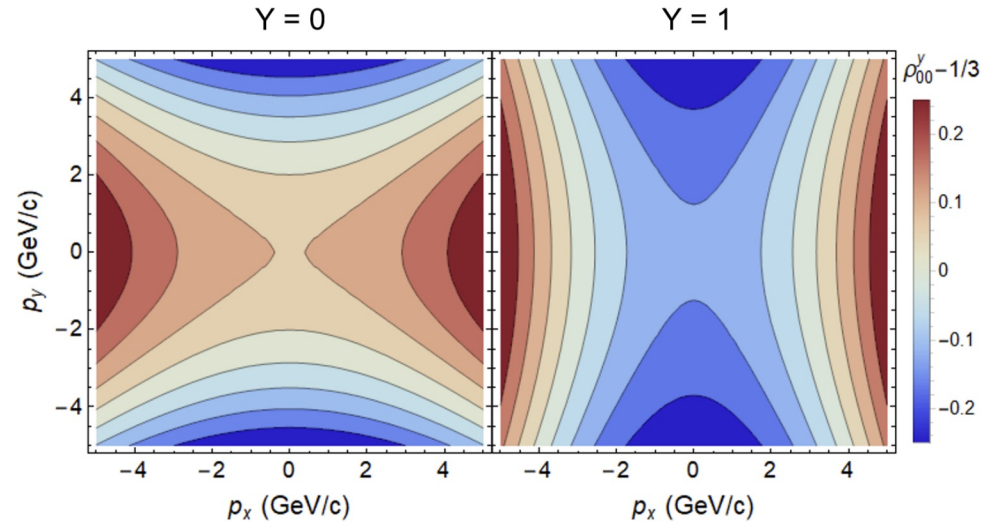
- [1] STAR Collaboration. Nature **614**, 244–248 (2023)
- [2] X.L. Sheng et al. PRD **101**, 096005 (2020).
- [3] X.L. Sheng et al. PRD **105**, 099903 (2022).
- [4] X.L. Sheng et al. PRD **102**, 056013 (2020).
- [5] X.L. Sheng et al. arXiv:2206.05868 [**hep-ph**] (2023).
- [6] X.L. Sheng et al. PRL **131**, 042304 (2023).
- [7] X.L. Sheng et al. arXiv:2308.14038 [**nucl-th**] (2023)

# Motivation

STAR Collaboration, Nature 614 (2023) 7947.



Sheng et al., arXiv:2308.14038 [nucl-th].



- Large positive global spin alignment ( $\rho_{00} > 1/3$ ) for  $\phi$ -meson was measured for the first time at mid-central collisions.
- Increased statistics for new and identical energies from BES-II.
  - Consistence with higher precision?
- Where does this large signal come from in the  $\phi$ -meson phase space?
- Can the leading theory predict the rapidity dependence?

# Analysis Information

- Dataset: Au+Au 19.6 GeV  
BES-II
  - Year: 2019
  - Production tag:  
production\_19GeV\_2019
  - Triggers used: 640001, 640011,  
640021, 640031, 640041,  
640051
  - Embedding request id:  
20214203, 20214204
  - Bad run list from  
StRefMultCorr
- Dataset: Au+Au 14.6 GeV  
BES-II
  - Year: 2019
  - Production tag:  
production\_14p5GeV\_2019
  - Triggers used: 650000
  - Embedding request id:  
20221502, 20221503
  - Bad run list from  
StRefMultCorr



# Analysis Information

## Event Level Cuts

- $|v_z| < 70$  cm
- $|v_r| < 2$  cm
- $n\text{BToFMatch} > 2$
- Pile-up rejection cuts from StRefMultCorr
- Centrality from StRefMultCorr

## TPC Track Cuts for $K^{+/-}$

- $0.1 < p_T < 10$  GeV/c
- $|\text{DCA}| < 2$  cm
- No. TPC hits  $> 15$
- TPC hit ratio  $> 0.52$
- $|\eta| < 1$

## PID Cuts for $K^{+/-}$

- $|\text{n}\sigma_K| < 2.5$
- ToF:  $0.16 < M^2 < 0.36$

$$\phi \rightarrow K^+ K^-$$

## EPD Event Plane Cuts (1<sup>st</sup> Order)

- Use StEpdEpFinder
- $v_1$  vs.  $\eta$  weighting as described here:  
<https://drupal.star.bnl.gov/STAR/blog/iupsal/determining-eta-weights-epd-event-plane-analysis>

## TPC Event Plane Cuts (2<sup>nd</sup> Order)

- $0.15 < p_T < 2$  GeV/c
- $|\text{DCA}| < 1$  cm
- No. TPC hits  $> 15$
- TPC hit ratio  $> 0.52$
- $|\eta| < 1$
- Sub-event plane method ( $\eta$  gap = 0.1)
- Apply run-by-run, centrality and  $v_z$  wise re-centering and shift calibrations

# Analysis Information

$$Q_n \cos(n\Psi_n) = \sum_i w_i \cos(n\varphi_i); \quad Q_n \sin(n\Psi_n) = \sum_i w_i \sin(n\varphi_i)$$

$$\Psi_n = \left( \tan^{-1} \frac{\sum_i w_i \sin(n\varphi_i)}{\sum_i w_i \cos(n\varphi_i)} \right) / n$$

$$R_1 = \sqrt{\langle \cos 2(\Psi_1 - \Psi_{1,r}) \rangle}$$

$$R_2 = \sqrt{\langle \cos 2(\Psi_2 - \Psi_{2,r}) \rangle}$$

$n$ : harmonic order in anisotropic flow distribution

$i$ :  $i^{\text{th}}$  particle in event

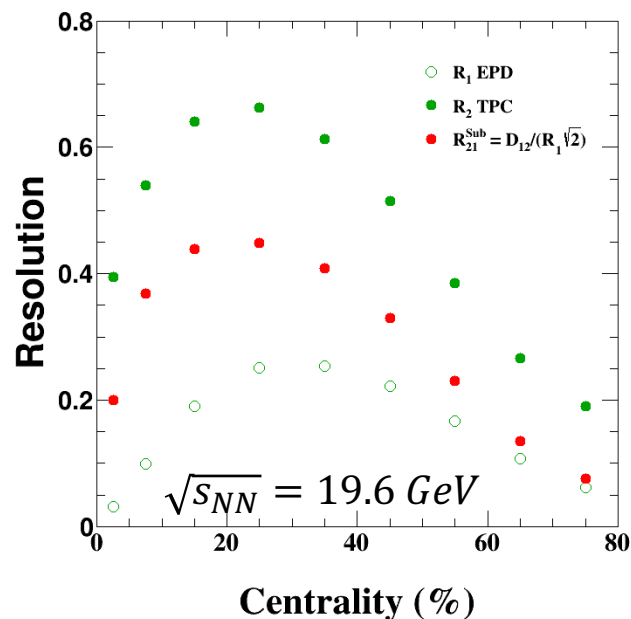
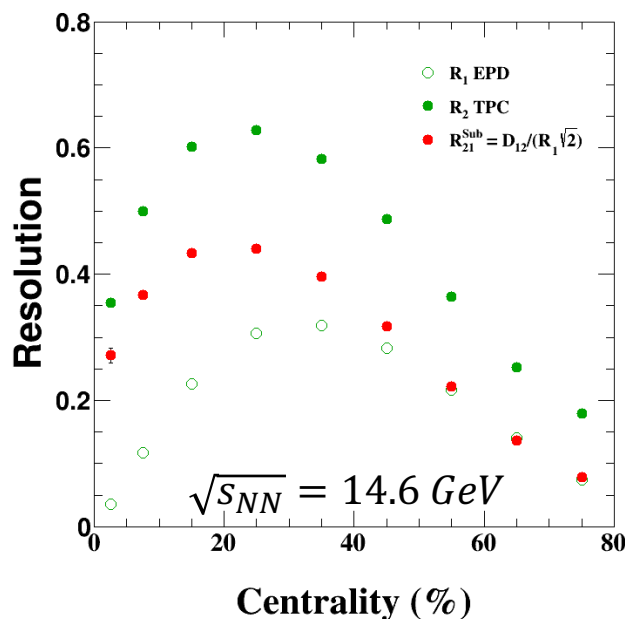
$Q_n$ : flow vector

$\varphi_i$ : angle of particle trajectory in lab frame

$w_i$ : weight (determined by transverse momentum)

if  $p_T < 2$  GeV/c,  $w_i = p_T$ ;      if  $p_T \geq 2$  GeV/c,  $w_i = 2$

See slide XX for information about deriving  $R_{21}^{\text{Sub}}$ .



# Technical Details

## Calculating $\rho_{00}$ from angular distribution of decay daughters:

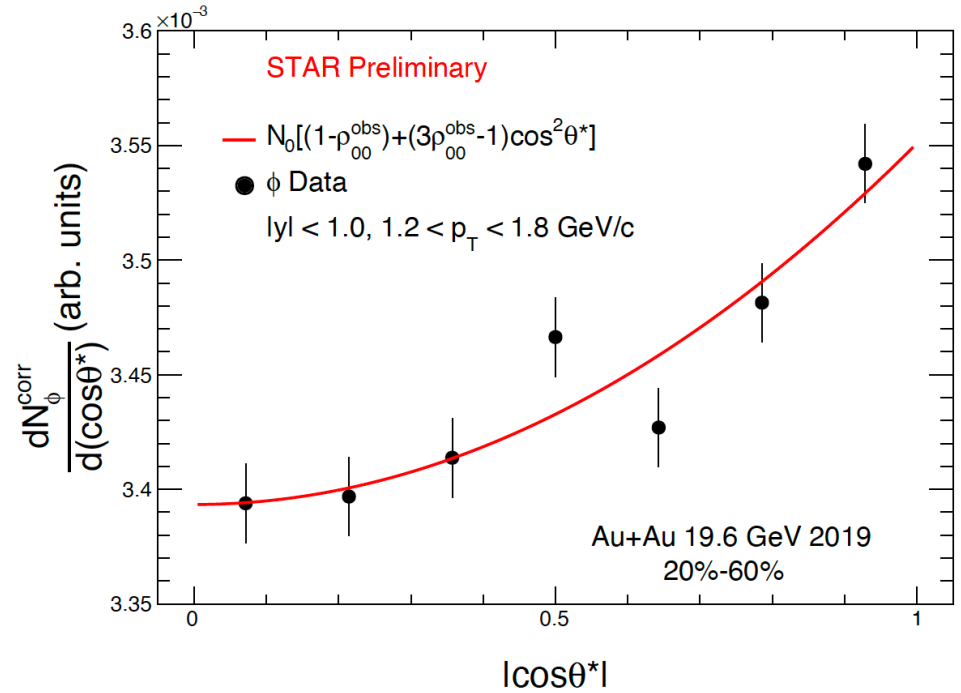
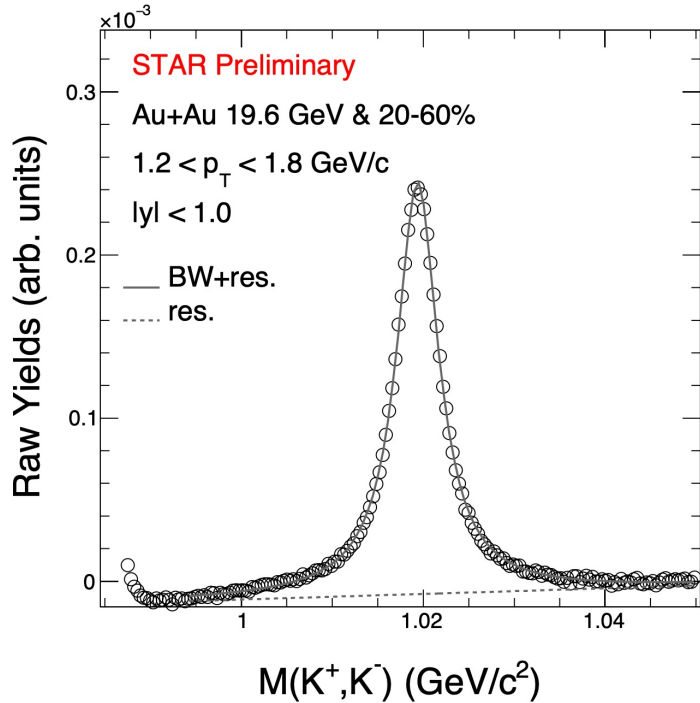
- Total  $\phi$  meson yield calculated for each  $\cos(\theta^*)$  bin.
- Correct yields for TPC tracking x ToF matching efficiency and acceptance.
  - Simulate  $\phi$  decay in Pythia6 and apply efficiency and acceptance cuts to decay daughters to find efficiency vs.  $\cos(\theta^*)$ .
- Event plane resolution ( $R_1$  or  $R_{21}^{\text{sub}}$ ) correction applied with following formula:

$$\rho_{00} = \frac{1}{3} + \frac{4}{1 + 3R} \left( \rho_{00}^{\text{obs}} - \frac{1}{3} \right)$$

Extra information regarding rapidity dependent  $\phi$ -meson  $\rho_{00}$  extraction and efficiency x acceptance corrections:

<https://drupal.star.bnl.gov/STAR/blog/gwilks3/Preliminary-Request-Details-phi-meson-global-spin-alignment>

# Technical Details



- Event-mixing is used to subtract background and extract yields from histogram integration in seven  $|\cos\theta^*|$  bins using Breit-Wigner + poly3 residual background:

- $\frac{1}{2\pi} \frac{AF}{(m-m_\phi)+(\Gamma/2)^2} + poly3(m)$

- Yields vs.  $|\cos\theta^*|$  are corrected for the geometric acceptance and tracking/PID efficiencies from previous slide.

- $\rho_{00}^{obs}$  is extracted from a fit to the corrected yields vs.  $|\cos\theta^*|$ :  $\frac{dN}{d\cos\theta^*} = N_0 \times [(1 - \rho_{00}^{obs}) + (3\rho_{00}^{obs} - 1)\cos^2\theta^*]$

All the plots for each step of this analysis have been posted to the following blog page:

<https://drupal.star.bnl.gov/STAR/blog/gwilks3/φ-meson-Global-Spin-Alignment-Step-Step-Analysis-Details>

# EP Resolution and Acceptance Correction

- To ensure  $\rho_{00}$  with respect to the 2<sup>nd</sup> order EP is consistent with  $\rho_{00}$  with respect to the 1<sup>st</sup> order EP one must use the 2<sup>nd</sup> order EP “resolution” with respect to the reaction plane that the 1<sup>st</sup> order EP is perturbing around.

$$R_{21} = \langle \cos 2(\Psi_2 - \Psi_{r,1}) \rangle$$

- $R_{21}$  can be found by using the following relation.

$$\begin{aligned} D_{12} &\equiv \langle \cos 2(\Psi_1 - \Psi_2) \rangle \\ &= \langle \cos 2(\Psi_1 - \Psi_{r,1} + \Psi_{r,1} - \Psi_2) \rangle \\ &\approx \langle \cos 2(\Psi_1 - \Psi_{r,1}) \rangle \langle \cos 2(\Psi_{r,1} - \Psi_2) \rangle \\ &= R_1 \cdot R_{21}. \end{aligned}$$

- Since we are using the 2<sup>nd</sup> order **sub-event** plane for our  $\rho_{00}$  calculations, we must use  $R_{21}^{Sub}$  instead.

$$R_{21}^{Sub} = R_{21}/\sqrt{2}$$

# $\phi$ -meson $\rho_{00}$ vs $p_T$ : Systematics

1. Choose central values for each source of systematic error.
2. Vary one cut at a time while keeping the others at the default value. Vary yield extraction method for non-default cuts. Calculate  $\rho_{00}$  for each variation and calculate the sources error with:

$$\Delta\rho_{00,sys}^i = \frac{\rho_{00,max}^i - \rho_{00,min}^i}{\sqrt{12}}$$

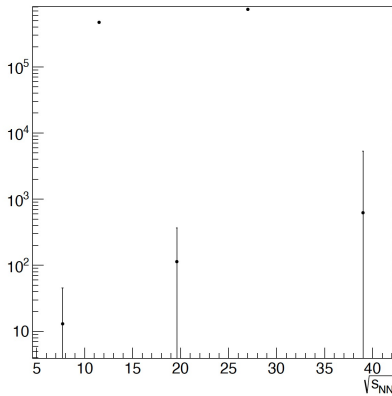
3. Combine all sources of systematics:

$$\Delta\rho_{00,sys} = \sqrt{\sum_i (\Delta\rho_{00,sys}^i)^2}$$

# Au+Au 14.6 GeV $p_T$ spectra interpolation

$$\frac{1}{2\pi m_T} \frac{d^2N}{dm_T dy} = \frac{dN/dy(n-1)(n-2)}{2\pi n T_{\text{Levy}}(n T_{\text{Levy}} + m_0(n-2))} \times \left(1 + \frac{m_T - m_0}{n T_{\text{Levy}}}\right)^{-n},$$

- Using Lévy function for interpolation is difficult due to parameter  $n$  varying too much energy to energy.
- Function used for sampling  $p_T$  in 19.6 GeV simulations.



$$\frac{1}{2\pi m_T} \frac{d^2N}{dm_T dy} = \frac{dN/dy}{2\pi T_{\text{exp}}(m_0 + T_{\text{exp}})} e^{-(m_T - m_0)/T_{\text{exp}}},$$

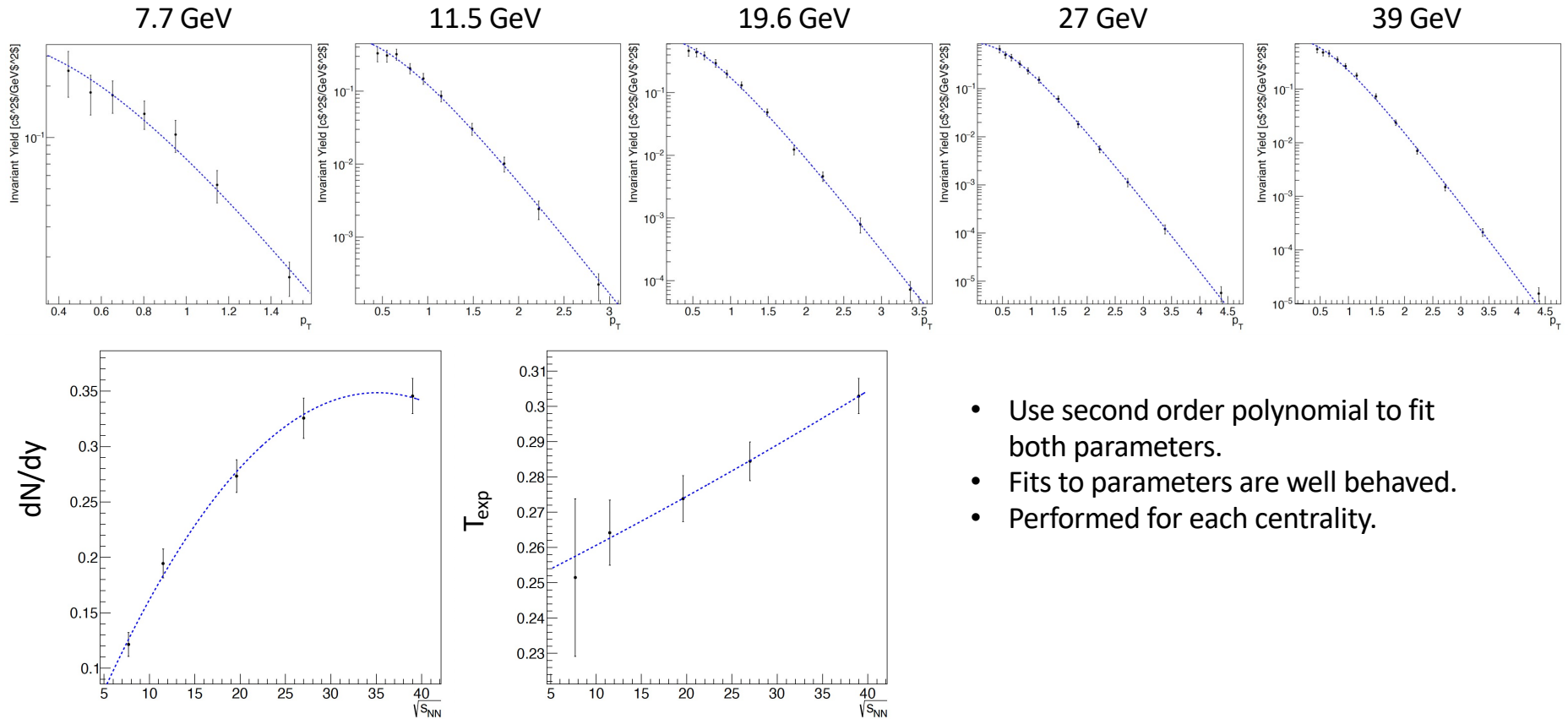
- In exponential function we have two well behaved parameters ( $dN/dy$ ) and  $T_{\text{exp}}$
- This will be used for extrapolation.
- Fit the distributions of the two parameters as a function of collision energy.
  - We really only need  $T_{\text{exp}}$  since  $dN/dy$  is just a normalization and we just want the shape.
- Then we can just grab the interpolated parameters for 14.6 GeV and generate the spectra for simulation.

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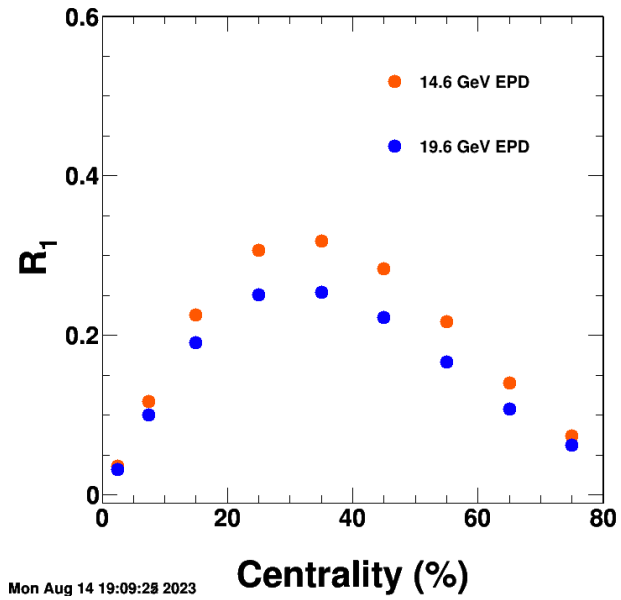
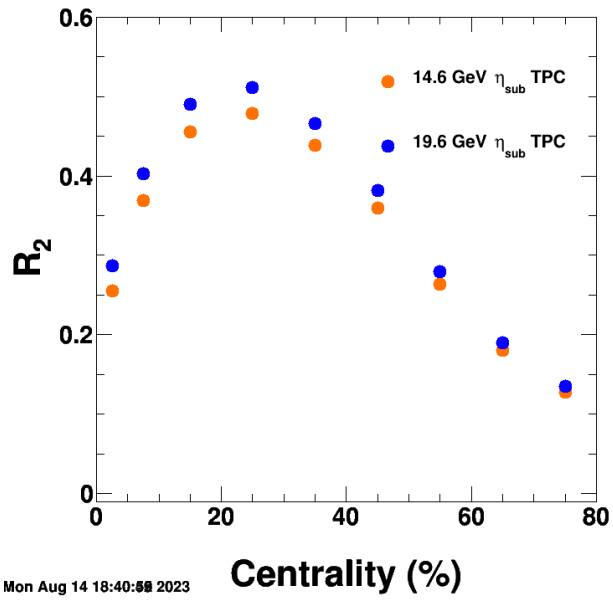


# Au+Au 14.6 GeV $p_T$ spectra interpolation

10-20% centrality



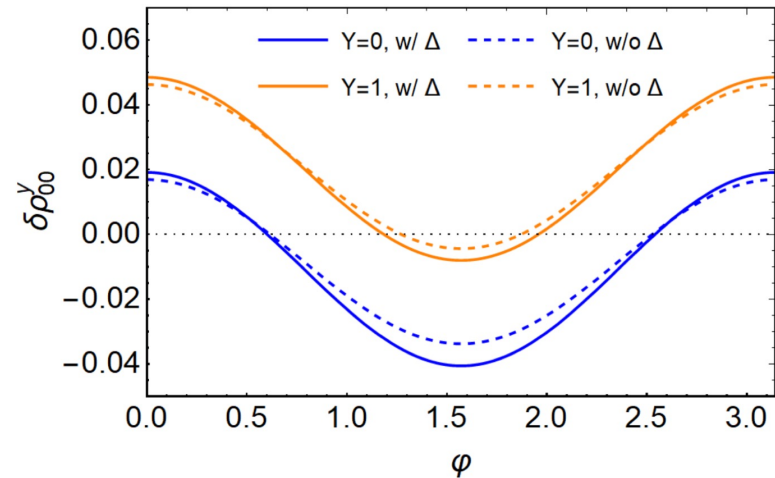
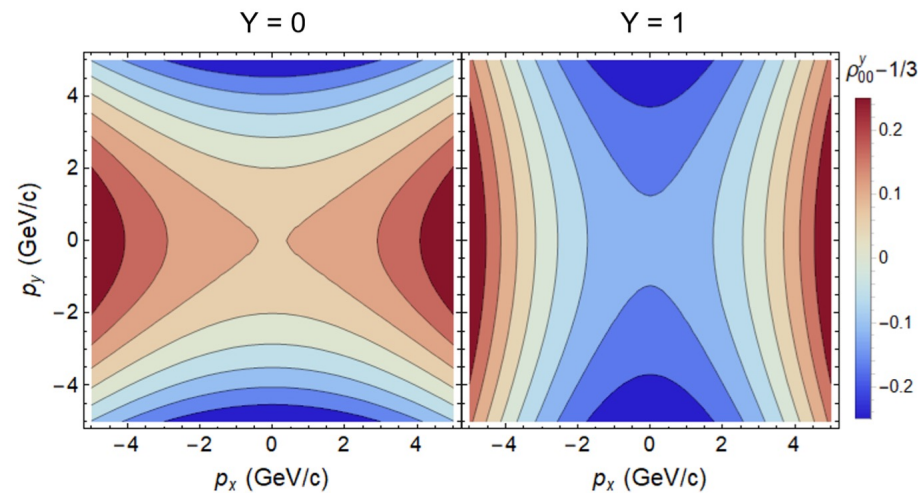
- Use second order polynomial to fit both parameters.
- Fits to parameters are well behaved.
- Performed for each centrality.



# Theory Predictions

- Motion of the  $\phi$ -meson in the lab frame induces anisotropy of field fluctuations in  $\phi$ -meson rest frame perpendicular to the motion.

$$\langle \delta \rho_{00}^y \rangle (\mathbf{p}) \propto \frac{1}{2} p_T^2 [3 \cos(2\varphi) - 1] + \sqrt{m_\phi^2 + p_T^2} \sinh^2 Y.$$

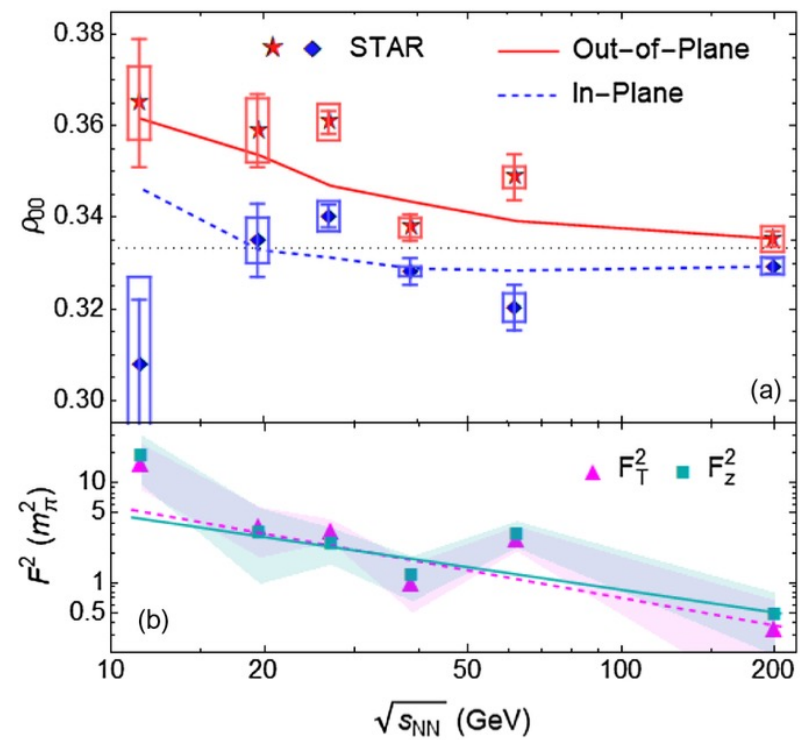


# Theory Uncertainty

From Xin-Li Sheng on uncertainty calculations:

1. By fitting center values for  $\rho_{00}^y$  and  $\rho_{00}^x$ , we obtain the center values for parameters  $F_T^2$  and  $F_z^2$ . Since we have two parameters and two results, there is no calculation uncertainty in this process.
2. In a similar way, we calculate  $F_T^2$  and  $F_z^2$  using  $(\rho_{00}^y \pm \sigma_y)$  and  $(\rho_{00}^x \pm \sigma_x)$ , where  $\sigma$  denotes the total uncertainty, given by the STAR's paper. So we obtain four sets of parameters. For each parameter, we take the maximum value among these sets as the upper limit for the uncertainty band, and take the minimum value as the lower limit.
3. Using the above four sets of parameters, we calculate  $\rho_{00}$  as a function of rapidity and obtain four results. Again, we take the maximum (minimum) value as the upper (lower) limit for the uncertainty band.”

X.L. Sheng et al. PRL 131, 042304 (2023).



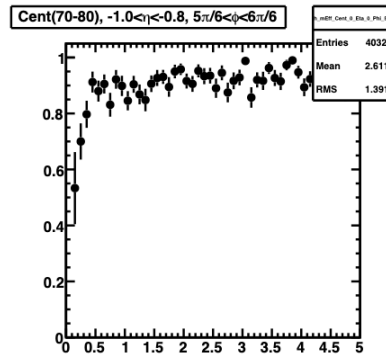
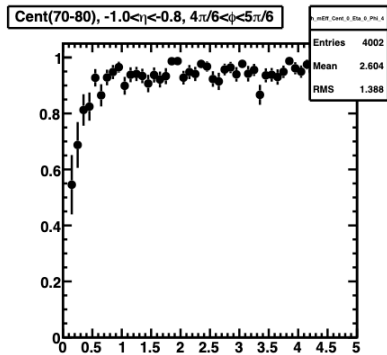
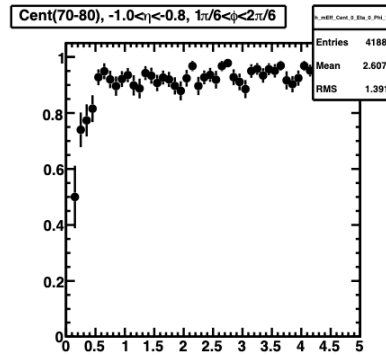
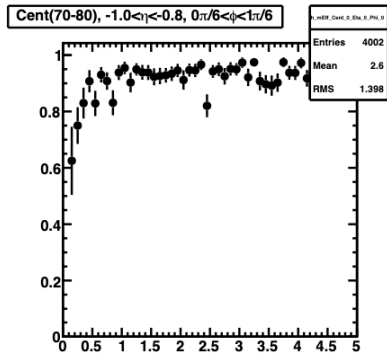
$$\rho_{00}(x, \mathbf{k}) \approx \frac{1}{3} + \underbrace{C_1 \left[ \frac{1}{3} \boldsymbol{\omega}' \cdot \boldsymbol{\omega}' - (\boldsymbol{\epsilon}_0 \cdot \boldsymbol{\omega}')^2 \right]}_{\text{vorticity contributions are negligible}} - \underbrace{C_2 \left[ \frac{1}{3} \boldsymbol{\epsilon}' \cdot \boldsymbol{\epsilon}' - (\boldsymbol{\epsilon}_0 \cdot \boldsymbol{\epsilon}')^2 \right]} - \frac{4g_\phi^2}{m_\phi^2 T_h^2} C_1 \left[ \frac{1}{3} \mathbf{B}'_\phi \cdot \mathbf{B}'_\phi - (\boldsymbol{\epsilon}_0 \cdot \mathbf{B}'_\phi)^2 \right] - \frac{4g_\phi^2}{m_\phi^2 T_h^2} C_2 \left[ \frac{1}{3} \mathbf{E}'_\phi \cdot \mathbf{E}'_\phi - (\boldsymbol{\epsilon}_0 \cdot \mathbf{E}'_\phi)^2 \right],$$

$$\langle (g_\phi \mathbf{B}_{x,y}^\phi / T_h)^2 \rangle = \langle (g_\phi \mathbf{E}_{x,y}^\phi / T_h)^2 \rangle \equiv F_T^2$$

$$\langle (g_\phi \mathbf{B}_z^\phi / T_h)^2 \rangle = \langle (g_\phi \mathbf{E}_z^\phi / T_h)^2 \rangle \equiv F_z^2$$

# TPC Tracking Efficiency

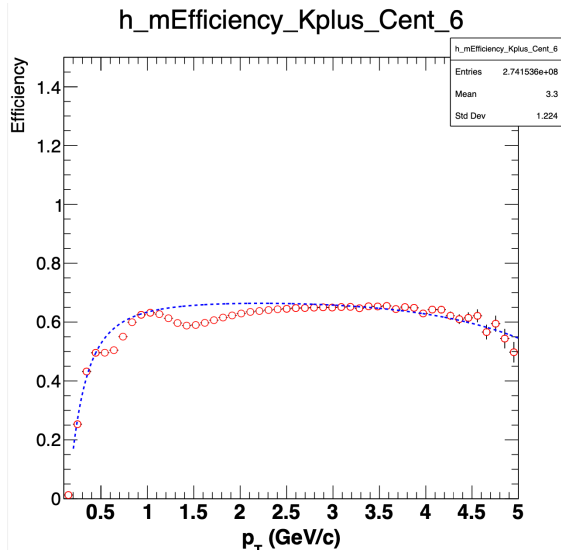
- From Embedding
- RC/MC vs  $p_T$
- Apply all event level cuts before track level cuts.
- RC tracks must pass all TPC track cuts.



Binning:

- $\eta$  bin edges =  $[-1.0, -0.8, -0.6, -0.4, -0.2, 0.0, 0.2, 0.4, 0.6, 0.8, 1.0]$
- $\phi$  bin edges =  $[-\pi, -5\pi/6, -4\pi/6, -3\pi/6, -2\pi/6, -\pi/6, 0, \pi/6, 2\pi/6, 3\pi/6, 4\pi/6, 5\pi/6, \pi]$
- Centrality bin edges =  $[0, 5, 10, 20, 30, 40, 50, 60, 70, 80]$  %
- $p_T$  has 50 equal width bins from 0.0 to 5.0 GeV/c

# ToF Matching Efficiency



- From data: [number of tracks that pass TPC track cut,  $n_{\sigma, K^{+/-}} < 0.4$ , and have a ToF Match ( $\beta > 0$ )]/[number of tracks that pass just TPC track cuts and  $n_{\sigma, K^{+/-}} < 0.4$ ] ( $N_{\text{ToF}}/N_{\text{TPC}}$ ).
  - We apply tight  $n_{\sigma, K^{+/-}}$  cut to ensure TPC tracks are mostly  $K^{+/-}$ .
- Apply all event level cuts before track level cuts.
- We use fit to distribution as input to simulation for  $p_T > 0.3$  GeV/c and histogram values for  $p_T \leq 0.3$  GeV/c.
- Fit Function:  $p_0 \left[ \left( \frac{1}{(p_T - p_1)^2 + p_2} \right) - \left( \frac{p_4}{e^{p_T - p_3} + p_5} \right) + p_6 \right]$
- We do not fit the regions at  $p_T \sim [0.4, 0.8]$  and  $\sim [1.2, 2.5]$  due to known hadron contamination effect causing artificial dips in the ToF Matching efficiency. These  $p_T$  windows are manually shifted.
- We first fit the  $p_T$  distributions integrated over all  $\phi$  and  $\eta$  bins.
- Then fit the distributions for each  $\eta$  bin integrated over  $\phi$ .
- Fix all parameters except for the normalization from the above fit. Fit distribution to the tail end of each  $\phi$ -bin for correct normalization.

## Binning:

- $\eta$  bin edges = [-1.0, -0.8, -0.6, -0.4, -0.2, 0.0, 0.2, 0.4, 0.6, 0.8, 1.0]
- $\phi$  bin edges = [- $\pi$ , -5 $\pi/6$ , -4 $\pi/6$ , -3 $\pi/6$ , -2 $\pi/6$ , - $\pi/6$ , 0,  $\pi/6$ , 2 $\pi/6$ , 3 $\pi/6$ , 4 $\pi/6$ , 5 $\pi/6$ ,  $\pi$ ]
- Centrality bin edges = [0, 5, 10, 20, 30, 40, 50, 60, 70, 80] %
- $p_T$  has 50 equal width bins from 0.0 to 5.0 GeV/c

# Inputs to Simulation ( $v_2$ , $p_T$ spectra)

These are some examples of the distributions used to generate the  $\phi$ -meson kinematics in simulation. See webpage on title slide for more.

14.6 GeV  $v_2$  distributions are from preliminary BES-II results.

19.6 GeV  $v_2$  distributions are from published BES-I results.

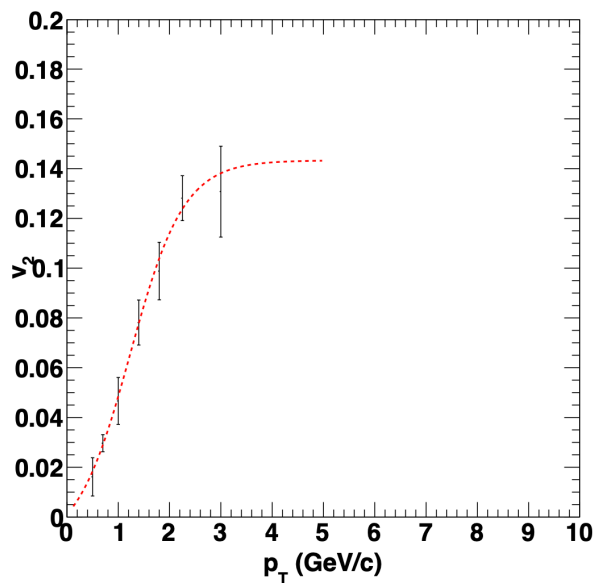
14.6 GeV  $p_T$  spectra are interpolated from published results.

19.6 GeV  $p_T$  spectra are from published results.

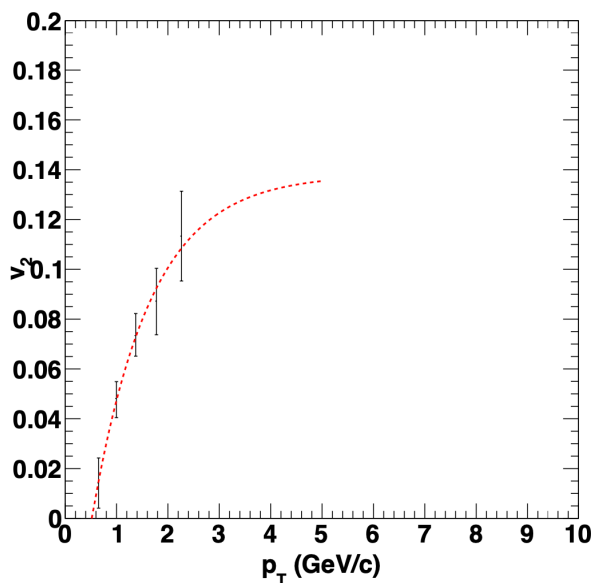
Rapidity spectra are still in progress in the LFS UPC PWG. We use a flat rapidity spectra.

19.6 GeV 30-40% Centrality

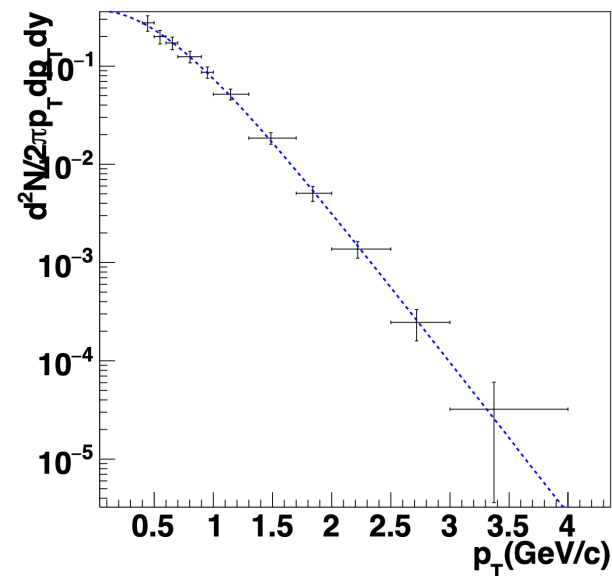
14.6 GeV 10-40% Centrality



19.6 GeV 10-40% Centrality



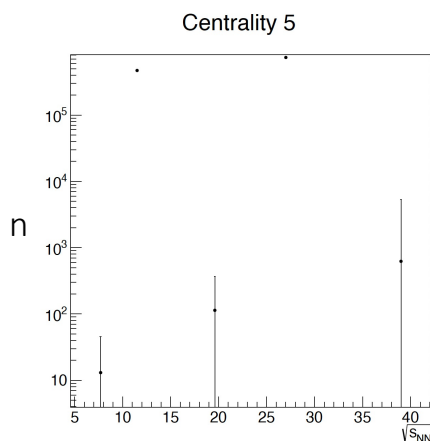
doi:10.17182/hepdata.72068.v1/t16



# Au+Au 14.6 GeV $p_T$ spectra interpolation

$$\frac{1}{2\pi m_T} \frac{d^2N}{dm_T dy} = \frac{dN/dy(n-1)(n-2)}{2\pi n T_{\text{Levy}}(n T_{\text{Levy}} + m_0(n-2))} \times \left(1 + \frac{m_T - m_0}{n T_{\text{Levy}}}\right)^{-n},$$

- Using Lévy function for interpolation is difficult due to parameter  $n$  varying too much energy to energy.
- Function used for sampling  $p_T$  in 19.6 GeV simulations.



$$\frac{1}{2\pi m_T} \frac{d^2N}{dm_T dy} = \frac{dN/dy}{2\pi T_{\text{exp}}(m_0 + T_{\text{exp}})} e^{-(m_T - m_0)/T_{\text{exp}}},$$

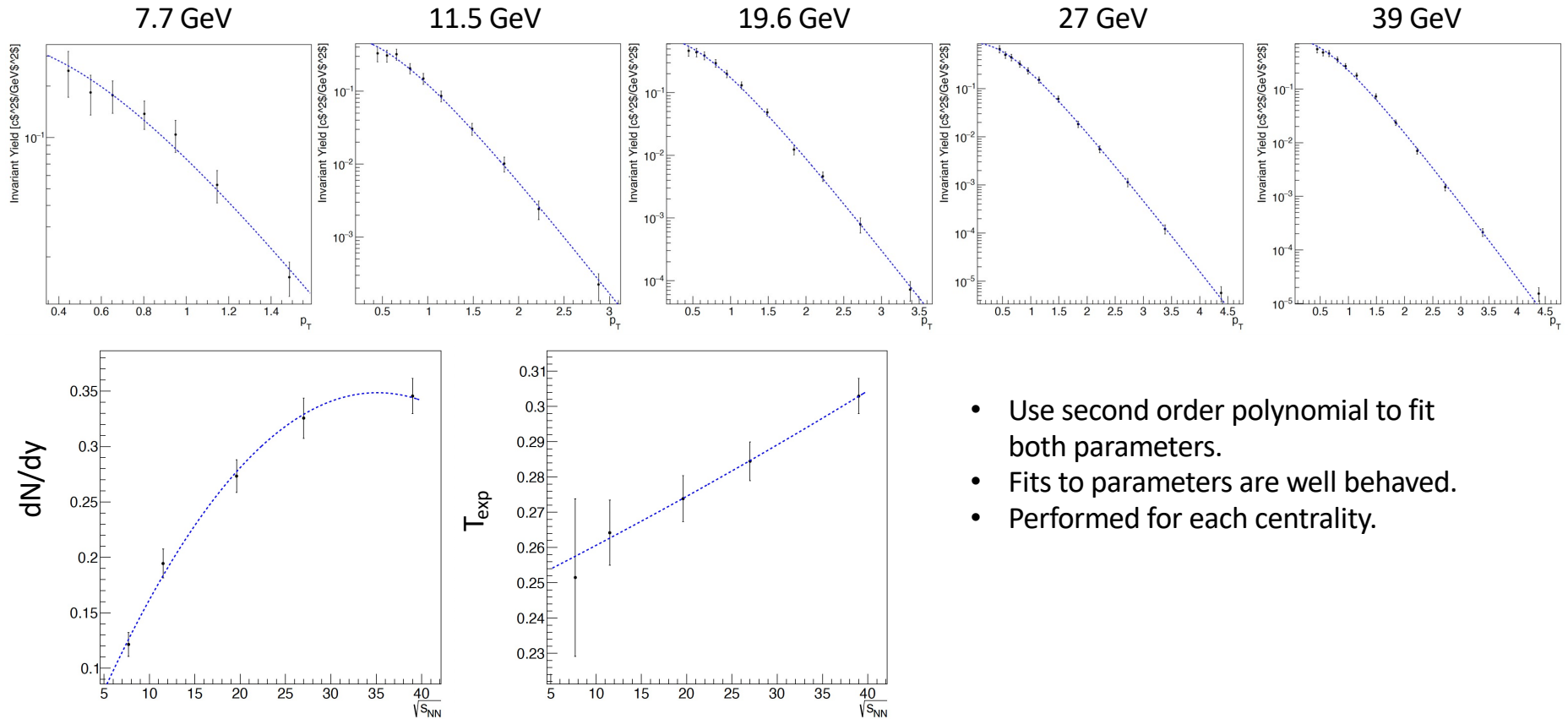
- In exponential function we have two well behaved parameters ( $dN/dy$ ) and  $T_{\text{exp}}$
- This will be used for extrapolation.
- Fit the distributions of the two parameters as a function of collision energy.
  - We really only need  $T_{\text{exp}}$  since  $dN/dy$  is just a normalization and we just want the shape.
- Then we can just grab the interpolated parameters for 14.6 GeV and generate the spectra for simulation.

PHYSICAL REVIEW C **79**, 064903 (2009)



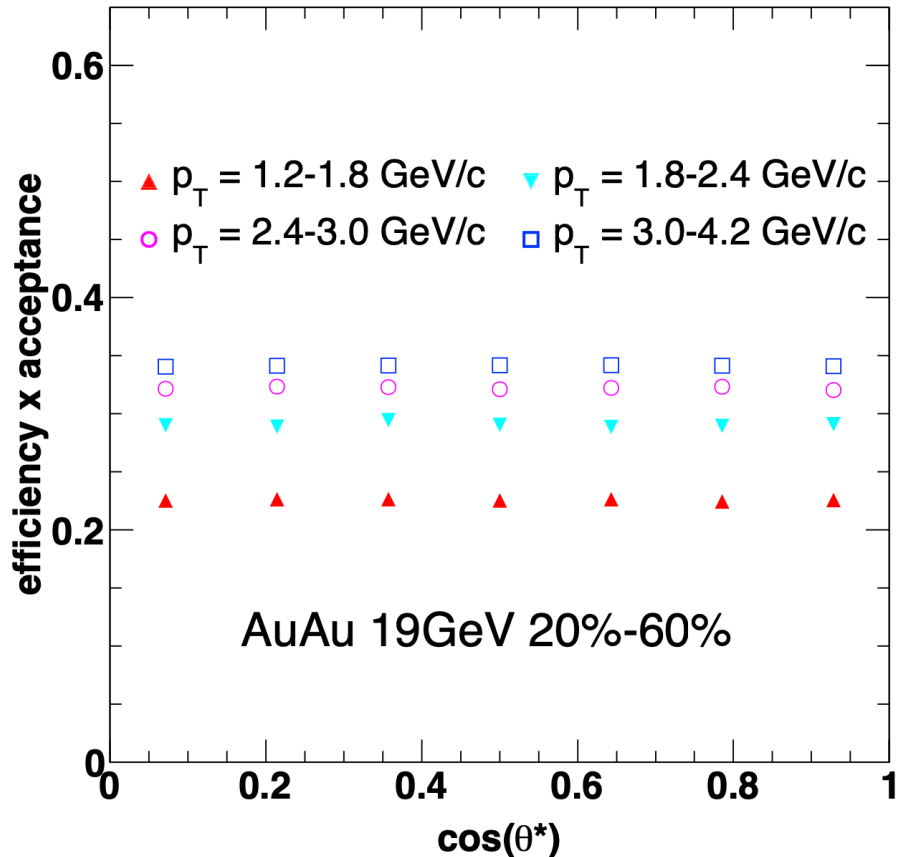
# Au+Au 14.6 GeV $p_T$ spectra interpolation

10-20% centrality



- Use second order polynomial to fit both parameters.
- Fits to parameters are well behaved.
- Performed for each centrality.

# Technical Details



- Use Pythia6 to decay
- MC  $\phi$  input flat in rapidity
  - $p_T$  from spectra or interpolated
  - $\phi$  from  $v_2$  distribution.
- Drop tracks using TPC tracking and ToF matching efficiency of  $K^+$  and  $K^-$  in each  $\eta$  &  $\phi$  bin.
- If both kaons pass efficiency cuts and  $\eta$  acceptance cut, reconstruct  $\phi$  meson.
- Smear EP according to known EP resolution in each centrality.
- Fill histogram for RC and MC counts in each  $\cos(\theta^*)$  bin.

# Conclusions

- Results are consistent for 1<sup>st</sup> and 2<sup>nd</sup> order event planes.
- BES-I and BES-II integrated  $\rho_{00}$  for mid-central collisions are consistent for 19.6 GeV and we report higher precision.
- We show the  $p_T$  and centrality dependent  $\rho_{00}$ .
- Rapidity dependent results show an increasing trend with  $\rho_{00} \sim 1/3$  at  $|y| = 0$  and  $\rho_{00} > 1/3$  signal at  $|y| = 1$ .
  - Consistent with theory predictions in [1].
  - Motion of  $\phi$ -meson induces anisotropy of field fluctuations perpendicular to motion, resulting in larger  $\rho_{00}$  in this perpendicular plane [2].

[1] X.L. Sheng et al. PRL **131**, 042304 (2023).

[2] X.L. Sheng et al. arXiv:2308.14038 [nucl-th] (2023).